

Chapter 1

Basic Algebraic Operations

1.1 Numbers

1.

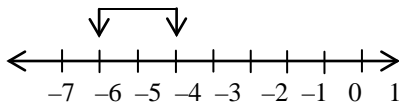
The numbers -3 and 14 are integers. They are also rational numbers since they can be written as $\frac{-3}{1}$ and $\frac{14}{1}$.

2.

The absolute value of -6 is 6 , and the absolute value of -7 is 7 . We write these as $|-6| = 6$ and $|-7| = 7$.

3.

$-6 < -4$; -6 is to the left of -4 .



4.

The reciprocal of $\frac{3}{2}$ is $\frac{1}{\frac{3}{2}} = 1 \times \frac{2}{3} = \frac{2}{3}$.

5.

3 is an integer, rational $\left(\frac{3}{1}\right)$, and real.

$\sqrt{-4}$ is imaginary.

$-\frac{\pi}{6}$ is irrational (because π is an irrational number) and real.

6.

$-\sqrt{-6}$ is imaginary.

$-2.33 = \frac{-233}{100}$ is rational and real.

$\frac{\sqrt{7}}{3}$ is irrational (because $\sqrt{7}$ is an irrational number) and real.

7.

$$|3| = 3$$

$$|-4| = 4$$

$$\left|-\frac{\pi}{2}\right| = \frac{\pi}{2}$$

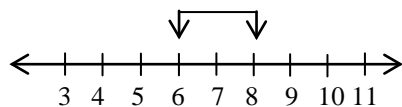
8.

$$|-0.857| = 0.857$$

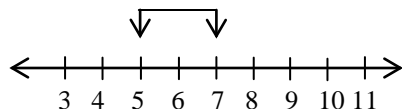
$$|\sqrt{2}| = \sqrt{2}$$

$$\left|-\frac{19}{4}\right| = \frac{19}{4}$$

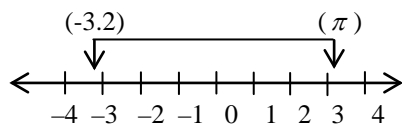
9.

 $6 < 8$; 6 is to the left of 8.

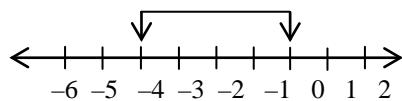
10.

 $7 > 5$; 7 is to the right of 5.

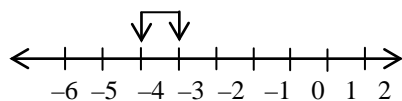
11.

 $\pi > -3.2$; π (3.14159...) is to the right of -3.2 .

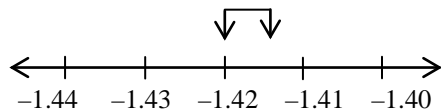
12.

 $-4 < 0$; -4 is to the left of 0.

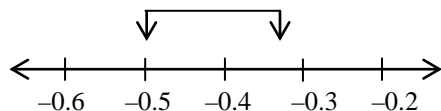
13.

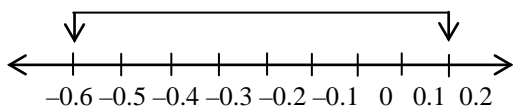
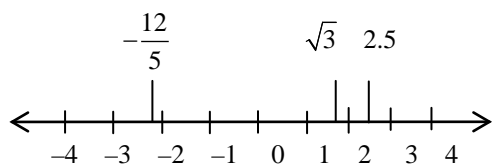
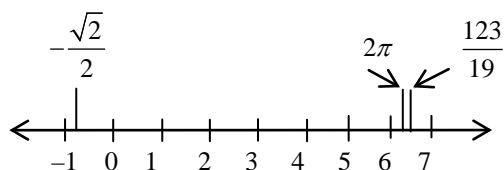
 $-4 < -|-3|$; -4 is to the left of $-|-3|$, ($-|-3| = -(3) = -3$).

14.

 $-\sqrt{2} > -1.42$; $(-\sqrt{2} = -(1.414\dots) = -1.414\dots)$, $-\sqrt{2}$ is to the right of -1.42 .

15.

 $-\frac{1}{3} > -\frac{1}{2}$; $-\frac{1}{3} = -0.33\dots$ is to the right of $-\frac{1}{2} = -0.5$.

16. $-0.6 < 0.2$; -0.6 is to the left of 0.2 .**17.**The reciprocal of 3 is $\frac{1}{3}$.The reciprocal of $-\frac{4}{\sqrt{3}}$ is $-\frac{1}{\frac{4}{\sqrt{3}}} = -\frac{\sqrt{3}}{4}$.The reciprocal of $\frac{y}{b}$ is $\frac{1}{\frac{y}{b}} = \frac{b}{y}$.**18.**The reciprocal of $-\frac{1}{3}$ is $-\frac{1}{\frac{1}{3}} = -\frac{3}{1} = -3$.The reciprocal of $-0.25 = -\frac{1}{4}$ is $-\frac{1}{\frac{1}{4}} = -\frac{4}{1} = -4$.The reciprocal of x is $\frac{1}{x}$.**19.**Find 2.5 , $-\frac{12}{5} = -2.4$; $\sqrt{3} = 1.732\dots$ **20.**Find $-\frac{\sqrt{2}}{2} = -\frac{1.414\dots}{2} = -0.707$; $2\pi = 2 \times 3.14\dots = 6.28$; $\frac{123}{19} = 6.47$.**21.**An absolute value is not always positive, $|0| = 0$ which is not positive.

22.

Since $2.17 = \frac{217}{100}$, it is rational.

23.

The reciprocal of the reciprocal of any positive or negative number is the number itself.

The reciprocal of n is $\frac{1}{n}$; the reciprocal of $\frac{1}{n}$ is $\frac{1}{\frac{1}{n}} = 1 \cdot \frac{n}{1} = n$.

24.

A rational number can be expressed as a fraction of integers. So if the denominator in the fraction must be 11, then find the integer x so that $-1.0 < \frac{x}{11} < -0.9$. If $x = -11$, it would equal the lower limit $\frac{-11}{11} = -1.0$. So it must be an integer larger than -11 . If $x = -10$, then $\frac{-10}{11} = -0.90909\dots$, which is rational.

25.

A rational number can be expressed as a fraction of integers. So, if the numerator in the fraction must be 3, then find the integer x , so that $0.13 < \frac{3}{x} < 0.14$. So $0.13 = \frac{13}{100}$, and we can find the equivalent fraction of $\frac{13}{100}$ that has 3 as a numerator by rearranging and solving the following equation:

$$\frac{13}{100} = \frac{3}{x}$$

$$13(x) = 100 \times 3$$

$$x = \frac{300}{13}$$

$$x = 23.077$$

$$0.13 = \frac{3}{23.077}$$

However, since x must be an integer and less than the answer above to make our fraction with the numerator of 3 greater than 0.13, we assign 23 to x , making $\frac{3}{23} = 0.1304$, which is rational. $0.13 < 0.1304 < 0.14$.

26.

No, $|b - a| = |b| - |a|$, as shown below.

If $a > 0$, then $|a| = a$.

If $b > a$ and $a > 0$, then $|b| = b$.

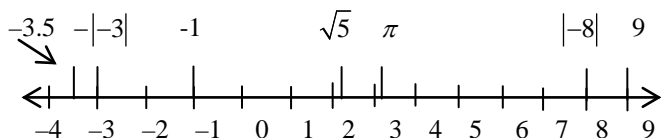
If $b > a$ then $b - a > 0$, then $|b - a| = b - a$.

Therefore, $|b - a| = b - a = |b| - |a|$.

The two sides of the expression are equivalent, one side is not less than the other.

27.

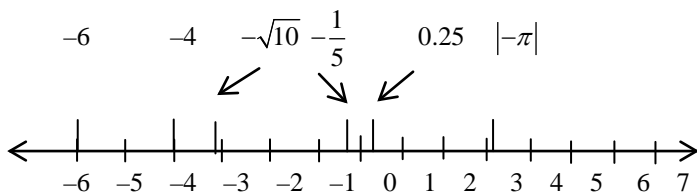
List these numbers from smallest to largest: -1 , 9 , $\pi = 3.14$, $\sqrt{5} = 2.236$, $|-8| = 8$, $-|-3| = -3$, -3.5 .



So, from smallest to largest, they are -3.5 , $-|-3|$, -1 , $\sqrt{5}$, π , $|-8|$, 9 .

28.

List these numbers from smallest to largest: $-\frac{1}{5} = -0.20$, $-\sqrt{10} = -3.16$, $-|-6| = -6$, -4 , 0.25 , $|\pi| = 3.14$.



So, from smallest to largest, they are $-|-6|$, -4 , $-\sqrt{10}$, $-\frac{1}{5}$, 0.25 , $|\pi|$.

29.

If a and b are positive integers and $b > a$, then

- (a) $b - a$ is a positive integer.
- (b) $a - b$ is a negative integer.
- (c) $\frac{b-a}{b+a}$, the numerator and denominator are both positive, but the numerator is less than the denominator, so the answer is a positive rational number that is less than 1.

30.

If a and b are positive integers, then

- (a) $a + b$ is a positive integer
- (b) a / b is a positive rational number
- (c) $a \times b$ is a positive integer

31.

(a) Is the absolute value of a positive or a negative integer always an integer?

$|x| = x$, so the absolute value of a positive integer is an integer.

$|-x| = x$, so the absolute value of a negative integer is an integer.

(b) Is the reciprocal of a positive or negative integer always a rational number?

If x is a positive or negative integer, then the reciprocal of x is $\frac{1}{x}$. Since both 1 and x are integers, the reciprocal is a rational number.

32.

(a) Is the absolute value of a positive or negative rational number rational?

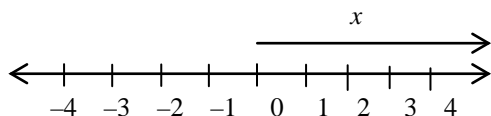
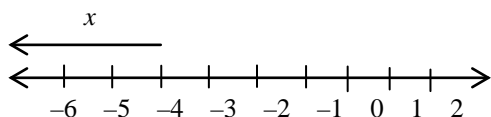
 $|x| = x$, so if x is a positive or negative rational number, the absolute value of it is also a rational number.

(b) Is the reciprocal of a positive or negative rational number a rational number?

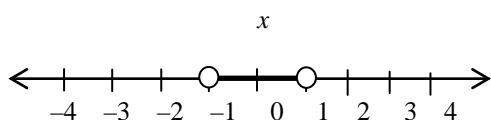
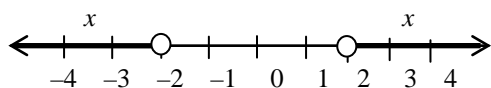
A rational number is a number that can be expressed as a fraction where both the numerator and denominator are integers and the denominator is not zero. So a rational number $\frac{\text{integer } a}{\text{integer } b}$ has a reciprocal of $\frac{1}{\frac{\text{integer } a}{\text{integer } b}} = \frac{\text{integer } b}{\text{integer } a}$, which is also a

rational number if integer a is not zero.

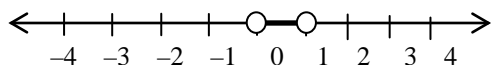
33.

(a) If $x > 0$, then x is a positive number located to the right of zero on the number line.(b) If $x < -4$, then x is a negative number located to the left of -4 on the number line.

34.

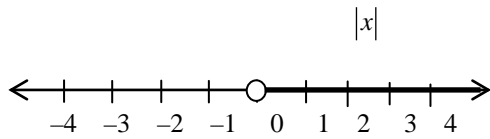
(a) If $|x| < 1$, then $-1 < x < 1$.(b) $|x| > 2$, then $x < -2$ or $x > 2$.

35.

If $x > 1$, then $\frac{1}{x}$ is a positive number less than 1. Or $0 < \frac{1}{x} < 1$. $\frac{1}{x}$ 

36.

If $x < 0$, then $|x|$ is a positive number greater than zero.



37.

$a + bj = a + b\sqrt{-1}$ is a real number when $\sqrt{-1}$ is eliminated, which is when $b = 0$. So $a + bj$ is a real number for all real values of a and $b = 0$.

38.

The variables are w and t .

The constants are c , 0.1, and 1.

39.

$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2}$. Find C_T , where $C_1 = 0.0040\text{F}$ and $C_2 = 0.0010\text{F}$.

$$\frac{1}{C_T} = \frac{1}{0.0040} + \frac{1}{0.0010}$$

$$\frac{1}{C_T} = \frac{1(0.0040) + 1(0.0010)}{0.0040 \times 0.0010}$$

$$C_T = \frac{0.0040 \times 0.0010}{0.0040 + 0.0010}$$

$$C_T = 0.00080 \text{ F}$$

40.

$$|100V| = 100V$$

$$|-200V| = 200V$$

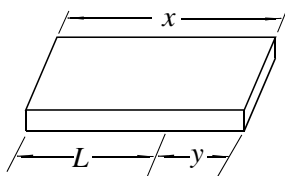
$$|-200V| > |100V|$$

41.

$$N = \frac{a \text{ bits}}{\text{bytes}} \times \frac{1000 \text{ bytes}}{1 \text{ kilobyte}} \times n \text{ kilobytes}$$

$$N = 1000 \text{ } an \text{ bits}$$

42.



x = length of base in m

y = the shortened length in centimetres.

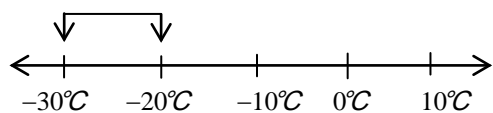
$100x$ = length of base in cm

$y + L = 100x$, all dimensions in cm

$L = 100x - y$

43.

Yes, $-20\text{ }^{\circ}\text{C} > -30\text{ }^{\circ}\text{C}$ because $-30\text{ }^{\circ}\text{C}$ is found to the left of $-20\text{ }^{\circ}\text{C}$ on the number line.



44.

For $I < 4\text{ A}$, $V > 12\text{ V}$.

1.2 Fundamental Operations of Algebra

1.

$$16 - 2 \times (-3) = 16 - (-6) = 16 + 6 = 22$$

2.

$$\frac{-18}{-6} + 5 - (-2)(3) = 3 + 5 - (-6) = 8 + 6 = 14$$

3.

$$\frac{-12}{8-2} + \frac{5-1}{2(-1)} = \frac{-12}{6} + \frac{4}{-2} = -2 + (-2) = -4$$

4.

$$\frac{7 \times 6}{0 \times 0} = \frac{42}{0} = \text{is undefined, not indeterminate.}$$

5.

$$8 + (-4) = 8 - 4 = 4$$

6.

$$-4 + (-7) = -4 - 7 = -11$$

7.

$$\begin{aligned} -3 + 9 &= 6 \text{ or alternatively} \\ -3 + 9 &= +(9-3) = +(6) = 6 \end{aligned}$$

8.

$$\begin{aligned} 18 - 21 &= -3 \text{ or alternatively} \\ 18 - 21 &= -(21-18) = -(3) = -3 \end{aligned}$$

9.

$$-19 - (-16) = -19 + 16 = -3$$

10.

$$8 - (-4) = 8 + 4 = 12$$

11.

$$8(-3) = -(8 \times 3) = -24$$

12.

$$-9(3) = -27$$

13.

$$-7(-5) = +(7 \times 5) = 35$$

14.

$$\frac{-9}{3} = -3$$

15.

$$\frac{-6(20-10)}{-3} = \frac{-6(10)}{-3} = \frac{-60}{-3} = 20$$

16.

$$\frac{28}{-7(6-5)} = \frac{28}{-7(1)} = \frac{28}{-7} = -4$$

17.

$$-2(4)(-5) = -8(-5) = 40$$

18.

$$3(-4)(6) = -12(6) = -72$$

19.

$$2(2-7) \div 10 = 2(-5) \div 10 = -10 \div 10 = -1$$

20.

$$\frac{-64}{-2|4-8|} = \frac{-64}{-2|-4|} = \frac{-64}{-2(4)} = \frac{-64}{-8} = 8$$

21.

$$-9 - |2-10| = -9 - |-8| = -9 - 8 = -17$$

22.

$$(7-7) \div (5-7) = 0 \div (-2) = 0$$

23.

$$\frac{17-7}{7-7} = \frac{10}{0} = \text{is undefined}$$

24.

$$\frac{7-7}{7-7} = \frac{0}{0} = \text{is indeterminate}$$

25.

$$8 - 3(-4) = 8 + 12 = 20$$

26.

$$20 + 8 \div 4 = 20 + 2 = 22$$

27.

$$-2(-6) + \left| \frac{8}{-2} \right| = 12 + |-4| = 12 + 4 = 16$$

28.

$$-10 - (-6)(-8) = -10 - (48) = -58$$

29.

$$30(-6)(-2) \div (0 - 40) = 30(12) \div (-40) = 360 \div (-40) = -9$$

30.

$$\frac{7 - |-5|}{-1(-2)} = \frac{7 - 5}{2} = \frac{2}{2} = 1$$

31.

$$\frac{24}{3 + (-5)} - 4(-9) = \frac{24}{-2} + (4 \times 9) = -12 + 36 = 24$$

32.

$$\frac{-18}{3} - \frac{4 - 6}{-1} = -6 - \frac{-2}{-1} = -6 - 2 = -8$$

33.

$$\begin{aligned} -7 - \frac{|-14|}{2(2-3)} - 3|6-8| &= -7 - \frac{14}{2(-1)} - 3|-2| \\ &= -7 - \frac{14}{-2} - 3(2) \\ &= -7 - (-7) - 6 \\ &= -7 + 7 - 6 \\ &= -6 \end{aligned}$$

34.

$$\begin{aligned} -7(-3) + \frac{6}{-3} - (-9) &= +(7 \times 3) + (-2) + 9 \\ &= 21 - 2 + 9 \\ &= 28 \end{aligned}$$

35.

$$\begin{aligned} \frac{3(-9) - 2(-3)}{3 - 10} &= \frac{-(3 \times 9) + (2 \times 3)}{-7} \\ &= \frac{-27 + 6}{-7} \\ &= \frac{-21}{-7} \\ &= 3 \end{aligned}$$

36.

$$\frac{20(-12) - 40(-15)}{98 - |-98|} = \frac{-240 + 600}{98 - 98} = \frac{360}{0} = \text{is undefined}$$

37.

$6(7) = (7)6$ demonstrates the commutative law of multiplication.

38.

$6 + 8 = 8 + 6$ demonstrates the commutative law of addition.

39.

$6(3+1) = 6(3) + 6(1)$ demonstrates the distributive law.

40.

$4(5 \times \pi) = (4 \times 5)\pi$ demonstrates the associative law of multiplication.

41.

$3+(5+9) = (3+5)+9$ demonstrates the associative law of addition.

42.

$8(3-2) = 8(3) - 8(2)$ demonstrates the distributive law.

43.

$(\sqrt{5} \times 3) \times 9 = \sqrt{5} \times (3 \times 9)$ demonstrates the associative law of multiplication.

44.

$(3 \times 6) \times 7 = 7 \times (3 \times 6)$ demonstrates the commutative law of multiplication.

45.

$-a + (-b) = -a - b$, which is expression (d).

46.

$b - (-a) = b + a = a + b$, which is expression (a).

47.

$-b - (-a) = -b + a = a - b$, which is expression (b).

48.

$-a - (-b) = -a + b = b - a$, which is expression (c).

49.

(a) The sign of a product of an even number of negative numbers is positive. Example: $-3(-6) = 18$

(b) The sign of a product of an odd number of negative numbers is negative.

Example: $-5(-4)(-2) = -40$

50.

Subtraction is not commutative because $x - y \neq y - x$. Example: $7 - 5 = 2$ does not equal $5 - 7 = -2$

51.

Yes, from the definition in Section 1.1, the absolute value of a positive number is the number itself, and the absolute value of a negative number is the corresponding positive number. So for values of x where $x > 0$ (positive) or $x = 0$ (neutral) then $|x| = x$.

Example: $|4| = 4$.

The claim that absolute values of negative numbers $|x| = -x$ is also true.

Example: if x is -6 , then $|-6| = -(-6) = 6$.

52.

The incorrect answer was achieved by subtracting before multiplying or dividing which violates the order of operations.

$$24 - 6 \div 2 \times 3 \neq 18 \div 2 \times 3 = 9 \times 3 = 27$$

The correct value is:

$$24 - 6 \div 2 \times 3 = 24 - 3 \times 3 = 24 - 9 = 15$$

53.

(a) $-xy = 1$ is true for values of x and y that are negative reciprocals of each other or $y = -\frac{1}{x}$, providing that the number x in

the denominator is not zero. So if $x = 12$, then $y = -\frac{1}{12}$ and $-xy = -(12)\left(-\frac{1}{12}\right) = 1$.

(b) $\frac{x-y}{x-y} = 1$ is true for all values of x and y , providing that $x \neq y$ to prevent division by zero.

54.**(a)**

$|x + y| = |x| + |y|$ is true for values where both x and y are positive or either are zero:

$|x + y| = |x| + |y|$, when $x \geq 0$ and $y \geq 0$.

Example:

$$|6 + 3| = 6 + 3 = 9 \text{ and}$$

$$|6| + |3| = 6 + 3 = 9$$

$|x + y| = |x| + |y|$ is also true for values where both x and y are negative

$|x + y| = |x| + |y|$, when $x < 0$ and $y < 0$.

Example:

$$|-11 + (-7)| = |-18| = 18$$

$$|-11| + |-7| = 11 + 7 = 18$$

$|x + y| = |x| + |y|$ is not true however, when x and y have opposite signs

$|x + y| \neq |x| + |y|$, when $x > 0$ and $y < 0$; or $x < 0$ and $y > 0$.

Example:

$$|-21 + 6| = |-15| = 15,$$

$$|-21| + |6| = 21 + 6 = 27 \neq 15$$

$$|4 + (-5)| = |-1| = 1,$$

$$|4| + |-5| = 4 + 5 = 9 \neq 1$$

(b)

The same argument as above holds true for $|x - y| = |x| - |y|$

$|x - y| = |x| - |y|$ is true for values where both x and y are positive or either are zero:

$|x - y| = |x| - |y|$, when $x \geq 0$ and $y \geq 0$.

Example:

$$|6 - 3| = 6 - 3 = 3 \text{ and}$$

$$|6| - |3| = 6 - 3 = 3$$

$|x - y| = |x| - |y|$ is also true for values where both x and y are negative:

$|x - y| = |x| - |y|$, when $x < 0$ and $y < 0$.

Example:

$$|-11 - (-7)| = |-11 + 7| = |-4| = 4$$

$$|-11| - |-7| = 11 - 7 = 4$$

$|x - y| = |x| - |y|$ is not true however, when x and y have opposite signs

$|x - y| \neq |x| - |y|$, when $x > 0$ and $y < 0$; or $x < 0$ and $y > 0$.

Example:

$$|21 - (-6)| = |21 + 6| = |27| = 27,$$

$$|21| - |-6| = 21 - 6 = 15 \neq 27$$

55. The change in the meter energy reading E would be:

$$E_{change} = E_{used} - E_{generated}$$

$$E_{change} = 2.1 \text{ kW} \cdot \text{h} - 1.5 \text{ kW} (3.0 \text{ h})$$

$$E_{change} = 2.1 \text{ kW} \cdot \text{h} - 4.5 \text{ kW} \cdot \text{h}$$

$$E_{change} = -2.4 \text{ kW} \cdot \text{h}$$

56.

Assuming that this batting average is for the current season only which is just starting, the number of hits is zero and the total number of at-bats is also zero giving us a batting average = $\frac{\text{number of hits}}{\text{at - bats}} = \frac{0}{0}$ which is indeterminate, not 0.000.

57.

The average temperature for the week is:

$$T_{avg} = \frac{7 + 3 + (-2) + (-3) + (-1) + 4 + 6}{7} \text{ } ^\circ\text{C}$$

$$T_{avg} = \frac{7 + 3 - 2 - 3 - 1 + 4 + 6}{7} \text{ } ^\circ\text{C}$$

$$T_{avg} = \frac{14}{7} \text{ } ^\circ\text{C} = 2.0 \text{ } ^\circ\text{C}$$

58.

The vertical distance from the flare gun is

$$d = (20)(5) + (-5)(25)$$

$$d = 100 + (-125)$$

$$d = 100 - 125$$

$$d = -25 \text{ m}$$

The flare is 25 m below the flare gun.

59.

The sum of the voltages is

$$V_{sum} = 6\text{V} + (-2\text{V}) + 8\text{V} + (-5\text{V}) + 3\text{V}$$

$$V_{sum} = 6\text{V} - 2\text{V} + 8\text{V} - 5\text{V} + 3\text{V}$$

$$V_{sum} = 10\text{V}$$

60.**(a)**

The change in the current for the first interval is the second reading – the first reading

$$\text{Change}_1 = -0.2 \text{ mA} - 0.7 \text{ mA} = -0.9 \text{ mA} .$$

(b)

The change in the current for the middle intervals is the third reading – the second reading

$$\text{Change}_2 = -0.9 \text{ mA} - (-0.2 \text{ mA}) = -0.9 \text{ mA} + 0.2 \text{ mA} = -0.7 \text{ mA} .$$

(c)

The change in the current for the last interval is the last reading – the third reading

$$\text{Change}_3 = -0.6 \text{ mA} - (-0.9 \text{ mA}) = -0.6 \text{ mA} + 0.9 \text{ mA} = 0.3 \text{ mA} .$$

61.

The oil drilled by the first well is $100 \text{ m} + 200 \text{ m} = 300 \text{ m}$ which equals the depth drilled by the second well
 $200 \text{ m} + 100 \text{ m} = 300 \text{ m} .$

$100 \text{ m} + 200 \text{ m} = 200 \text{ m} + 100 \text{ m}$ demonstrates the commutative law of addition.

62.

The first tank leaks $12 \frac{\text{L}}{\text{h}}(7 \text{ h}) = 84 \text{ L} .$ The second tank leaks $7 \frac{\text{L}}{\text{h}}(12 \text{ h}) = 84 \text{ L} .$

$12 \times 7 = 7 \times 12$ demonstrates the commutative law of multiplication.

63.

The total time spent browsing these websites is the total time spent browsing the first site by each person + the total time

$$t = 4 \text{ persons} \times 8 \frac{\text{minutes}}{\text{person}} + 4 \text{ persons} \times 6 \frac{\text{minutes}}{\text{person}}$$

$$t = 32 \text{ min} + 24 \text{ min}$$

$$t = 56 \text{ min}$$

spent browsing the second site by each person OR

$$t = 4 \text{ persons} \times (8 + 6) \frac{\text{minutes}}{\text{person}}$$

$$t = 4 \text{ persons} \times 14 \frac{\text{minutes}}{\text{person}}$$

$$t = 56 \text{ min}$$

which illustrates the distributive law.

64.

Distance = rate \times time

$$d = \left(600 \frac{\text{km}}{\text{h}} + 50 \frac{\text{km}}{\text{h}} \right) 3 \text{ h}$$

$$d = 600 \frac{\text{km}}{\text{h}} (3\text{h}) + 50 \frac{\text{km}}{\text{h}} (3\text{h})$$

$$d = 1800 \text{ km} + 150 \text{ km} = 1950 \text{ km}$$

OR

$$d = \left(600 \frac{\text{km}}{\text{h}} + 50 \frac{\text{km}}{\text{h}} \right) 3 \text{ h}$$

$$d = \left(650 \frac{\text{km}}{\text{h}} \right) 3 \text{ h}$$

$$d = 1950 \text{ km}$$

This illustrates the distributive law.

1.3 Measurement, Calculation, and Approximate Numbers

1.

0.390 has three significant digits since the zero is after the decimal. The zero is not necessary as a placeholder and should not be written unless it is significant.

2.

35.303 rounded off to four significant digits is 35.30.

3.

In finding the product of the approximate numbers, $2.483 \times 30.5 = 75.7315$, but since 30.5 has 3 significant digits, the answer is 75.7.

4.

$38.3 - 21.9(-3.58) = 116.702$ using exact numbers; if we estimate the result, $40 - 20(-4) = 120$.

5.

1 megahertz = 1 MHz = 1 000 000 Hz

6.

1 kilowatt = 1 kW = 1000 W

7.

1 millimetre = 1 mm = 0.001 m

8.

1 picosecond = 1 ps = 1×10^{-12} s

9.

1 kV = 1 kilovolt = 1000 volts

10.

1 G Ω = 1 gigaohm = 1×10^9 ohms

11.

1 mA = 1 milliampere = 0.001 amperes

12.

1 pF = 1 picofarad = 1×10^{-12} farads

13.

$1 \text{ km} \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \cdot \left(\frac{100 \text{ cm}}{1 \text{ m}} \right) = 100\,000 \text{ cm}$

14.

$1 \text{ kg} \left(\frac{1000 \text{ g}}{1 \text{ kg}} \right) \cdot \left(\frac{1000 \text{ mg}}{1 \text{ g}} \right) = 1\,000\,000 \text{ mg}$

15.

$$20 \text{ s} \left(\frac{1 \text{ Ms}}{1\,000\,000 \text{ s}} \right) = 0.000\,02 \text{ Ms}$$

16.

$$800 \text{ Pa} \left(\frac{1 \text{ kPa}}{1\,000 \text{ Pa}} \right) = 0.8 \text{ kPa}$$

17.

$$250 \text{ mm}^2 \left(\frac{1 \text{ m}}{1\,000 \text{ mm}} \right)^2 = 0.000\,25 \text{ m}^2$$

18.

$$1.75 \text{ m}^2 \left(\frac{100 \text{ cm}}{1 \text{ m}} \right)^2 = 17\,500 \text{ cm}^2$$

19.

$$80.0 \text{ m}^3 \left(\frac{1000 \text{ L}}{1 \text{ m}^3} \right) = 80\,000 \text{ L (with 3 significant digits)}$$

20.

$$0.125 \text{ L} \left(\frac{1000 \text{ mL}}{1 \text{ L}} \right) = 125 \text{ mL}$$

21.

$$45.0 \text{ m/s} \left(\frac{100 \text{ cm}}{1 \text{ m}} \right) = 4500 \text{ cm/s (with 3 significant digits)}$$

22.

$$1.32 \frac{\text{km}}{\text{h}} \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \cdot \left(\frac{1 \text{ h}}{3600 \text{ s}} \right) = 0.367 \text{ m/s}$$

23.

$$9.80 \frac{\text{m}}{\text{s}^2} \left(\frac{100 \text{ cm}}{1 \text{ m}} \right) \cdot \left(\frac{60 \text{ s}}{1 \text{ min}} \right)^2 = 3\,530\,000 \text{ cm/min}^2$$

24.

$$5.10 \frac{\text{g}}{\text{cm}^3} \left(\frac{1 \text{ kg}}{1000 \text{ g}} \right) \cdot \left(\frac{100 \text{ cm}}{1 \text{ m}} \right)^3 = 5100 \text{ kg/m}^3 \text{ (with 3 significant digits)}$$

25.

$$25 \text{ h} \left(\frac{3600 \text{ s}}{1 \text{ h}} \right) \cdot \left(\frac{1000 \text{ ms}}{1 \text{ s}} \right) = 90\,000\,000 \text{ ms (with 2 significant digits)}$$

26.

$$5.25 \text{ mV} \left(\frac{1 \text{ V}}{1000 \text{ mV}} \right) \cdot \left(\frac{1 \text{ W/A}}{1 \text{ V}} \right) = 0.005\,25 \text{ W/A}$$

27.

$$15.0 \mu\text{F} \left(\frac{1 \text{ F}}{1\,000\,000 \mu\text{F}} \right) \cdot \left(\frac{1 \text{ C/V}}{1 \text{ F}} \right) \cdot \left(\frac{1000 \text{ mC}}{1 \text{ C}} \right) = 0.0150 \text{ mC/V}$$

28.

To travel 1 m, light takes $1/299\,792\,458 \text{ s}$.

$$1 \text{ y} \left(\frac{365.25 \text{ d}}{1 \text{ y}} \right) \cdot \left(\frac{24 \text{ h}}{1 \text{ d}} \right) \cdot \left(\frac{3600 \text{ s}}{1 \text{ h}} \right) = 31\,557\,600 \text{ s}$$

$$\frac{1 \text{ m}}{1/299\,792\,458 \text{ s}} \left(\frac{31\,557\,600 \text{ s}}{1 \text{ y}} \right) = 9\,460\,730\,472\,580\,800 \text{ m} = 9.461 \times 10^{15} \text{ m/y}$$

29.

The distance around the orbit should be $d = 2\pi r = 2\pi(150\,000\,000 \text{ km}) = 942\,477\,796.1 \text{ km}$.

$$1 \text{ y} \left(\frac{365.25 \text{ d}}{1 \text{ y}} \right) \cdot \left(\frac{24 \text{ h}}{1 \text{ d}} \right) = 8766 \text{ h}$$

Orbital speed is the ratio of distance travelled to time elapsed:

$$v = \frac{d}{t} = \frac{942\,477\,796.1 \text{ km}}{8766 \text{ h}} = 107\,515 \text{ km/h} = 110\,000 \text{ km/h}$$

30.

$$101\,300 \text{ Pa} \left(\frac{1 \text{ kPa}}{1\,000 \text{ Pa}} \right) = 101.3 \text{ kPa}$$

31.

$$56 \text{ L} \left(\frac{1 \text{ m}^3}{1\,000 \text{ L}} \right) \left(\frac{100 \text{ cm}}{1 \text{ m}} \right)^3 = 56\,000 \text{ cm}^3$$

32.

$$0.160 \text{ kg} \left(\frac{1000 \text{ g}}{1 \text{ kg}} \right) \cdot \left(\frac{1000 \text{ mg}}{1 \text{ g}} \right) = 160\,000 \text{ mg}$$

33.

$$6800 \frac{\text{m}}{\text{s}} \left(\frac{1 \text{ km}}{1000 \text{ m}} \right) \cdot \left(\frac{3600 \text{ s}}{1 \text{ h}} \right) = 24\,480 \text{ km/h} = 24\,000 \text{ km/h}$$

34.

Convert 1.5 TB to kB:

$$1.5 \text{ TB} \left(\frac{1\,000\,000\,000\,000 \text{ B}}{1 \text{ TB}} \right) \cdot \left(\frac{1 \text{ kB}}{1000 \text{ B}} \right) = 1\,500\,000\,000 \text{ kB}$$

Compare the memories:

$$\left(\frac{1\,500\,000\,000 \text{ kB}}{64 \text{ kB}} \right) = 23\,437\,500 \text{ times greater}$$

35.

$$112 \text{ cm}^2 \left(\frac{1 \text{ m}}{100 \text{ cm}} \right)^2 = 0.0112 \text{ m}^2$$

36.

$$0.024 \text{ MW} \cdot \text{h} \left(\frac{3600 \text{ s}}{1 \text{ h}} \right) \cdot \left(\frac{1\,000\,000 \text{ W}}{1 \text{ MW}} \right) \cdot \left(\frac{1 \text{ J/s}}{1 \text{ W}} \right) = 86\,400\,000 \text{ J} = 86\,000\,000 \text{ J}$$

37.

$$1000 \frac{\text{kg}}{\text{m}^3} \left(\frac{1000 \text{ g}}{1 \text{ kg}} \right) \cdot \left(\frac{1 \text{ m}^3}{1000 \text{ L}} \right) = 1000 \text{ g/L}$$

38.

$$8500 \frac{\text{mL}}{\text{min}} \left(\frac{1 \text{ L}}{1000 \text{ mL}} \right) \cdot \left(\frac{1 \text{ m}^3}{1000 \text{ L}} \right) \cdot \left(\frac{1 \text{ min}}{60 \text{ s}} \right) = 0.000\,14 \text{ m}^3/\text{s}$$

39.

$$332 \frac{\text{m}}{\text{s}} \left(\frac{1 \text{ km}}{1000 \text{ m}} \right) \cdot \left(\frac{3600 \text{ s}}{1 \text{ h}} \right) = 1195.2 \text{ km/h} = 1200 \text{ km/h (with 3 significant digits)}$$

40.

$$\frac{15.0 \text{ g}}{0.060 \text{ L}} \left(\frac{1000 \text{ mg}}{1 \text{ g}} \right) \cdot \left(\frac{1 \text{ L}}{10 \text{ dL}} \right) = 25\,000 \text{ mg/dL}$$

41.

$$1.35 \frac{\text{kW}}{\text{m}^2} \left(\frac{1000 \text{ W}}{1 \text{ kW}} \right) \cdot \left(\frac{1 \text{ J/s}}{1 \text{ W}} \right) \cdot \left(\frac{1 \text{ m}}{100 \text{ cm}} \right)^2 = 0.135 \text{ J}/(\text{s} \cdot \text{cm}^2)$$

42.

Orbital speed is the ratio of distance travelled to time elapsed:

$$v = \frac{d}{t} = \frac{2\,400\,000 \text{ km}}{28 \text{ d}} \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \cdot \left(\frac{1 \text{ d}}{24 \text{ h}} \right) \cdot \left(\frac{1 \text{ h}}{3600 \text{ s}} \right) = 992.06 \text{ m/s} = 990 \text{ m/s}$$

43.

$$1.2 \times 10^6 \frac{\text{A}}{\text{m}^2} \left(\frac{1000 \text{ mA}}{1 \text{ A}} \right) \cdot \left(\frac{1 \text{ m}}{100 \text{ cm}} \right)^2 = 120\,000 \text{ mA/cm}^2$$

44.

$$\frac{2.0 \text{ L}}{24 \text{ km}} \left(\frac{100 \text{ km}}{100 \text{ km}} \right) = 8.3 \text{ L}/(100 \text{ km})$$

45.

8 cylinders is exact because they can be counted. 55 km/h is approximate since it is measured.

46.

0.002 mm thick is a measurement and is therefore an approximation. \$7.50 is an exact price.

47.24 hr and 1440 min (60 min/h \times 24 h = 1440 min) are both exact numbers.**48.**

50 keys is exact because you can count them; 50 h of use is approximate since it is a measurement of time.

49.

107 has 3 significant digits; 3004 has 4 significant digits.

50.

3600 has 2 significant digits; 730 has two significant digits.

51.

6.80 has 3 significant digits since the zero indicates precision; 6.08 has 3 significant digits.

52.

0.8735 has 4 significant digits; 0.0075 has two significant digits.

53.

3000 has 1 significant digit; 3000.1 has 5 significant digits.

54.

1.00 has 3 significant digits since the zeros indicate precision; 0.01 has 1 significant digit since leading zeros are not significant.

55.

(a) 0.01 has more decimal places (2) and is more precise.

(b) 30.8 has more significant digits (3) and is more accurate.

56.

(a) Both 0.041 and 7.673 have the same precision as they have the same number of decimal places (3).

(b) 7.673 is more accurate because it has more significant digits (4) than 0.041, which has 2 significant digits.

57.

(a) Both 0.1 and 78.0 have the same precision as they have the same number of decimal places.

(b) 78.0 is more accurate because it has more significant digits (3) than 0.1, which has 1 significant digit.

58.

(a) 0.004 is more precise because it has more decimal places (3).

(b) 7040 is more accurate because it has more significant digits (3) than 0.004, which has only 1 significant digit.

59.

(a) 0.004 is more precise because it has more decimal places (3).

(b) Both have the same accuracy as they both have 1 significant digit.

60.

(a) Both 50.060 and 8.914 have the same precision as they have the same number of decimal places (3).

(b) 50.060 is more accurate because it has more significant digits (5) than 8.914, which has 4 significant digits.

61.

- (a) 4.936 rounded to 3 significant digits is 4.94.
- (b) 4.936 rounded to 2 significant digits is 4.9.

62.

- (a) 80.53 rounded to 3 significant digits is 80.5.
- (b) 80.53 rounded to 2 significant digits is 81.

63.

- (a) 50 893 rounded to 3 significant digits is 50 900.
- (b) 50 893 rounded to 2 significant digits is 51 000.

64.

- (a) 7.005 rounded to 3 significant digits is 7.00 since 0 is the nearest even to 0.5.
- (b) 7.005 rounded to 2 significant digits is 7.0.

65.

- (a) 9545 rounded to 3 significant digits is 9540 since 4 is the nearest even to 4.5
- (b) 9549 rounded to 2 significant digits is 9500.

66.

- (a) 30.96 rounded to 3 significant digits is 31.0.
- (b) 30.96 rounded to 2 significant digits is 31.

67.

- (a) 0.9449 rounded to 3 significant digits is 0.945.
- (b) 0.9449 rounded to 2 significant digits is 0.94.

68.

- (a) 0.9999 rounded to 3 significant digits is 1.00.
- (b) 0.9999 rounded to 2 significant digits is 1.0.

69.

- (a) Estimate: $13 + 1 - 2 = 12$
- (b) Calculator: $12.78 + 1.0495 - 1.633 = 12.1965$, which is 12.20 to 0.01 precision

70.

(a) Estimate: $4 \times 17 = 68$

(b) Calculator: $3.64(17.06) = 62.0984$, which is 62.1 to 3 significant digits

71.

(a) Estimate: $0.04 - \frac{0.05}{2} = 0.015$

(b) Calculator: $0.0350 - \frac{0.0450}{1.909} = 0.011427$, which is 0.0114 to 0.0001 precision

72.

(a) Estimate: $\frac{0.3}{1 \times 0.5} = 0.6$

(b) Calculator: $\frac{0.3275}{1.096 \times 0.50085} = 0.596613494$, which is 0.5966 to 4 significant digits

73.

(a) Estimate: $\frac{20 \times 0.02}{10 - 8} = 0.2$

(b) Calculator: $\frac{23.962 \times 0.01537}{10.965 - 8.249} = 0.135602334$, which is 0.1356 to 4 significant digits

74.

(a) Estimate: $\frac{0.7 + 0.05}{300 \times 3} = 0.0083\dots$

(b) Calculator: $\frac{0.69378 + 0.04997}{257.4 \times 3.216} = 0.0008984675496$, which is 0.0008985 to 4 significant digits

75.

(a) Estimate: $\frac{4000}{500} - \frac{2 \times 300}{400} = 6.5$

(b) Calculator: $\frac{3872}{503.1} - \frac{2.056 \times 309.6}{395.2} = 6.08561098$, which is 6.086 to 4 significant digits

76.

(a) Estimate: $\frac{1}{0.6} + \frac{4}{3-1} = 3.66\dots$

(b) Calculator: $\frac{1.00}{0.5926} + \frac{3.6957}{2.935 - 1.054} = 3.652231698$, which is 3.65 to 3 significant digits

77.

$0.9788 + 14.9 = 15.8788$ since the least precise number in the question has 4 decimal places.

78.

$17.311 - 22.98 = -5.669$ since the least precise number in the question has 3 decimal places.

79.

$3.142 \times 65 = 204.23$, which is 204.2 because the least accurate number has 4 significant digits.

80.

$8.62 \div 1728 = 0.004988$, which is 0.00499 because the least accurate number has 3 significant digits.

81.

With a frequency listed as 2.75 MHz, the least possible frequency is 2.745 MHz, and the greatest possible frequency is 2.755 MHz. Any measurements between those limits would round to 2.75 MHz.

82.

For an engine displacement stated at 2400 cm^3 , the least possible displacement is 2350 cm^3 , and the greatest possible displacement is 2450 cm^3 . Any measurements between those limits would round to 2400 cm^3 .

83.

The speed of sound is $5.23 \text{ km} \div 15 \text{ s} = 0.3486\dots \text{ km/s} = 348.6\dots \text{ m/s}$. However, the least accurate measurement was time since it has only 2 significant digits. The correct answer is 350 m/s.

84.

$4.4 \text{ s} - 2.72 \text{ s} = 1.68 \text{ s}$, but the answer must be given according to precision of the least precise measurement in the question, so the correct answer is 1.7 s.

85.

(a) $2.2 + 3.8 \times 4.5 = 2.2 + (3.8 \times 4.5) = 19.3$

(b) $(2.2 + 3.8) \times 4.5 = 6.0 \times 4.5 = 27$

86.

(a) $6.03 \div 2.25 + 1.77 = (6.03 \div 2.25) + 1.77 = 4.45$

(b) $6.03 \div (2.25 + 1.77) = 6.03 \div 4.02 = 1.5$

87.

(a) $2 + 0 = 2$

(b) $2 - 0 = 2$

(c) $0 - 2 = -2$

(d) $2 \times 0 = 0$

(e) $2 \div 0 = \text{error}$; from Section 1.2, an equation that has 0 in the denominator is undefined when the numerator is not also 0.

88.

(a) $2 \div 0.0001 = 20\,000$; $2 \div 0 = \text{error}$

(b) $0.0001 \div 0.0001 = 1$; $0 \div 0 = \text{error}$

(c) Any number divided by zero is undefined. Zero divided by zero is indeterminate.

89.

Pick any six digit integer for $x = 231\,465$ and rearrange those digits for $y = 164\,352$.

$(x - y) \div 9 = (231\,465 - 164\,352) \div 9 = 7457$. A smaller *integer* number results.

90.

$$9 \times 8 + 7 + 6 + 5 + 4 + 3 + 2 + 1 + 0 = 100$$

91.

$$\pi = 3.14159265\dots$$

(a) $\pi < 3.1416$

$$22 \div 7 = 3.1428$$

(b) $\pi < (22 \div 7)$

92.

(a) $8 \div 33 = 0.2424\dots = 0.\overline{24}$

(b) $\pi = 3.14159265\dots$

93.

(a) $1 \div 3 = 0.333\dots$ It is a rational number since it is a repeating decimal.

(b) $5 \div 11 = 0.454545\dots$ It is a rational number since it is a repeating decimal.

(c) $2 \div 5 = 0.400\dots$ It is a rational number since it is a repeating decimal (0 is the repeating part).

94.

$124 \div 990 = 0.12525\dots$ the calculator may show the answer as 0.1252525253 because it has rounded up for the next 5 that doesn't fit on the screen.

95.

$32.4 \text{ MJ} + 26.704 \text{ MJ} + 36.23 \text{ MJ} = 95.334 \text{ MJ}$. The answer must be to the same precision as the least precise measurement. The answer is 95.3 MJ.

96.

The difference in speed of the two jets is the speed of the second jet (1450 km/h) minus the speed of the first jet (938 km/h): $1450 \text{ km/h} - 938 \text{ km/h} = 512 \text{ km/h}$. But since 1450 is rounded to the tens precision, the answer must be as well. The answer is 510 km/h.

97.

$$1 \text{ K} = 1024 \text{ bytes}$$

$$256 \text{ K} \cdot \left(\frac{1024 \text{ bytes}}{1 \text{ K}} \right) = 262\,144 \text{ bytes}$$

98.

$$V = (15.2 \, \Omega + 5.64 \, \Omega + 101.23 \, \Omega) \times 3.55 \text{ A}$$

$$V = 122.07 \, \Omega \times 3.55 \text{ A}$$

$$V = 433.3485 \text{ V}$$

$$V = 433 \text{ V to 3 significant digits}$$

99.

$$\frac{100(40.63 + 52.96)}{105.30 + 52.96} = 59.1386 \% = 59.14 \% \text{ to 4 significant digits}$$

100.

$$T = \frac{50.45(9.80)}{1 + 100.9 \div 23} = 91.779 \text{ N} = 92 \text{ N to 2 significant digits}$$

1.4 Exponents**1.**

$$(-x^3)^2 = [(-1)x^3]^2 = (-1)^2(x^3)^2 = (1)x^6 = x^6$$

2.

$$2x^0 = 2(1) = 2$$

3.

$$\left(\frac{b^2t}{a^3x}\right)^{-2} = \frac{(b^2t)^{-2}}{(a^3x)^{-2}} = \frac{(a^3x)^2}{(b^2t)^2} = \frac{(a^3)^2(x^2)}{(b^2)^2(t^2)} = \frac{a^6x^2}{b^4t^2}$$

4.

$$8 - (-1)^3 - 2(-3)^2 = 8 - (-1) - 2(9) = 8 + 1 - 18 = -9$$

5.

$$x^3x^4 = x^{3+4} = x^7$$

6.

$$y^2y^7 = y^{2+7} = y^9$$

7.

$$2b^4b^2 = 2b^{4+2} = 2b^6$$

8.

$$3k^5k = 3k^{5+1} = 3k^6$$

9.

$$\frac{m^5}{m^3} = m^{5-3} = m^2$$

10.

$$\frac{2x^6}{x} = 2x^{6-1} = 2x^5$$

11.

$$\frac{n^5}{7n^9} = \frac{n^{5-9}}{7} = \frac{n^{-4}}{7} = \frac{1}{7n^4}$$

12.

$$\frac{3s}{s^4} = 3s^{1-4} = 3s^{-3} = \frac{3}{s^3}$$

13.

$$(P^2)^4 = P^{2(4)} = P^8$$

14.

$$(x^8)^3 = x^{8(3)} = x^{24}$$

15.

$$(2\pi)^3 = (2)^3(\pi^3) = 8\pi^3$$

16.

$$(ax)^5 = a^5x^5$$

17.

$$(aT^2)^{30} = a^{30}T^{2(30)} = a^{30}T^{60}$$

18.

$$(3r^2)^3 = (3)^3r^{2(3)} = 27r^6$$

19.

$$\left(\frac{2}{b}\right)^3 = \frac{(2)^3}{b^3} = \frac{8}{b^3}$$

20.

$$\left(\frac{F}{t}\right)^{20} = \frac{F^{20}}{t^{20}}$$

21.

$$\left(\frac{x^2}{2}\right)^4 = \frac{x^{2(4)}}{(2)^4} = \frac{x^8}{16}$$

22.

$$\left(\frac{3}{n^3}\right)^3 = \frac{(3)^3}{n^{3(3)}} = \frac{27}{n^9}$$

23.

$$(8a)^0 = 1$$

24.

$$6v^0 = 6(1) = 6$$

25.

$$-3x^0 = -3(1) = -3$$

26.

$$-(-2)^0 = -1(1) = -1$$

27.

$$6^{-1} = \frac{1}{6^1} = \frac{1}{6}$$

28.

$$-w^{-5} = -\frac{1}{w^5}$$

29.

$$\frac{1}{R^{-2}} = R^2$$

30.

$$\frac{1}{-t^{-48}} = -t^{48}$$

31.

$$(-t^2)^7 = [(-1)(t^2)]^7 = (-1)^7 t^{2(7)} = (-1)t^{14} = -t^{14}$$

32.

$$(-y^3)^5 = [(-1)(y^3)]^5 = (-1)^5 y^{3(5)} = (-1)y^{15} = -y^{15}$$

33.

$$(2v^2)^{-6} = (2)^{-6} v^{2(-6)} = \frac{v^{-12}}{(2)^6} = \frac{1}{64v^{12}}$$

34.

$$-(-c^4)^{-4} = (-1)[(-1)c^4]^{-4} = (-1)(-1)^{-4} (c^{4(-4)}) = \frac{(-1)}{(-1)^4} (c^{-16}) = -\frac{1}{c^{16}}$$

35.

$$-\frac{L^{-3}}{L^{-5}} = -L^{-3-(-5)} = -L^2$$

36.

$$2i^{40}i^{-70} = 2i^{40+(-70)} = 2i^{-30} = \frac{2}{i^{30}}$$

37.

$$\frac{2v^4}{(2v)^4} = \frac{2v^4}{(2)^4(v^4)} = \frac{2v^4}{16v^4} = \frac{1}{8}$$

38.

$$\frac{x^2x^3}{(x^2)^3} = \frac{x^{2+3}}{x^{2(3)}} = \frac{x^5}{x^6} = \frac{1}{x}$$

39.

$$\frac{(n^2)^4}{(n^4)^2} = \frac{n^{2(4)}}{n^{4(2)}} = \frac{n^8}{n^8} = 1$$

40.

$$\frac{(3t)^{-1}}{3t^{-1}} = \frac{(3)^{-1}t^{-1}}{3t^{-1}} = \frac{t}{3(3)t} = \frac{1}{9}$$

41.

$$(\pi^0 x^2 a^{-1})^{-1} = \pi^{0(-1)} x^{2(-1)} a^{-1(-1)} = \pi^0 x^{-2} a^1 = \frac{a}{x^2}$$

42.

$$(3m^{-2}n^4)^{-2} = (3)^{-2} m^{-2(-2)} n^{4(-2)} = \frac{m^4}{9n^8}$$

43.

$$(-8g^{-1}s^3)^2 = (-8)^2 g^{-1(2)} s^{3(2)} = \frac{64s^6}{g^2}$$

44.

$$ax^{-2}(-a^2x)^3 = ax^{-2}(-1)^3(a^{2(3)})x^3 = -\frac{a(a^6)x^3}{x^2} = -a^{1+6}x^{3-2} = -a^7x$$

45.

$$\left(\frac{4x^{-1}}{a^{-1}}\right)^{-3} = \frac{(4)^{-3}x^{-1(-3)}}{a^{-1(-3)}} = \frac{x^3}{64a^3}$$

46.

$$\left(\frac{2b^2}{y^5}\right)^{-2} = \frac{(2)^{-2}b^{2(-2)}}{y^{5(-2)}} = \frac{b^{-4}}{4y^{-10}} = \frac{y^{10}}{4b^4}$$

47.

$$\frac{15n^2T^5}{3n^{-1}T^6} = \frac{5n^{2-(-1)}}{T} = \frac{5n^3}{T}$$

48.

$$\frac{(nRT^{-2})^{32}}{R^{-2}T^{32}} = \frac{n^{32}R^{32(-2)}T^{-2(32)}}{T^{32}} = \frac{n^{32}R^{34}T^{-64}}{T^{32}} = \frac{n^{32}R^{34}}{T^{32-(-64)}} = \frac{n^{32}R^{34}}{T^{96}}$$

49.

$$7(-4) - (-5)^2 = -28 - 25 = -53$$

50.

$$6 + (-2)^5 - (-2)(8) = 6 + (-32) - (-16) = 6 - 32 + 16 = -10$$

51.

$$-(-26.5)^2 - (-9.85)^3 = -(702.25) - (-955.671625) = 253.421625$$

which gets rounded to 253 because 702.25 and -955.671625 are both accurate to only 3 significant digits due to the original numbers having only 3 significant digits.

52.

$-0.711^2 - (-0.809)^6 = (-1)(0.711)^2 - (-0.809)^6 = (-1)(0.505521) - (0.2803439122) = -0.7858649122$
 which gets rounded to 3 significant digits: -0.786 .

53.

$$\frac{3.07(-1.86)}{(-1.86)^4 + 1.596} = \frac{-5.7102}{11.96883216 + 1.596} = \frac{-5.7102}{13.56483216} = -0.420956185$$

which gets rounded to 3 significant digits: -0.421 .

54.

$$\frac{15.66^2 - (-4.017)^4}{1.044(-3.68)} = \frac{245.2356 - 260.379822692}{-3.84192} = \frac{-15.144222692}{-3.84192} = 3.941837074$$

which gets rounded to 3 significant digits: 3.94 .

55.

$$\begin{aligned} 2.38(-60.7)^2 - \frac{2540}{1.17^3} + 0.806^5(26.1^3 - 9.88^4) &= 2.38(3684.49) - \frac{2540}{1.601613} + 0.340153708(17779.581 - 9528.57108736) \\ &= 8769.0862 - 1585.901213339 + 0.340153708(8251.00991264) \\ &= 7183.184986661 + 2806.61161529 = 9989.79660319 \end{aligned}$$

which gets rounded to 3 significant digits: 9990 .

56.

$$\begin{aligned} 0.513(-2.778) - (-3.67)^3 + \frac{0.889^4}{1.89 - 1.09^2} \\ &= -1.425114 - (-49.430863) + \frac{0.624607283}{1.89 - 1.1881} \\ &= 48.005749 + \frac{0.624607283}{0.7019} \\ &= 48.005749 + 0.889880728 \\ &= 48.895629728 \end{aligned}$$

which gets rounded to 3 significant digits: 48.9 .

57.

$$\left(\frac{1}{x^{-1}}\right)^{-1} = \frac{1^{-1}}{x^{-1(-1)}} = \frac{1}{x}, \text{ which is the reciprocal of } x.$$

58.

$$\left(\frac{0.2 - 5^{-1}}{10^{-2}}\right)^0 = \left(\frac{0.2 - \frac{1}{5}}{\frac{1}{100}}\right)^0 = \left(\frac{0}{0.01}\right)^0 = 0^0 \neq 1, \text{ since } a^0 = 1 \text{ requires that } a \neq 0.$$

59.If $a^3 = 5$, then

$$a^{12} = a^{3(4)}$$

$$a^{12} = (a^3)^4$$

$$a^{12} = (5)^4$$

$$a^{12} = 625$$

60.If $\frac{1}{a^2} < \frac{1}{a}$, then for any negative value of a , a will be negative, and a^2 will be positive, making all values of $\frac{1}{a^2}$ greater than

$$\frac{1}{a}.$$

61. $(x^a \cdot x^{-a})^5 = (x^{a-a})^5 = (x^0)^5 = x^{0(5)} = x^0 = 1$, provided that $x \neq 0$.**62.**

$$(y^{a-b} \cdot y^{a+b})^2 = (y^{a-b+a+b})^2 = (y^{2a})^2 = y^{2a(2)} = y^{4a}.$$

63.

$$\begin{aligned} \left(\frac{kT}{hc}\right)^3 (GkThc)^2 c &= \frac{k^3 T^3}{h^3 c^3} \cdot (G^2 k^2 T^2 h^2 c^2) c \\ &= \frac{k^3 T^3}{h^3 c^3} \cdot (G^2 k^2 T^2 h^2 c^3) \\ &= \frac{(G^2 k^{2+3} T^{2+3} c^{3-3})}{h^1} \\ &= \frac{G^2 k^5 T^5}{h} \end{aligned}$$

64.

$$GmM(mr)^{-1}(r^{-2}) = \frac{GmM}{mr^{1+2}} = \frac{GM}{r^3}$$

65.

$$\pi \left(\frac{r}{2}\right)^3 \left(\frac{4}{3\pi r^2}\right) = \pi \left(\frac{r^3}{8}\right) \left(\frac{4}{3\pi r^2}\right) = \frac{4r}{24} = \frac{r}{6}$$

66.

$$\begin{aligned} \frac{gM}{2\pi fC(2\pi fM)^2} &= \frac{gM}{2\pi fC(4\pi^2 f^2 M^2)} \\ &= \frac{gM}{8\pi^3 f^3 CM^2} \\ &= \frac{g}{8\pi^3 f^3 CM} \end{aligned}$$

67.

$$\begin{aligned}2500\left(1 + \frac{0.042}{4}\right)^{24} &= \$2500(1.0105)^{24} \\ &= \$2500(1.28490602753) \\ &= \$3212.26700688 \\ &= \$3212.27\end{aligned}$$

68.

$$\begin{aligned}\frac{6.85(1000 - 20(6.85)^2 + (6.85)^3)}{1850} &= \frac{6.85(1000 - 20(46.9225) + (321.419125))}{1850} \\ &= \frac{6.85(1321.419125 - 938.45)}{1850} \\ &= \frac{6.85(382.969125)}{1850} \\ &= \frac{2623.33850625}{1850} \\ &= 1.418020814 \\ &= 1.42 \text{ cm}\end{aligned}$$

1.5 Scientific Notation

1.

$$8.06 \times 10^3 = 8060$$

2.

$$\begin{aligned} 750\,000\,000\,000^{-1} &= (7.5 \times 10^{11})^{-1} \\ &= 7.5^{-1} \times 10^{-11} \\ &= 0.1333\ldots \times 10^{-11} \\ &= 1.33 \times 10^{-12} \end{aligned}$$

rounded to 3 significant digits.

3.

$$4.5 \times 10^4 = 45\,000$$

4.

$$6.8 \times 10^7 = 68\,000\,000$$

5.

$$2.01 \times 10^{-3} = 0.002\,01$$

6.

$$9.61 \times 10^{-5} = 0.000\,096\,1$$

7.

$$3.23 \times 10^0 = 3.23 \times 1 = 3.23$$

8.

$$8 \times 10^0 = 8 \times 1 = 8$$

9.

$$1.86 \times 10 = 18.6$$

10.

$$1 \times 10^{-1} = 0.1$$

11.

$$4000 = 4 \times 10^3$$

12.

$$56\,000 = 5.6 \times 10^4$$

13.

$$0.0087 = 8.7 \times 10^{-3}$$

14.

$$0.7 = 7 \times 10^{-1}$$

15.

$$6.09 = 6.09 \times 10^0$$

16.

$$100 = 1 \times 10^2$$

17.

$$0.063 = 6.3 \times 10^{-2}$$

18.

$$0.000\ 090\ 8 = 9.08 \times 10^{-5}$$

19.

$$1 = 1 \times 10^0$$

20.

$$10 = 1 \times 10^1$$

21.

$$28\ 000(2\ 000\ 000\ 000) = 2.8 \times 10^4 (2 \times 10^9) = 5.6 \times 10^{13}$$

22.

$$50\ 000(0.006) = 5 \times 10^4 (6 \times 10^{-3}) = 300 = 3 \times 10^2$$

23.

$$\frac{88\ 000}{0.0004} = \frac{8.8 \times 10^4}{4 \times 10^{-4}} = 2.2 \times 10^8$$

24.

$$\frac{0.000\ 03}{6\ 000\ 000} = \frac{3 \times 10^{-5}}{6 \times 10^6} = 5 \times 10^{-12}$$

25.

$$2 \times 10^{-35} + 3 \times 10^{-34} = 0.2 \times 10^{-34} + 3 \times 10^{-34} = 3.2 \times 10^{-34}$$

26.

$$5.3 \times 10^{12} - 3.7 \times 10^{10} = 530 \times 10^{10} - 3.7 \times 10^{10} = 526.3 \times 10^{10} = 5.263 \times 10^{12}$$

27.

$$(1.2 \times 10^{29})^3 = 1.2^3 \times 10^{29(3)} = 1.728 \times 10^{87}$$

28

$$(2 \times 10^{-16})^{-5} = 2^{-5} \times 10^{-16(-5)} = 0.031\ 25 \times 10^{80} = 3.125 \times 10^{78}$$

29.

$$1280(865\ 000)(43.8) = 4.849\ 536 \times 10^{10}$$

which gets rounded to 4.85×10^{10} .

30.

$$0.0000569(3,190,000) = 181.511$$

which gets rounded to 1.82×10^2 .

31.

$$\frac{0.0732(6710)}{0.00134(0.0231)} = \frac{491.172}{0.000030954} = 1.5867803 \times 10^7$$

which gets rounded to 1.59×10^7 .

32.

$$\frac{0.00452}{2430(97100)} = \frac{0.00452}{235953000} = 1.915635741 \times 10^{-11}$$

which gets rounded to 1.92×10^{-11} .

33.

$$(3.642 \times 10^{-8})(2.736 \times 10^5) = 9.964512 \times 10^{-3}$$

which gets rounded to 9.965×10^{-3} .

34.

$$\frac{(7.309 \times 10^{-1})^2}{5.9843(2.5036 \times 10^{-20})} = \frac{0.53421481}{1.49787029 \times 10^{-19}} = 3.56656723394 \times 10^{18}$$

which gets rounded to 3.567×10^{18} .

35.

$$\frac{(3.69 \times 10^{-7})(4.61 \times 10^{21})}{0.0504} = \frac{1.70109 \times 10^{15}}{0.0504} = 3.37517857142 \times 10^{16}$$

which gets rounded to 3.38×10^{16} .

36.

$$\frac{(9.907 \times 10^7)(1.08 \times 10^{12})^2}{(3.603 \times 10^{-5})(2054)} = \frac{(9.907 \times 10^7)(1.1664 \times 10^{24})}{0.07400562} = \frac{1.01555248 \times 10^{32}}{0.07400562} = 1.56143882045 \times 10^{33}$$

which gets rounded to 1.56×10^{33} .

37.

$$2000000 \text{ kW} = 2 \times 10^6 \text{ kW}$$

38.

$$8500000000 \text{ bytes} = 8.5 \times 10^{10} \text{ bytes}$$

39.

$$0.000003 \text{ W} = 3 \times 10^{-6} \text{ W}$$

40.

$$0.0075 \text{ mm} = 7.5 \times 10^{-3} \text{ mm}$$

41.

$$2000000000 \text{ Hz} = 2 \times 10^9 \text{ Hz}$$

42.

$$3.086 \times 10^{16} \text{ m} = 30\,860\,000\,000\,000\,000 \text{ m}$$

43.

$$1.6 \times 10^{-12} \text{ W} = 0.000\,000\,000\,001\,6 \text{ W}$$

44.

$$2.4 \times 10^{-43} = 0.000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,24$$

45.

$$\begin{aligned} 2\,000\,000 \text{ kW} &= 2 \times 10^6 \text{ kW} \\ &= 2 \times 10^6 \times 10^3 \text{ W} \\ &= 2 \times 10^9 \text{ W} \\ &= 2 \text{ GW} \end{aligned}$$

46.

$$\begin{aligned} 85\,000\,000\,000 \text{ bytes} &= 85 \times 10^9 \text{ bytes} \\ &= 85 \text{ gigabytes} \end{aligned}$$

47.

$$\begin{aligned} 0.000\,003 \text{ W} &= 3 \times 10^{-6} \text{ W} \\ &= 3 \mu\text{W} \end{aligned}$$

48.

$$\begin{aligned} 0.0075 \text{ mm} &= 7.5 \times 10^{-3} \text{ mm} \\ &= 7.5 \times 10^{-3} \times 10^{-3} \text{ m} \\ &= 7.5 \times 10^{-6} \text{ m} \\ &= 7.5 \mu\text{m} \end{aligned}$$

49.

$$\begin{aligned} 2\,000\,000\,000 \text{ Hz} &= 2 \times 10^9 \text{ Hz} \\ &= 2 \text{ GHz} \end{aligned}$$

50.

- (a) $2300 = 2.3 \times 10^3$
- (b) $0.23 = 230 \times 10^{-3}$
- (c) $23 = 23 \times 10^0$

51.

- (a) $8\,090\,000 = 8.09 \times 10^6$
- (b) $809\,000 = 809 \times 10^3$
- (c) $0.0809 = 80.9 \times 10^{-3}$

52.

(a)

$$\text{googol} = 1 \times 10^{100} = 10^{100}$$

(b)

$$\text{googolplex} = 10^{\text{googol}} = 10^{10^{100}}$$

53.

$$\text{googol} = 10^{100}, \text{ so to find the ratio } \frac{10^{100}}{10^{79}} = 10^{100-79} = 10^{21}$$

A googol is 10^{21} times larger than the number of electrons in the universe.

54.

$$\frac{7.5 \times 10^{-15} \text{ s}}{\text{addition}} \times 5.6 \times 10^6 \text{ additions} = 4.2 \times 10^{-8} \text{ s}$$

55.

$$0.000\ 000\ 039\ \% = 0.000\ 000\ 000\ 39$$

$$0.000\ 000\ 000\ 39 \times 0.085 \text{ mg} = 3.315 \times 10^{-11} \text{ mg} = 3.3 \times 10^{-11} \text{ mg}$$

56.

$$\frac{7.3 \times 10^4 \text{ km}}{3.00 \times 10^5 \text{ km/s}} = 2.456\dots \times 10^{-1} \text{ s} = 2.46 \times 10^{-1} \text{ s}$$

57.

(a)

$$1 \text{ day} \times \frac{24 \text{ h}}{\text{day}} \times \frac{60 \text{ min}}{\text{h}} \times \frac{60 \text{ s}}{\text{min}} = 86400 \text{ s} = 8.64 \times 10^4 \text{ s}$$

(b)

$$100 \text{ year} \times \frac{365.25 \text{ day}}{\text{year}} \times \frac{24 \text{ h}}{\text{day}} \times \frac{60 \text{ min}}{\text{h}} \times \frac{60 \text{ s}}{\text{min}} = 3\ 155\ 760\ 000 \text{ s} = 3.155\ 760\ 0 \times 10^9 \text{ s}$$

58.

$$\frac{1.66 \times 10^{-27} \text{ kg}}{\text{amu}} \times \frac{1.6 \times 10^1 \text{ amu}}{\text{oxygen atoms}} \times 1.25 \times 10^8 \text{ oxygen atoms} = 3.32 \times 10^{-18} \text{ kg}$$

59.

$$W = kT^4$$

$$W = 5.7 \times 10^{-8} \text{ W/K}^4 \times (3.03 \times 10^2 \text{ K})^4$$

$$W = 5.7 \times 10^{-8} \text{ W/K}^4 \times 8.428\ 892\ 481 \times 10^9 \text{ K}^4$$

$$W = 4.804\ 468\ 714\ 17 \times 10^2 \text{ W}$$

$$W = 4.8 \times 10^2 \text{ W}$$

60.

$$R = \frac{k}{d^2} = \frac{2.196 \times 10^{-8} \Omega \cdot \text{m}^2}{(7.998 \times 10^{-5} \text{m})^2} = \frac{2.196 \times 10^{-8} \Omega \cdot \text{m}^2}{6.3968004 \times 10^{-9} \text{m}^2} = 3.43296626857 \Omega = 3.433 \Omega$$

61.

$$\frac{1.496 \times 10^8 \text{km}}{\text{AU}} \times \frac{\text{AU}}{4.99 \times 10^2 \text{s}} = 2.99799599198 \times 10^5 \text{km/s} = 2.998 \times 10^5 \text{km/s}$$

This is the same speed mentioned in Question 56 as the speed of radio waves.

1.6 Roots and Radicals

1.

$$-\sqrt[3]{64} = -\sqrt[3]{(4)^3} = -4$$

2.

$$\sqrt{(15)(5)}$$

Neither 15 nor 5 is a perfect square, so this expression is not as useful. However, if we further factor the 15 to $\sqrt{(3)(5)(5)} = \sqrt{3(5)^2} = 5\sqrt{3}$, the result can still be obtained.

3.

$$\sqrt{16 \times 9} = \sqrt{144} = \sqrt{12^2} = 12$$

4.

$-\sqrt{-64}$ is still imaginary because an even root (in this case $n = 2$) of a negative number is imaginary, regardless of the numerical factor placed in front of the root.

5.

$$\sqrt{81} = \sqrt{9^2} = 9$$

6.

$$\sqrt{225} = \sqrt{(25)(9)} = \sqrt{25} \times \sqrt{9} = 5 \times 3 = 15$$

7.

$$-\sqrt{121} = -\sqrt{11^2} = -11$$

8.

$$-\sqrt{36} = -\sqrt{6^2} = -6$$

9.

$$-\sqrt{49} = -\sqrt{7^2} = -7$$

10.

$$\sqrt{0.25} = \sqrt{\frac{1}{4}} = \frac{\sqrt{1}}{\sqrt{4}} = \frac{1}{2} = 0.5$$

11.

$$\sqrt{0.09} = \sqrt{\frac{9}{100}} = \frac{\sqrt{9}}{\sqrt{100}} = \frac{3}{10} = 0.3$$

12.

$$-\sqrt{900} = -\sqrt{(9)(100)} = -\sqrt{9} \times \sqrt{100} = -3 \times 10 = -30$$

13.

$$\sqrt[3]{125} = \sqrt[3]{5^3} = 5$$

14.

$$\sqrt[4]{16} = \sqrt[4]{2^4} = 2$$

15.

$$\sqrt[3]{-216} = \sqrt[3]{(-6)^3} = -6$$

16.

$$\sqrt[5]{-32} = \sqrt[5]{(-2)^5} = -2$$

17.

$$(\sqrt{5})^2 = \sqrt{5} \times \sqrt{5} = 5$$

18.

$$(\sqrt[3]{31})^3 = \sqrt[3]{31} \times \sqrt[3]{31} \times \sqrt[3]{31} = 31$$

19.

$$(-\sqrt[3]{-47})^3 = (-1)^3 (\sqrt[3]{-47})^3 = (-1)(-47) = 47$$

20.

$$(\sqrt[5]{-23})^5 = -23$$

21.

$$(-\sqrt[4]{53})^4 = (-1)^4 (\sqrt[4]{53})^4 = (1)(53) = 53$$

22.

$$-\sqrt{32} = -\sqrt{(16)(2)} = -\sqrt{16} \times \sqrt{2} = -4\sqrt{2}$$

23.

$$\sqrt{1200} = \sqrt{(100)(4)(3)} = \sqrt{100} \times \sqrt{4} \times \sqrt{3} = 10 \times 2 \times \sqrt{3} = 20\sqrt{3}$$

24.

$$\sqrt{50} = \sqrt{(25)(2)} = \sqrt{25} \times \sqrt{2} = 5 \times \sqrt{2} = 5\sqrt{2}$$

25.

$$2\sqrt{84} = 2\sqrt{(4)(21)} = 2 \times \sqrt{4} \times \sqrt{21} = 2 \times 2 \times \sqrt{21} = 4\sqrt{21}$$

26.

$$\frac{\sqrt{108}}{2} = \frac{\sqrt{(36)(3)}}{2} = \frac{\sqrt{36} \times \sqrt{3}}{2} = \frac{6 \times \sqrt{3}}{2} = 3\sqrt{3}$$

27.

$$\sqrt{\frac{80}{7-3}} = \sqrt{\frac{80}{4}} = \sqrt{20} = \sqrt{4 \times 5} = \sqrt{4} \times \sqrt{5} = 2 \times \sqrt{5} = 2\sqrt{5}$$

28.

$$\sqrt{81 \times 10^2} = \sqrt{81} \times \sqrt{10^2} = 9 \times 10 = 90$$

29.

$$\sqrt[3]{8^2} = \sqrt[3]{64} = \sqrt[3]{4^3} = 4$$

30.

$$\sqrt[4]{9^2} = \sqrt[4]{81} = \sqrt[4]{3^4} = 3$$

31.

$$\frac{7^2 \sqrt{81}}{3^2 \sqrt{49}} = \frac{(49)(9)}{(9)(7)} = \frac{(49)\cancel{9}}{\cancel{9}(7)} = 7$$

32.

$$\frac{2^5 \sqrt[5]{243}}{3 \sqrt{144}} = \frac{32 \sqrt[5]{3^5}}{3 \sqrt{12^2}} = \frac{(32)\cancel{3}}{\cancel{3}(12)} = \frac{8}{3}$$

33.

$$\sqrt{36+64} = \sqrt{100} = \sqrt{10^2} = 10$$

34.

$$\sqrt{25+144} = \sqrt{169} = \sqrt{13^2} = 13$$

35.

$$\sqrt{3^2+9^2} = \sqrt{9+81} = \sqrt{90} = \sqrt{(9)(10)} = \sqrt{9} \times \sqrt{10} = 3\sqrt{10}$$

36.

$$\sqrt{8^2-4^2} = \sqrt{64-16} = \sqrt{48} = \sqrt{(16)(3)} = \sqrt{16} \times \sqrt{3} = 4\sqrt{3}$$

37.

$$\sqrt{85.4} = 9.24121204171, \text{ which is rounded to } 9.24$$

38.

$$\sqrt{3762} = 61.3351449007, \text{ which is rounded to } 61.34$$

39.

$$\sqrt{0.4729} = 0.68767724987, \text{ which is rounded to } 0.6877$$

40.

$$\sqrt{0.0627} = 0.25039968051, \text{ which is rounded to } 0.250$$

41.

(a)

$$\sqrt{1296+2304} = \sqrt{3600} = 60, \text{ which is expressed as } 60.00$$

(b)

$$\sqrt{1296} + \sqrt{2304} = 36 + 48 = 84, \text{ which is expressed as } 84.00$$

42.**(a)**

$$\sqrt{10.6276 + 2.1609} = \sqrt{12.7885} = 3.57610122899, \text{ which is rounded to } 3.57610$$

(b)

$$\sqrt{10.6276} + \sqrt{2.1609} = 3.26 + 1.47 = 4.73, \text{ which is expressed as } 4.7300$$

43.**(a)**

$$\begin{aligned} \sqrt{0.0429^2 - 0.0183^2} &= \sqrt{0.00184041 - 0.00033489} \\ &= \sqrt{0.00150552} \\ &= 0.03880103091 \\ &= 0.0388 \end{aligned}$$

(b)

$$\begin{aligned} \sqrt{0.0429^2} - \sqrt{0.0183^2} &= 0.0429 - 0.0183 \\ &= 0.0246 \end{aligned}$$

44.**(a)**

$$\begin{aligned} \sqrt{3.625^2 + 0.614^2} &= \sqrt{13.140625 + 0.376996} \\ &= \sqrt{13.517621} \\ &= 3.67663174658 \\ &= 3.677 \end{aligned}$$

(b)

$$\begin{aligned} \sqrt{3.625^2} + \sqrt{0.614^2} &= 3.625 + 0.614 \\ &= 4.239 \end{aligned}$$

45.

$$\sqrt{207s} = \sqrt{(207)(46)} = \sqrt{9522} = 97.5807358037 = 98 \text{ km/h}$$

46.

$$\begin{aligned} \sqrt{Z^2 - X^2} &= \sqrt{(5.362 \Omega)^2 - (2.875 \Omega)^2} \\ &= \sqrt{28.751044 \Omega^2 - 8.265625 \Omega^2} \\ &= \sqrt{20.485419 \Omega^2} \\ &= 4.52608208056 \Omega \\ &= 4.526 \Omega \end{aligned}$$

47.

$$\begin{aligned}
 \sqrt{\frac{B}{d}} &= \sqrt{\frac{2.18 \times 10^9 \text{ Pa}}{1.03 \times 10^3 \text{ kg/m}^3}} \\
 &= \sqrt{2116504.85436 \frac{\text{N/m}^2}{\text{kg/m}^3}} \\
 &= \sqrt{2116504.85436 \frac{(\text{kg} \cdot \text{m/s}^2)/\text{m}^2}{\text{kg/m}^3}} \\
 &= \sqrt{2116504.85436 \text{ m}^2/\text{s}^2} \\
 &= 1454.82124481 \text{ m/s} \\
 &= 1450 \text{ m/s}
 \end{aligned}$$

48.

$$\begin{aligned}
 \sqrt{40m} &= \sqrt{(40)(75)} \\
 &= \sqrt{3000} \\
 &= 54.7722557505 \\
 &= 55 \text{ m/s}
 \end{aligned}$$

49.

$$\begin{aligned}
 \sqrt{w^2 + h^2} &= \sqrt{(93.0 \text{ cm})^2 + (52.1 \text{ cm})^2} \\
 &= \sqrt{8649 \text{ cm}^2 + 2714.41 \text{ cm}^2} \\
 &= \sqrt{11363.41 \text{ cm}^2} \\
 &= 106.599296432 \text{ cm} \\
 &= 107 \text{ cm}
 \end{aligned}$$

50.

$$\begin{aligned}
 100 \left(1 - \sqrt{\frac{V}{C}} \right) &= 100 \left(1 - \sqrt{\frac{15000}{22000}} \right) \\
 &= 100 \left(1 - \sqrt{0.68181818181} \right) \\
 &= 100(1 - 0.82572282684) \\
 &= 100(0.17427717615) \\
 &= 17.427717615 \% \\
 &= 17 \%
 \end{aligned}$$

51.

$\sqrt{a^2} = a$ is not necessarily true for negative values of a because a^2 will be a positive number, regardless whether a is negative or positive. The principal root calculated is assumed to be positive, but there are always two solutions to a square root, $\sqrt{a^2} = \pm a$ since $(+a)^2 = a^2$ and $(-a)^2 = a^2$ (see the introduction to this chapter section), so it is sometimes true and sometimes false for negative values of a , depending on which root solution is desired. If *only principal roots* are considered, then it will *not* be true for negative values of a . For example, $\sqrt{(-4)^2} = \sqrt{16} = 4 \neq -4$.

52.

(a) $x > \sqrt{x}$ when $x > 1$. Any number greater than 1 will have a square root that is smaller than itself. For example, $2 > \sqrt{2} = 1.41$

(b) $x = \sqrt{x}$ when $x = 1$ or $x = 0$ because the only numbers that are their own squares are 0 and 1 (i.e., $0^2 = 0$ and $1^2 = 1$).

(c) $x < \sqrt{x}$ when $0 < x < 1$. Any number between 0 and 1 will have a square root larger than itself. For example, $0.25 < \sqrt{0.25} = 0.5$

53.

(a)

$\sqrt[3]{2140} = 12.8865874254$, which is rounded to 12.9

(b)

$\sqrt[3]{-0.214} = -0.59814240297$, which is rounded to -0.598

A calculator screen showing two calculations. The first line shows the cube root of 2140, resulting in 12.88658743. The second line shows the cube root of -0.214, resulting in -0.598142403.

54.

(a)

$\sqrt[7]{0.382} = 0.87155493458$, which is rounded to 0.872

(b)

$\sqrt[7]{-382} = -2.33811675837$, which is rounded to -2.34

A calculator screen showing two calculations. The first line shows the seventh root of 0.382, resulting in 0.8715549346. The second line shows the seventh root of -382, resulting in -2.338116758.

55.

(a) $\sqrt[4]{-81}$ is imaginary since it is an even root of a negative number.

(b) $\sqrt[7]{-128}$ is real since it is an odd root of a negative number.

56.

(a) $\sqrt[3]{-32} = -2$ is real since it is an odd root of a negative number.

(b) $\sqrt[4]{-64}$ is imaginary since it is an even root of a negative number.

1.7 Addition and Subtraction of Algebraic Expressions

1.

$$3x + 2y - 5y = 3x - 3y$$

2.

$$3c - (2b - c) = 3c - 2b + c = -2b + 4c$$

3.

$$\begin{aligned} 3ax - [(ax - 5s) - 2ax] &= 3ax - [ax - 5s - 2ax] \\ &= 3ax - [-ax - 5s] \\ &= 3ax + ax + 5s \\ &= 4ax + 5s \end{aligned}$$

4.

$$\begin{aligned} 3a^2b - \{a - [2a^2b - (a + 2b)]\} &= 3a^2b - \{a - [2a^2b - a - 2b]\} \\ &= 3a^2b - \{a - 2a^2b + a + 2b\} \\ &= 3a^2b - \{2a - 2a^2b + 2b\} \\ &= 3a^2b - 2a + 2a^2b - 2b \\ &= 5a^2b - 2a - 2b \end{aligned}$$

5.

$$5x + 7x - 4x = 8x$$

6.

$$6t - 3t - 4t = -t$$

7.

$$2y - y + 4x = y + 4x$$

8.

$$4C + L - 6C = -2C + L$$

9.

$$2F - 2T - 2 + 3F - T = 5F - 3T - 2$$

10.

$$x - 2y + 3x - y + z = 4x - 3y + z$$

11.

$$a^2b - a^2b^2 - 2a^2b = -a^2b - a^2b^2$$

12.

$$xy^2 - 3x^2y^2 + 2xy^2 = 3xy^2 - 3x^2y^2$$

13.

$$s + (3s - 4 - s) = s + (2s - 4) = s + 2s - 4 = 3s - 4$$

14.

$$5 + (3 - 4n + p) = 5 + 3 - 4n + p = -4n + p + 8$$

15.

$$v - (4 - 5x + 2v) = v - 4 + 5x - 2v = -v + 5x - 4$$

16.

$$2a - (b - a) = 2a - b + a = 3a - b$$

17.

$$2 - 3 - (4 - 5a) = -1 - 4 + 5a = 5a - 5$$

18.

$$\sqrt{A} + (h - 2\sqrt{A}) - 3\sqrt{A} = \sqrt{A} + h - 2\sqrt{A} - 3\sqrt{A} = -4\sqrt{A} + h$$

19.

$$(a - 3) + (5 - 6a) = a - 3 + 5 - 6a = -5a + 2$$

20.

$$(4x - y) - (-2x - 4y) = 4x - y + 2x + 4y = 6x + 3y$$

21.

$$-(t - 2u) + (3u - t) = -t + 2u + 3u - t = -2t + 5u$$

22.

$$2(x - 2y) + (5x - y) = 2x - 4y + 5x - y = 7x - 5y$$

23.

$$3(2r + s) - (-5s - r) = 6r + 3s + 5s + r = 7r + 8s$$

24.

$$3(a - b) - 2(a - 2b) = 3a - 3b - 2a + 4b = a + b$$

25.

$$-7(6 - 3j) - 2(j + 4) = -42 + 21j - 2j - 8 = 19j - 50$$

26.

$$-(5t + a^2) - 2(3a^2 - 2st) = -5t - a^2 - 6a^2 + 4st = -7a^2 + 4st - 5t$$

27.

$$\begin{aligned} -[(6 - n) - (2n - 3)] &= -[6 - n - 2n + 3] \\ &= -[-3n + 9] \\ &= 3n - 9 \end{aligned}$$

28.

$$\begin{aligned} -[(A - B) - (B - A)] &= -[A - B - B + A] \\ &= -[2A - 2B] \\ &= -2A + 2B \end{aligned}$$

29.

$$\begin{aligned} 2[4 - (t^2 - 5)] &= 2[4 - t^2 + 5] \\ &= 2[-t^2 + 9] \\ &= -2t^2 + 18 \end{aligned}$$

30.

$$\begin{aligned} 3[-3 - (a - 4)] &= 3[-3 - a + 4] \\ &= 3[-a + 1] \\ &= -3a + 3 \end{aligned}$$

31.

$$\begin{aligned} -2[-x - 2a - (a - x)] &= -2[-x - 2a - a + x] \\ &= -2[-3a] \\ &= 6a \end{aligned}$$

32.

$$\begin{aligned} -2[-3(x - 2y) + 4y] &= -2[-3x + 6y + 4y] \\ &= -2[-3x + 10y] \\ &= 6x - 20y \end{aligned}$$

33.

$$\begin{aligned} aZ - [3 - (aZ + 4)] &= aZ - [3 - aZ - 4] \\ &= aZ - [-aZ - 1] \\ &= aZ + aZ + 1 \\ &= 2aZ + 1 \end{aligned}$$

34.

$$\begin{aligned} 9v - [6 - (v - 4) + 4v] &= 9v - [6 - v + 4 + 4v] \\ &= 9v - [3v + 10] \\ &= 9v - 3v - 10 \\ &= 6v - 10 \end{aligned}$$

35.

$$\begin{aligned} 8c - \{5 - [2 - (3 + 4c)]\} &= 8c - \{5 - [2 - 3 - 4c]\} \\ &= 8c - \{5 - 2 + 3 + 4c\} \\ &= 8c - \{6 + 4c\} \\ &= 8c - 6 - 4c \\ &= 4c - 6 \end{aligned}$$

36.

$$\begin{aligned} 7y - \{y - [2y - (x - y)]\} &= 7y - \{y - [2y - x + y]\} \\ &= 7y - \{y - [3y - x]\} \\ &= 7y - \{y - 3y + x\} \\ &= 7y - \{-2y + x\} \\ &= 7y + 2y - x \\ &= -x + 9y \end{aligned}$$

37.

$$\begin{aligned}
 5p - (q - 2p) - [3q - (p - q)] &= 5p - q + 2p - [3q - p + q] \\
 &= 5p - q + 2p - [4q - p] \\
 &= 7p - q - 4q + p \\
 &= 8p - 5q
 \end{aligned}$$

38.

$$\begin{aligned}
 -(4 - \sqrt{LC}) - [(5\sqrt{LC} - 7) - (6\sqrt{LC} + 2)] &= -4 + \sqrt{LC} - [5\sqrt{LC} - 7 - 6\sqrt{LC} - 2] \\
 &= -4 + \sqrt{LC} - [-\sqrt{LC} - 9] \\
 &= -4 + \sqrt{LC} + \sqrt{LC} + 9 \\
 &= 2\sqrt{LC} + 5
 \end{aligned}$$

39.

$$\begin{aligned}
 -2\{-(4 - x^2) - [3 + (4 - x^2)]\} &= -2\{-4 + x^2 - [3 + 4 - x^2]\} \\
 &= -2\{-4 + x^2 - 3 - 4 + x^2\} \\
 &= -2\{2x^2 - 11\} \\
 &= -4x^2 + 22
 \end{aligned}$$

40.

$$\begin{aligned}
 -\{-(x - 2a) - b\} - (a - x) &= -\{-x + 2a - b\} - a + x \\
 &= -\{x - 2a + b - a + x\} \\
 &= -\{-3a + b + 2x\} \\
 &= 3a - b - 2x
 \end{aligned}$$

41.

$$\begin{aligned}
 5V^2 - (6 - (2V^2 + 3)) &= 5V^2 - (6 - 2V^2 - 3) \\
 &= 5V^2 - (-2V^2 + 3) \\
 &= 5V^2 + 2V^2 - 3 \\
 &= 7V^2 - 3
 \end{aligned}$$

42.

$$\begin{aligned}
 -2F + 2((2F - 1) - 5) &= -2F + 2(2F - 1 - 5) \\
 &= -2F + 2(2F - 6) \\
 &= -2F + 4F - 12 \\
 &= 2F - 12
 \end{aligned}$$

43.

$$\begin{aligned}
 -(3t - (7 + 2t - (5t - 6))) &= -(3t - (7 + 2t - 5t + 6)) \\
 &= -(3t - (-3t + 13)) \\
 &= -(3t + 3t - 13) \\
 &= -(6t - 13) \\
 &= -6t + 13
 \end{aligned}$$

44.

$$\begin{aligned}
 a^2 - 2(x - 5 - (7 - 2(a^2 - 2x) - 3x)) &= a^2 - 2(x - 5 - (7 - 2a^2 + 4x - 3x)) \\
 &= a^2 - 2(x - 5 - (7 - 2a^2 + x)) \\
 &= a^2 - 2(x - 5 - 7 + 2a^2 - x) \\
 &= a^2 - 2(2a^2 - 12) \\
 &= a^2 - 4a^2 + 24 \\
 &= -3a^2 + 24
 \end{aligned}$$

45.

$$\begin{aligned}
 -4[4R - 2.5(Z - 2R) - 1.5(2R - Z)] &= -4[4R - 2.5Z + 5R - 3R + 1.5Z] \\
 &= -4[6R - Z] \\
 &= -24R + 4Z
 \end{aligned}$$

46.

$$\begin{aligned}
 3\{2.1e - 1.3[f - 2(e - 5f)]\} &= 3\{2.1e - 1.3[f - 2e + 10f]\} \\
 &= 3\{2.1e - 1.3[-2e + 11f]\} \\
 &= 3\{2.1e + 2.6e - 14.3f\} \\
 &= 3\{4.7e - 14.3f\} \\
 &= 14.1e - 42.9f
 \end{aligned}$$

47.

$$3D - (D - d) = 3D - D + d = 2D + d$$

48.

$$i_1 - (2 - 3i_2) + i_2 = i_1 - 2 + 3i_2 + i_2 = i_1 + 4i_2 - 2$$

49.

$$\begin{aligned}
 \left[\left(B + \frac{4}{3}\alpha \right) + 2 \left(B - \frac{2}{3}\alpha \right) \right] - \left[\left(B + \frac{4}{3}\alpha \right) - \left(B - \frac{2}{3}\alpha \right) \right] &= \left[B + \frac{4}{3}\alpha + 2B - \frac{4}{3}\alpha \right] - \left[B + \frac{4}{3}\alpha - B + \frac{2}{3}\alpha \right] \\
 &= [3B] - \left[\frac{6}{3}\alpha \right] \\
 &= 3B - 2\alpha
 \end{aligned}$$

50.

$$\begin{aligned}
 \text{Distance} &= 30 \text{ km/h} \times (t - 1) \text{ h} + 40 \text{ km/h} \times (t + 2) \text{ h} \\
 &= 30(t - 1) \text{ km} + 40(t + 2) \text{ km} \\
 &= (30t - 30 + 40t + 80) \text{ km} \\
 &= (70t + 50) \text{ km}
 \end{aligned}$$

51.

$$\begin{aligned}
 \text{Photos} &= x(15 \text{ exposures}) + (x + 10)(25 \text{ exposures}) \\
 &= (15x + 25x + 250) \text{ exposures} \\
 &= (40x + 250) \text{ exposures}
 \end{aligned}$$

52.

$$\begin{aligned}
 \text{Difference} &= 2[(2n+1)(\$3) - (n-2)(\$2)] \\
 &= \$ 2[6n+3-2n+4] \\
 &= \$ 2[4n+7] \\
 &= \$ (8n+14)
 \end{aligned}$$

53.**(a)**

$$\begin{aligned}
 (2x^2 - y + 2a) + (3y - x^2 - b) &= 2x^2 - y + 2a + 3y - x^2 - b \\
 &= x^2 + 2y + 2a - b
 \end{aligned}$$

(b)

$$\begin{aligned}
 (2x^2 - y + 2a) - (3y - x^2 - b) &= 2x^2 - y + 2a - 3y + x^2 + b \\
 &= 3x^2 - 4y + 2a + b
 \end{aligned}$$

54.

$$\begin{aligned}
 (3a^2 + b - c^3) + (2c^3 - 2b - a^2) - (4c^3 - 4b + 3) &= 3a^2 + b - c^3 + 2c^3 - 2b - a^2 - 4c^3 + 4b - 3 \\
 &= 2a^2 + 3b - 3c^3 - 3
 \end{aligned}$$

55.

$$\begin{aligned}
 |a - b| &= | -(-a + b) | \\
 &= | -(b - a) | \\
 &= | -1 \times (b - a) | \\
 &= | -1 | \times | (b - a) | \\
 &= 1 \times | (b - a) | \\
 &= | (b - a) |
 \end{aligned}$$

56.

$$(a - b) - c = a - b - c$$

However,

$$a - (b - c) = a - b + c$$

Since they are not equivalent, subtraction is not associative.

For example, $(10 - 5) - 2 = 5 - 2 = 3$ is not the same as $10 - (5 - 2) = 10 - 3 = 7$.

1.8 Multiplication of Algebraic Expressions

1.

$$\begin{aligned} 2s^3(-st^4)^3(4s^2t) &= 2s^3(-1)^3s^3t^{12}(4s^2t) \\ &= -2s^6t^{12}(4s^2t) \\ &= -8s^8t^{13} \end{aligned}$$

2.

$$\begin{aligned} -2ax(3ax^2 - 4yz) &= (-2ax)(3ax^2) - (-2ax)(4yz) \\ &= (-6a^2x^3) - (-8axyz) \\ &= -6a^2x^3 + 8axyz \end{aligned}$$

3.

$$\begin{aligned} (x-2)(x-3) &= x(x) + x(-3) + (-2)(x) + (-2)(-3) \\ &= x^2 - 3x - 2x + 6 \\ &= x^2 - 5x + 6 \end{aligned}$$

4.

$$\begin{aligned} (2a-b)^2 &= (2a-b)(2a-b) \\ &= (2a)(2a) + (2a)(-b) + (2a)(-b) + (-b)(-b) \\ &= 4a^2 - 2ab - 2ab + b^2 \\ &= 4a^2 - 4ab + b^2 \end{aligned}$$

5.

$$(a^2)(ax) = a^3x$$

6.

$$(2xy)(x^2y^3) = 2x^3y^4$$

7.

$$(-ac^2)(acx^3) = -a^2c^3x^3$$

8.

$$\begin{aligned} (-2cs^2)(-4cs)^2 &= (-2cs^2)(-4cs)(-4cs) \\ &= (-2cs^2)(16c^2s^2) \\ &= -32c^3s^4 \end{aligned}$$

9.

$$\begin{aligned} (2ax^2)^2(-2ax) &= (2ax^2)(2ax^2)(-2ax) \\ &= (4a^2x^4)(-2ax) \\ &= -8a^3x^5 \end{aligned}$$

10.

$$\begin{aligned}(6pq^3)(3pq^2)^2 &= (6pq^3)(3pq^2)(3pq^2) \\ &= (6pq^3)(9p^2q^4) \\ &= 54p^3q^7\end{aligned}$$

11.

$$\begin{aligned}i^2(R+2r) &= (i^2)(R) + (i^2)(2r) \\ &= i^2R + 2i^2r\end{aligned}$$

12.

$$\begin{aligned}2x(p-q) &= (2x)(p) - (2x)(q) \\ &= 2px - 2qx\end{aligned}$$

13.

$$\begin{aligned}-3s(s^2-5t) &= (-3s)(s^2) + (-3s)(-5t) \\ &= -3s^3 + 15st\end{aligned}$$

14.

$$\begin{aligned}-3b(2b^2-b) &= (-3b)(2b^2) + (-3b)(-b) \\ &= -6b^3 + 3b^2\end{aligned}$$

15.

$$\begin{aligned}5m(m^2n+3mn) &= (5m)(m^2n) + (5m)(3mn) \\ &= 5m^3n + 15m^2n\end{aligned}$$

16.

$$\begin{aligned}a^2bc(2ac-3b^2c) &= (a^2bc)(2ac) + (a^2bc)(-3b^2c) \\ &= 2a^3bc^2 - 3a^2b^3c^2\end{aligned}$$

17.

$$\begin{aligned}3M(-M-N+2) &= (3M)(-M) + (3M)(-N) + (3M)(2) \\ &= -3M^2 - 3MN + 6M\end{aligned}$$

18.

$$\begin{aligned}-4c^2(-9gc-2c+g^2) &= (-4c^2)(-9cg) + (-4c^2)(-2c) + (-4c^2)(g^2) \\ &= 36c^3g + 8c^3 - 4c^2g^2\end{aligned}$$

19.

$$\begin{aligned}ax(cx^2)(x+y^3) &= acx^3(x+y^3) \\ &= (acx^3)(x) + (acx^3)(y^3) \\ &= acx^4 + acx^3y^3\end{aligned}$$

20.

$$\begin{aligned}-2(-3st^3)(3s-4t) &= 6st^3(3s-4t) \\ &= (6st^3)(3s) + (6st^3)(-4t) \\ &= 18s^2t^3 - 24st^4\end{aligned}$$

21.

$$\begin{aligned}(x-3)(x+5) &= (x)(x) + (x)(5) + (-3)(x) + (-3)(5) \\ &= x^2 + 5x - 3x - 15 \\ &= x^2 + 2x - 15\end{aligned}$$

22.

$$\begin{aligned}(a+7)(a+1) &= (a)(a) + (a)(1) + (7)(a) + (7)(1) \\ &= a^2 + a + 7a + 7 \\ &= a^2 + 8a + 7\end{aligned}$$

23.

$$\begin{aligned}(x+5)(2x-1) &= (x)(2x) + (x)(-1) + (5)(2x) + (5)(-1) \\ &= 2x^2 - x + 10x - 5 \\ &= 2x^2 + 9x - 5\end{aligned}$$

24.

$$\begin{aligned}(4t_1 + t_2)(2t_1 - 3t_2) &= (4t_1)(2t_1) + (4t_1)(-3t_2) + (t_2)(2t_1) + (t_2)(-3t_2) \\ &= 8t_1^2 - 12t_1t_2 + 2t_1t_2 - 3t_2^2 \\ &= 8t_1^2 - 10t_1t_2 - 3t_2^2\end{aligned}$$

25.

$$\begin{aligned}(2a-b)(3a-2b) &= (2a)(3a) + (2a)(-2b) + (-b)(3a) + (-b)(-2b) \\ &= 6a^2 - 4ab - 3ab + 2b^2 \\ &= 6a^2 - 7ab + 2b^2\end{aligned}$$

26.

$$\begin{aligned}(4w^2 - 3)(3w^2 - 1) &= (4w^2)(3w^2) + (4w^2)(-1) + (-3)(3w^2) + (-3)(-1) \\ &= 12w^4 - 4w^2 - 9w^2 + 3 \\ &= 12w^4 - 13w^2 + 3\end{aligned}$$

27.

$$\begin{aligned}(2s+7t)(3s-5t) &= (2s)(3s) + (2s)(-5t) + (7t)(3s) + (7t)(-5t) \\ &= 6s^2 - 10st + 21st - 35t^2 \\ &= 6s^2 + 11st - 35t^2\end{aligned}$$

28.

$$\begin{aligned}(5p-2q)(p+8q) &= (5p)(p) + (5p)(8q) + (-2q)(p) + (-2q)(8q) \\ &= 5p^2 + 40pq - 2pq - 16q^2 \\ &= 5p^2 + 38pq - 16q^2\end{aligned}$$

29.

$$\begin{aligned}(x^2-1)(2x+5) &= (x^2)(2x) + (x^2)(5) + (-1)(2x) + (-1)(5) \\ &= 2x^3 + 5x^2 - 2x - 5\end{aligned}$$

30.

$$\begin{aligned}(3y^2 + 2)(2y - 9) &= (3y^2)(2y) + (3y^2)(-9) + (2)(2y) + (-9)(2) \\ &= 6y^3 - 27y^2 + 4y - 18\end{aligned}$$

31.

$$\begin{aligned}(x - 2y - 4)(x - 2y + 4) \\ &= (x)(x) + (x)(-2y) + (x)(4) + (-2y)(x) + (-2y)(-2y) + (-2y)(4) + (-4)(x) + (-4)(-2y) + (-4)(4) \\ &= x^2 - 2xy + 4x - 2xy + 4y^2 - 8y - 4x + 8y - 16 \\ &= x^2 + 4y^2 - 4xy - 16\end{aligned}$$

32.

$$\begin{aligned}(2a + 3b + 1)(2a + 3b - 1) \\ &= (2a)(2a) + (2a)(3b) + (2a)(-1) + (3b)(2a) + (3b)(3b) + (3b)(-1) + (1)(2a) + (1)(3b) + (1)(-1) \\ &= 4a^2 + 6ab - 2a + 6ab + 9b^2 - 3b + 2a + 3b - 1 \\ &= 4a^2 + 9b^2 + 12ab - 1\end{aligned}$$

33.

$$\begin{aligned}2(a + 1)(a - 9) &= 2[(a)(a) + (a)(-9) + (1)(a) + (-9)(1)] \\ &= 2[a^2 - 9a + a - 9] \\ &= 2[a^2 - 8a - 9] \\ &= 2a^2 - 16a - 18\end{aligned}$$

34.

$$\begin{aligned}-5(y - 3)(y + 6) &= -5[(y)(y) + (y)(6) + (-3)(y) + (-3)(6)] \\ &= -5[y^2 + 6y - 3y - 18] \\ &= -5[y^2 + 3y - 18] \\ &= -5y^2 - 15y + 90\end{aligned}$$

35.

$$\begin{aligned}-3(3 - 2T)(3T + 2) &= -3[(3)(3T) + (3)(2) + (-2T)(3T) + (-2T)(2)] \\ &= -3[-6T^2 + 9T - 4T + 6] \\ &= -3[-6T^2 + 5T + 6] \\ &= 18T^2 - 15T - 18\end{aligned}$$

36.

$$\begin{aligned}2n(5 - n)(6n + 5) &= 2n[(5)(6n) + (5)(5) + (-n)(6n) + (-n)(5)] \\ &= 2n[-6n^2 + 30n - 5n + 25] \\ &= 2n[-6n^2 + 25n + 25] \\ &= -12n^3 + 50n^2 + 50n\end{aligned}$$

37.

$$\begin{aligned}2L(L + 1)(4 - L) &= 2L[(L)(4) + (L)(-L) + (1)(4) + (1)(-L)] \\ &= 2L[-L^2 + 4L - L + 4] \\ &= 2L[-L^2 + 3L + 4] \\ &= -2L^3 + 6L^2 + 8L\end{aligned}$$

38.

$$\begin{aligned}
 ax(x+4)(7-x^2) &= ax[(x)(7) + (x)(-x^2) + (4)(7) + (4)(-x^2)] \\
 &= ax[-x^3 - 4x^2 + 7x + 28] \\
 &= -ax^4 - 4ax^3 + 7ax^2 + 28ax
 \end{aligned}$$

39.

$$\begin{aligned}
 (2x-5)^2 &= (2x-5)(2x-5) \\
 &= (2x)(2x) + (2x)(-5) + (-5)(2x) + (-5)(-5) \\
 &= 4x^2 - 10x - 10x + 25 \\
 &= 4x^2 - 20x + 25
 \end{aligned}$$

40.

$$\begin{aligned}
 (x-3y)^2 &= (x-3y)(x-3y) \\
 &= (x)(x) + (x)(-3y) + (-3y)(x) + (-3y)(-3y) \\
 &= x^2 - 3xy - 3xy + 9y^2 \\
 &= x^2 - 6xy + 9y^2
 \end{aligned}$$

41.

$$\begin{aligned}
 (x_1 + 3x_2)^2 &= (x_1 + 3x_2)(x_1 + 3x_2) \\
 &= (x_1)(x_1) + (x_1)(3x_2) + (3x_2)(x_1) + (3x_2)(3x_2) \\
 &= x_1^2 + 3x_1x_2 + 3x_1x_2 + 9x_2^2 \\
 &= x_1^2 + 6x_1x_2 + 9x_2^2
 \end{aligned}$$

42.

$$\begin{aligned}
 (7m+1)^2 &= (7m+1)(7m+1) \\
 &= (7m)(7m) + (7m)(1) + (1)(7m) + (1)(1) \\
 &= 49m^2 + 7m + 7m + 1 \\
 &= 49m^2 + 14m + 1
 \end{aligned}$$

43.

$$\begin{aligned}
 (xyz-2)^2 &= (xyz-2)(xyz-2) \\
 &= (xyz)(xyz) + (xyz)(-2) + (-2)(xyz) + (-2)(-2) \\
 &= x^2y^2z^2 - 2xyz - 2xyz + 4 \\
 &= x^2y^2z^2 - 4xyz + 4
 \end{aligned}$$

44.

$$\begin{aligned}
 (b - 6x^2)^2 &= (b - 6x^2)(b - 6x^2) \\
 &= (b)(b) + (b)(-6x^2) + (-6x^2)(b) + (-6x^2)(-6x^2) \\
 &= b^2 - 6bx^2 - 6bx^2 + 36x^4 \\
 &= b^2 - 12bx^2 + 36x^4
 \end{aligned}$$

45.

$$\begin{aligned}
 2(x + 8)^2 &= 2[(x + 8)(x + 8)] \\
 &= 2[(x)(x) + (x)(8) + (8)(x) + (8)(8)] \\
 &= 2[x^2 + 8x + 8x + 64] \\
 &= 2[x^2 + 16x + 64] \\
 &= 2x^2 + 32x + 128
 \end{aligned}$$

46.

$$\begin{aligned}
 3(3R + 4)^2 &= 3[(3R + 4)(3R + 4)] \\
 &= 3[(3R)(3R) + (3R)(4) + (4)(3R) + (4)(4)] \\
 &= 3[9R^2 + 12R + 12R + 16] \\
 &= 3[9R^2 + 24R + 16] \\
 &= 27R^2 + 72R + 48
 \end{aligned}$$

47.

$$\begin{aligned}
 (2 + x)(3 - x)(x - 1) &= [(6 - 2x + 3x - x^2)](x - 1) \\
 &= (x - 1)[-x^2 + x + 6] \\
 &= (x)(-x^2) + (x)(x) + (6)(x) + (-1)(-x^2) + (-1)(x) + (-1)(6) \\
 &= -x^3 + x^2 + 6x + x^2 - x - 6 \\
 &= -x^3 + 2x^2 + 5x - 6
 \end{aligned}$$

48.

$$\begin{aligned}
 (3x - c^2)^3 &= (3x - c^2)(3x - c^2)(3x - c^2) \\
 &= [(3x)(3x) - 3c^2x - 3c^2x + c^4](3x - c^2) \\
 &= (3x - c^2)[9x^2 - 6c^2x + c^4] \\
 &= (3x)(9x^2) + (3x)(-6c^2x) + (3x)(c^4) + (-c^2)(9x^2) + (-c^2)(-6c^2x) + (-c^2)(c^4) \\
 &= 27x^3 - 18c^2x^2 + 3c^4x - 9c^2x^2 + 6c^4x - c^6 \\
 &= -c^6 + 9c^4x - 27c^2x^2 + 27x^3
 \end{aligned}$$

49.

$$\begin{aligned}
3T(T+2)(2T-1) &= 3T[(T)(2T) + (T)(-1) + (2)(2T) + (2)(-1)] \\
&= 3T[2T^2 - T + 4T - 2] \\
&= 3T[2T^2 - T + 4T - 2] \\
&= 3T[2T^2 + 3T - 2] \\
&= 6T^3 + 9T^2 - 6T
\end{aligned}$$

50.

$$\begin{aligned}
&[(x-2)^2(x+2)]^2 \\
&= [(x-2)(x-2)(x+2)][(x-2)(x-2)(x+2)] \\
&= [(x-2)[(x)(x) + (-2)(x) + (2)(x) + (-2)(2)][(x-2)[(x)(x) + (-2)(x) + (2)(x) + (-2)(2)]] \\
&= [(x-2)[x^2 - 2x + 2x - 4]][(x-2)[x^2 - 2x + 2x - 4]] \\
&= [(x-2)[x^2 - 4]][(x-2)[x^2 - 4]] \\
&= [(x)(x^2) + (-4)(x) + (-2)(x^2) + (-2)(-4)][(x)(x^2) + (-4)(x) + (-2)(x^2) + (-2)(-4)] \\
&= [x^3 - 2x^2 - 4x + 8][x^3 - 2x^2 - 4x + 8] \\
&= (x^3)(x^3) + (x^3)(-2x^2) + (x^3)(-4x) + (x^3)(8) + (-2x^2)(x^3) + (-2x^2)(-2x^2) + (-2x^2)(-4x) + (-2x^2)(8) \\
&\quad + (-4x)(x^3) + (-4x)(-2x^2) + (-4x)(-4x) + (-4x)(8) + (8)(x^3) + (8)(-2x^2) + (8)(-4x) + (8)(8) \\
&= x^6 - 2x^5 - 4x^4 + 8x^3 - 2x^5 + 4x^4 + 8x^3 - 16x^2 - 4x^4 + 8x^3 + 16x^2 - 32x + 8x^3 - 16x^2 - 32x + 64 \\
&= x^6 - 4x^5 - 4x^4 + 32x^3 - 16x^2 - 64x + 64
\end{aligned}$$

51.**(a)**

$$\begin{aligned}
(x+y)^2 &= (3+4)^2 = 7^2 = 49 \\
x^2 + y^2 &= 3^2 + 4^2 = 9 + 16 = 25 \\
(x+y)^2 &\neq x^2 + y^2 \\
49 &\neq 25
\end{aligned}$$

(b)

$$\begin{aligned}
(x-y)^2 &= (3-4)^2 = (-1)^2 = 1 \\
x^2 - y^2 &= 3^2 - 4^2 = 9 - 16 = -7 \\
(x-y)^2 &\neq x^2 - y^2 \\
1 &\neq -7
\end{aligned}$$

52.

$$\begin{aligned}
(98)(102) &= (100-2)(100+2) \\
&= (100)(100) + (100)(2) + (-2)(100) + (2)(-2) \\
&= 10000 + 200 - 200 - 4 \\
&= 9996
\end{aligned}$$

53.

$$(4)^2 - 1 = 16 - 1 = 15 = (3)(5)$$

If we let x equal an integer between 1 and 9, $1 < x < 9$, then $x^2 - 1$ can be factored to $(x-1)(x+1)$:

$$\begin{aligned}(x-1)(x+1) &= (x)(x) + (1)(x) + (-1)(x) + (1)(-1) \\ &= x^2 - x + x - 1 \\ &= x^2 - 1\end{aligned}$$

$(x-1)$ is the number before x , and $(x+1)$ is the number after x .

54.

$$\begin{aligned}(x-2)(x+2)(x+3)(x-3) &= [x^2 + 2x - 2x - 4][x^2 + 3x - 3x - 9] \\ &= (x^2 - 4)(x^2 - 9) \\ &= (x^2)(x^2) + (x^2)(-9) + (x^2)(-4) + (-4)(-9) \\ &= x^4 - 9x^2 - 4x^2 + 36 \\ &= x^4 - 13x^2 + 36\end{aligned}$$

If we group the $(x+2)$ with the $(x-2)$, then the $2x$ and $-2x$ will cancel each other out when we multiply the terms out. Likewise with the $(x+3)$ and the $(x-3)$.

55.

$$\begin{aligned}x^3 + y^3 &\neq (x+y)^3 \\ &\neq (x+y)(x+y)(x+y) \\ &\neq (x+y)[(x)(x) + (x)(y) + (y)(x) + (y)(y)] \\ &\neq (x+y)[x^2 + xy + xy + y^2] \\ &\neq (x+y)[x^2 + 2xy + y^2] \\ &\neq (x)(x^2) + (x)(2xy) + (x)(y^2) + (y)(x^2) + (y)(2xy) + (y)(y^2) \\ &\neq x^3 + 2x^2y + y^2x + x^2y + 2y^2x + y^3 \\ &\neq x^3 + 3x^2y + 3y^2x + y^3\end{aligned}$$

56.

$$\begin{aligned}(x+y)(x^2 - xy + y^2) \\ &= (x)(x^2) + (x)(-xy) + (x)(y^2) + (y)(x^2) + (y)(-xy) + (y)(y^2) \\ &= x^3 - x^2y + y^2x + x^2y - y^2x + y^3 \\ &= x^3 + y^3\end{aligned}$$

57.

$$\begin{aligned}P(1+0.01r)^2 &= P(1+0.01r)(1+0.01r) \\ &= P[(1)(1) + (1)(0.01r) + (0.01r)(1) + (0.01r)(0.01r)] \\ &= P[1 + 0.01r + 0.01r + 0.0001r^2] \\ &= 0.0001r^2P + 0.02rP + P\end{aligned}$$

58.

$$\begin{aligned} w(1-x)(4-x^2) &= w[(1)(4) + (1)(-x^2) + (-x)(4) + (-x)(-x^2)] \\ &= w[4 - x^2 - 4x + x^3] \\ &= x^3w - x^2w - 4wx + 4w \end{aligned}$$

59.

$$\begin{aligned} (2R - X)^2 - (R^2 + X^2) &= (2R - X)(2R - X) - (R^2 + X^2) \\ &= [(2R)(2R) + (2R)(-X) + (2R)(-X) + (-X)(-X)] - (R^2 + X^2) \\ &= 4R^2 - 2RX - 2RX + X^2 - R^2 - X^2 \\ &= 3R^2 - 4RX \end{aligned}$$

60.

$$\begin{aligned} (2T^3 + 3)(T^2 - T - 3) &= (2T^3)(T^2) + (2T^3)(-T) + (2T^3)(-3) + (3)(T^2) + (3)(-T) + (3)(-3) \\ &= 2T^5 - 2T^4 - 6T^3 + 3T^2 - 3T - 9 \end{aligned}$$

61.

$$\begin{aligned} \text{Number of switches} &= n^2 \\ &= (n+100)^2 \\ &= (n+100)(n+100) \\ &= (n)(n) + (n)(100) + (100)(n) + (100)(100) \\ &= n^2 + 100n + 100n + 10\,000 \\ &= n^2 + 200n + 10\,000 \end{aligned}$$

62.

$$\begin{aligned} (T^2 - 100)(T - 10)(T + 10) &= (T^2 - 100)[T^2 + 10T - 10T - 100] \\ &= (T^2 - 100)[T^2 - 100] \\ &= T^4 - 100T^2 - 100T^2 + 10\,000 \\ &= T^4 - 200T^2 + 10\,000 \end{aligned}$$

63.

$$\begin{aligned} (R_1 + R_2)^2 - 2R_2(R_1 + R_2) &= [(R_1 + R_2)(R_1 + R_2)] - 2R_2(R_1 + R_2) \\ &= [(R_1)(R_1) + (R_1)(R_2) + (R_2)(R_1) + (R_2)(R_2)] - 2R_1R_2 - 2R_2^2 \\ &= [R_1^2 + R_1R_2 + R_1R_2 + R_2^2] - 2R_1R_2 - 2R_2^2 \\ &= R_1^2 - R_2^2 \end{aligned}$$

64.

$$\begin{aligned} & 27x^2 - 24(x-6)^2 - (x-12)^3 \\ &= 27x^2 - 24(x-6)(x-6) - (x-12)(x-12)(x-12) \\ &= 27x^2 - 24[x^2 - 6x - 6x + 36] - (x-12)[x^2 - 12x - 12x + 144] \\ &= 27x^2 - 24[x^2 - 12x + 36] - (x-12)[x^2 - 24x + 144] \\ &= 27x^2 - 24x^2 + 288x - 864 - [(x)(x^2) + (x)(-24x) + (x)(144) + (-12)(x^2) + (-12)(-24x) + (-12)(144)] \\ &= 3x^2 + 288x - 864 - x^3 + 24x^2 - 144x + 12x^2 - 288x + 1728 \\ &= -x^3 + 39x^2 - 144x + 864 \end{aligned}$$

1.9 Division of Algebraic Expressions

1.

$$\frac{-6a^2xy^2}{-2a^2xy^5} = \left(\frac{-6}{-2}\right) \frac{a^{2-2}x^{1-1}}{y^{5-2}} = \frac{3}{y^3}$$

2.

$$\begin{aligned} \frac{4x^3y - 8x^3y^2 + 2x^2y}{2xy^2} &= \frac{4x^3y}{2xy^2} - \frac{8x^3y^2}{2xy^2} + \frac{2x^2y}{2xy^2} \\ &= \frac{2x^{3-1}}{y^{2-1}} - 4x^{3-1}y^{2-2} + \frac{x^{2-1}}{y^{2-1}} \\ &= \frac{2x^2}{y} - 4x^2 + \frac{x}{y} \end{aligned}$$

3.

$$\begin{array}{r} 3x-2 \\ 2x-1 \overline{)6x^2-7x+2} \\ \underline{6x^2-3x} \\ -4x+2 \\ \underline{-4x+2} \\ 0 \end{array}$$

4.

$$\begin{array}{r} 2x-1 \\ 4x^2-1 \overline{)8x^3-4x^2+0x+3} \\ \underline{8x^3-2x} \\ -4x^2+2x+3 \\ \underline{-4x^2+2x+1} \\ 2x+2 \end{array}$$

$$\frac{8x^3-4x^2+3}{4x^2-1} = 2x-1 + \frac{2x+2}{4x^2-1}$$

5.

$$\frac{8x^3y^2}{-2xy} = -4x^{3-1}y^{2-1} = -4x^2y$$

6.

$$\frac{-18b^7c^3}{bc^2} = -18b^{7-1}c^{3-2} = -18b^6c$$

7.

$$\frac{-16r^3t^5}{-4r^5t} = \frac{4t^{5-1}}{r^{5-3}} = \frac{4t^4}{r^2}$$

8.

$$\frac{51mn^5}{17m^2n^2} = \frac{3n^{5-2}}{m^{2-1}} = \frac{3n^3}{m}$$

9.

$$\frac{(15x^2)(4bx)(2y)}{30bxy} = \frac{120x^3by}{30bxy} = 4x^{3-1}b^{1-1}y^{1-1} = 4x^2$$

10.

$$\frac{(5sT)(8s^2T^3)}{10s^3T^2} = \frac{40s^3T^4}{10s^3T^2} = 4s^{3-3}T^{4-2} = 4T^2$$

11.

$$\frac{6(ax)^2}{-ax^2} = \frac{6a^2x^2}{-ax^2} = -6a^{2-1}x^{2-2} = -6a$$

12.

$$\frac{12a^2b}{(3ab^2)^2} = \frac{12a^2b}{9a^2b^4} = \frac{4a^{2-2}}{3b^{4-1}} = \frac{4}{3b^3}$$

13.

$$\frac{3a^2x + 6xy}{3x} = \frac{3a^2x}{3x} + \frac{6xy}{3x} = \frac{3a^2x^{1-1}}{3} + \frac{6x^{1-1}y}{3} = a^2 + 2y$$

14.

$$\frac{2m^2n - 6mn}{2m} = \frac{2m^2n}{2m} - \frac{6mn}{2m} = m^{2-1}n - 3m^{1-1}n = mn - 3n$$

15.

$$\frac{3rst - 6r^2st^2}{3rs} = \frac{3rst}{3rs} - \frac{6r^2st^2}{3rs} = r^{1-1}s^{1-1}t - 2r^{2-1}s^{1-1}t^2 = -2rt^2 + t$$

16.

$$\frac{-5a^2n - 10an^2}{5an} = \frac{-5a^2n}{5an} - \frac{10an^2}{5an} = -a^{2-1}n^{1-1} - 2a^{1-1}n^{2-1} = -a - 2n$$

17.

$$\begin{aligned} \frac{4pq^3 + 8p^2q^2 - 16pq^5}{4pq^2} &= \frac{4pq^3}{4pq^2} + \frac{8p^2q^2}{4pq^2} - \frac{16pq^5}{4pq^2} \\ &= p^{1-1}q^{3-2} + 2p^{2-1}q^{2-2} - 4p^{1-1}q^{5-2} \\ &= -4q^3 + 2p + q \end{aligned}$$

18.

$$\begin{aligned}\frac{a^2x_1x_2^2 + ax_1^3 - ax_1}{ax_1} &= \frac{a^2x_1x_2^2}{ax_1} + \frac{ax_1^3}{ax_1} - \frac{ax_1}{ax_1} \\ &= a^{2-1}x_1^{1-1}x_2^2 + a^{1-1}x_1^{3-1} - a^{1-1}x_1^{1-1} \\ &= ax_2^2 + x_1^2 - 1\end{aligned}$$

19.

$$\begin{aligned}\frac{2\pi fL - \pi fR^2}{\pi fR} &= \frac{2\pi fL}{\pi fR} - \frac{\pi fR^2}{\pi fR} \\ &= \frac{2f^{1-1}L}{R} - f^{1-1}R^{2-1} \\ &= \frac{2L}{R} - R\end{aligned}$$

20.

$$\begin{aligned}\frac{9(aB)^4 - 6aB^4}{3aB^3} &= \frac{9(aB)^4}{3aB^3} - \frac{6aB^4}{3aB^3} \\ &= \frac{9a^4B^4}{3aB^3} - \frac{6aB^4}{3aB^3} \\ &= 3a^{4-1}B^{4-3} - 2a^{1-1}B^{4-3} \\ &= 3a^3B - 2B\end{aligned}$$

21.

$$\begin{aligned}\frac{3ab^2 - 6ab^3 + 9a^2b^2}{9a^2b^2} &= \frac{3ab^2}{9a^2b^2} - \frac{6ab^3}{9a^2b^2} + \frac{9a^2b^2}{9a^2b^2} \\ &= \frac{b^{2-2}}{3a^{2-1}} - \frac{2b^{3-2}}{3a^{2-1}} + a^{2-2}b^{2-2} \\ &= \frac{1}{3a} - \frac{2b}{3a} + 1\end{aligned}$$

22.

$$\begin{aligned}\frac{2x^{n+2} + 4ax^n}{2x^n} &= \frac{2x^{n+2}}{2x^n} + \frac{4ax^n}{2x^n} \\ &= x^{n-n+2} + 2ax^{n-n} \\ &= x^2 + 2a\end{aligned}$$

23.

$$\begin{aligned}\frac{6y^{2n} - 4ay^{n+1}}{2y^n} &= \frac{6y^{2n}}{2y^n} - \frac{4ay^{n+1}}{2y^n} \\ &= 3y^{2n-n} - 2ay^{n-n+1} \\ &= 3y^n - 2ay\end{aligned}$$

24.

$$\begin{aligned}\frac{3a(F+T)b^2 - (F+T)}{a(F+T)} &= \frac{3a(F+T)b^2}{a(F+T)} - \frac{(F+T)}{a(F+T)} \\ &= \frac{3a^{1-1} \cancel{(F+T)} b^2}{\cancel{(F+T)}} - \frac{\cancel{(F+T)}}{a \cancel{(F+T)}} \\ &= 3b^2 - \frac{1}{a}\end{aligned}$$

25.

$$\begin{array}{r} \overline{2x+1} \\ x+3 \overline{) 2x^2 + 7x + 3} \\ \underline{2x^2 + 6x} \\ x + 3 \\ \underline{x+3} \\ 0 \end{array}$$

$$\frac{2x^2 + 7x + 3}{x+3} = 2x+1$$

26.

$$\begin{array}{r} \overline{3t-4} \\ t-1 \overline{) 3t^2 - 7t + 4} \\ \underline{3t^2 - 3t} \\ -4t + 4 \\ \underline{-4t + 4} \\ 0 \end{array}$$

$$\frac{3t^2 - 7t + 4}{t-1} = 3t-4$$

27.

$$\begin{array}{r} \overline{x-1} \\ x-2 \overline{) x^2 - 3x + 2} \\ \underline{x^2 - 2x} \\ -x + 2 \\ \underline{-x + 2} \\ 0 \end{array}$$

$$\frac{x^2 - 3x + 2}{x-2} = x-1$$

28.

$$\begin{array}{r}
 \overline{) 2x^2 - 5x - 7} \\
 \underline{2x^2 + 2x} \\
 - 7x - 7 \\
 \underline{-7x - 7} \\
 0
 \end{array}$$

$$\frac{2x^2 - 5x - 7}{x + 1} = 2x - 7$$

29.

$$\begin{array}{r}
 \overline{) 8x^3 - 14x^2 + x + 0} \\
 \underline{8x^3 - 12x^2} \\
 - 2x^2 + x \\
 \underline{-2x^2 + 3x} \\
 - 2x + 0 \\
 \underline{-2x + 3} \\
 - 3
 \end{array}$$

$$\frac{8x^3 - 14x^2 + x}{2x - 3} = 4x^2 - x - 1 - \frac{3}{2x - 3}$$

30.

$$\begin{array}{r}
 \overline{) 6y^2 + 7y + 6} \\
 \underline{6y^2 + 3y} \\
 4y + 6 \\
 \underline{4y + 2} \\
 4
 \end{array}$$

$$\frac{6y^2 + 7y + 6}{2y + 1} = 3y + 2 + \frac{4}{2y + 1}$$

31.

$$\begin{array}{r}
 \overline{) 4Z^2 - 5Z - 7} \\
 \underline{4Z^2 + 3Z} \\
 - 8Z - 7 \\
 \underline{-8Z - 6} \\
 - 1
 \end{array}$$

$$\frac{4Z^2 - 5Z - 7}{4Z + 3} = Z - 2 - \frac{1}{4Z + 3}$$

32.

$$\begin{array}{r}
 \overline{) 6x^2 - 5x - 9} \\
 \underline{6x^2 - 8x} \\
 3x - 9 \\
 \underline{3x - 4} \\
 -5
 \end{array}$$

$$\frac{6x^2 - 5x - 9}{3x - 4} = 2x + 1 - \frac{5}{3x - 4}$$

33.

$$\begin{array}{r}
 \overline{) x^3 + 3x^2 - 4x - 12} \\
 \underline{x^3 + 2x^2} \\
 x^2 - 4x \\
 \underline{x^2 + 2x} \\
 -6x - 12 \\
 \underline{-6x - 12} \\
 0
 \end{array}$$

$$\frac{x^3 + 3x^2 - 4x - 12}{x + 2} = x^2 + x - 6$$

34.

$$\begin{array}{r}
 \overline{) 3x^3 + 19x^2 + 13x - 20} \\
 \underline{3x^3 - 2x^2} \\
 21x^2 + 13x \\
 \underline{21x^2 - 14x} \\
 27x - 20 \\
 \underline{27x - 18} \\
 -2
 \end{array}$$

$$\frac{3x^3 + 19x^2 + 13x - 20}{3x - 2} = x^2 + 7x + 9 - \frac{2}{3x - 2}$$

35.

$$\begin{array}{r}
 \overline{2a^4 + 0a^3 + 4a^2 + 0a - 16} \\
 \underline{2a^4 - 4a^2} \\
 8a^2 - 16 \\
 \underline{8a^2 - 16} \\
 0
 \end{array}$$

$$\frac{2a^4 + 4a^2 - 16}{a^2 - 2} = 2a^2 + 8$$

36.

$$\begin{array}{r}
 \overline{6T^3 + T^2 + 0T + 2} \\
 \underline{6T^3 - 2T^2 + 4T} \\
 3T^2 - 4T + 2 \\
 \underline{3T^2 - T + 2} \\
 - 3T
 \end{array}$$

$$\frac{6T^3 + T^2 + 2}{3T^2 - T + 2} = 2T + 1 - \frac{3T}{3T^2 - T + 2}$$

37.

$$\begin{array}{r}
 \overline{x^3 + 0x^2 + 0x + 8} \\
 \underline{x^3 + 2x^2} \\
 - 2x^2 + 0x \\
 \underline{-2x^2 - 4x} \\
 4x + 8 \\
 \underline{4x + 8} \\
 0
 \end{array}$$

$$\frac{x^3 + 8}{x + 2} = x^2 - 2x + 4$$

38.

$$\begin{array}{r}
 D^2 + D + 1 \\
 D - 1 \overline{) D^3 + 0D^2 + 0D - 1} \\
 \underline{D^3 - 1D^2} \\
 D^2 + 0D \\
 \underline{D^2 - 1D} \\
 D - 1 \\
 \underline{D - 1} \\
 0
 \end{array}$$

$$\frac{D^3 - 1}{D - 1} = D^2 + D + 1$$

39.

$$\begin{array}{r}
 x - y \\
 x - y \overline{) x^2 - 2xy + y^2} \\
 \underline{x^2 - xy} \\
 -xy + y^2 \\
 \underline{-xy + y^2} \\
 0
 \end{array}$$

$$\frac{x^2 - 2xy + y^2}{x - y} = x - y$$

40.

$$\begin{array}{r}
 3r + 4R \\
 r - 3R \overline{) 3r^2 - 5rR + 2R^2} \\
 \underline{3r^2 - 9rR} \\
 4rR + 2R^2 \\
 \underline{4rR - 12R^2} \\
 14R^2
 \end{array}$$

$$\frac{3r^2 - 5rR + 2R^2}{r - 3R} = 3r + 4R + \frac{14R^2}{r - 3R}$$

41.

$$\begin{array}{r}
 \overline{x-y+z} \\
 x+y-z \overline{)x^2 - y^2 + 0xy + 0xz + 2yz - z^2} \\
 \underline{x^2 + xy - xz} \\
 - y^2 - xy + xz + 2yz - z^2 \\
 \underline{ - y^2 - xy + yz} \\
 xz + yz - z^2 \\
 \underline{ xz + yz - z^2} \\
 0
 \end{array}$$

$$\frac{x^2 - y^2 + 2yz - z^2}{x + y - z} = x - y + z$$

42.

$$\begin{array}{r}
 \overline{a^2+2ab+2b^2} \\
 a^2-2ab+2b^2 \overline{)a^4+0a^3b+0a^2b^2+0ab^3+b^4} \\
 \underline{a^4-2a^3b+2a^2b^2} \\
 2a^3b-2a^2b^2+0ab^3 \\
 \underline{ 2a^3b-4a^2b^2+4ab^3} \\
 2a^2b^2-4ab^3+b^4 \\
 \underline{ 2a^2b^2-4ab^3+4b^4} \\
 -3b^4 \\
 \frac{a^4+b^4}{a^2-2ab+2b^2} = a^2+2ab+2b^2 - \frac{3b^4}{a^2-2ab+2b^2}
 \end{array}$$

43.

We know that $2x+1$ multiplied by $x+c$ will give us $2x^2-9x-5$, so $2x^2-9x-5$ divided by $2x+1$ will give us $x+c$:

$$\begin{array}{r}
 \overline{x-5} \\
 2x+1 \overline{)2x^2-9x-5} \\
 \underline{2x^2+x} \\
 -10x-5 \\
 \underline{ -10x-5} \\
 0
 \end{array}$$

$$\begin{aligned}
 x+c &= x-5 \\
 c &= -5
 \end{aligned}$$

44.

$$\begin{array}{r}
 2x-3 \\
 3x+4 \overline{)6x^2 - x + k} \\
 \underline{6x^2 + 8x} \\
 -9x + k \\
 \underline{-9x - 12} \\
 0
 \end{array}$$

$$k - (-12) = 0$$

$$k + 12 = 0$$

$$k = -12$$

45.

$$\begin{array}{r}
 x^3 - x^2 + x - 1 \\
 x+1 \overline{)x^4 + 0x^3 + 0x^2 + 0x + 1} \\
 \underline{x^4 + x^3} \\
 -x^3 + 0x^2 \\
 \underline{-x^3 - x^2} \\
 x^2 + 0x \\
 \underline{x^2 + x} \\
 -x + 1 \\
 \underline{-x - 1} \\
 2
 \end{array}$$

$$\frac{x^4 + 1}{x + 1} = x^3 - x^2 + x - 1 + \frac{2}{x + 1} \neq x^3$$

46.

$$\begin{array}{r}
 x^2 - xy + y^2 \\
 x + y \overline{)x^3 + 0x^2y + 0y^2x + 0x + y^3} \\
 \underline{x^3 + x^2y} \\
 -x^2y + 0y^2x \\
 \underline{-x^2y - y^2x} \\
 y^2x + y^3 \\
 \underline{y^2x + y^3} \\
 0
 \end{array}$$

$$\frac{x^3 + y^3}{x + y} = x^2 - xy + y^2 \neq x^2 + y^2$$

47.

$$\begin{aligned}\frac{8A^5 + 4A^3\mu^2E^2 - A\mu^4E^4}{8A^4} &= \frac{8A^5}{8A^4} + \frac{4A^3\mu^2E^2}{8A^4} - \frac{A\mu^4E^4}{8A^4} \\ &= A^{5-4} + \frac{\mu^2E^2}{2A^{4-3}} - \frac{\mu^4E^4}{8A^{4-1}} \\ &= A + \frac{\mu^2E^2}{2A} - \frac{\mu^4E^4}{8A^3}\end{aligned}$$

48.

$$\begin{aligned}\frac{6R_1 + 6R_2 + R_1R_2}{6R_1R_2} &= \frac{6R_1}{6R_1R_2} + \frac{6R_2}{6R_1R_2} + \frac{R_1R_2}{6R_1R_2} \\ &= \frac{\cancel{R_1}}{\cancel{R_1}R_2} + \frac{\cancel{R_2}}{R_1\cancel{R_2}} + \frac{\cancel{R_1}\cancel{R_2}}{6\cancel{R_1}\cancel{R_2}} \\ &= \frac{1}{R_2} + \frac{1}{R_1} + \frac{1}{6}\end{aligned}$$

49.

$$\begin{aligned}\frac{GMm[(R+r)-(R-r)]}{2rR} &= \frac{GMm[R+r-R+r]}{2rR} \\ &= \frac{GMm[2r]}{2rR} \\ &= \frac{GMm\cancel{[2r]}}{\cancel{2r}R} \\ &= \frac{GMm}{R}\end{aligned}$$

50.

$$\begin{array}{r} 3T^2 - 2T - 4 \\ T - 2 \overline{) 3T^3 - 8T^2 + 0T + 8} \\ \underline{3T^3 - 6T^2} \\ -2T^2 + 0T \\ \underline{-2T^2 + 4T} \\ -4T + 8 \\ \underline{-4T + 8} \\ 0 \end{array}$$

51.

$$\left(\frac{s^2 - 2s - 2}{s^4 + 4}\right)^{-1} = \frac{s^4 + 4}{s^2 - 2s - 2}$$

$$\begin{array}{r}
 \overline{s^2 + 2s + 6} \\
s^2 - 2s - 2 \overline{)s^4 + 0s^3 + 0s^2 + 0s + 4} \\
\underline{2s^3 + 2s^2 + 0s} \\
2s^3 - 4s^2 - 4s \\
\underline{6s^2 + 4s + 4} \\
6s^2 - 12s - 12 \\
\underline{16s + 16}
\end{array}$$

$$\frac{s^4 + 4}{s^2 - 2s - 2} = s^2 + 2s + 6 + \frac{16s + 16}{s^2 - 2s - 2}$$

52.

$$\begin{array}{r}
 \overline{t^2 - 3t + 5} \\
2t + 100 \overline{)2t^3 + 94t^2 - 290t + 500} \\
\underline{2t^3 + 100t^2} \\
-6t^2 - 290t \\
\underline{-6t^2 - 300t} \\
10t + 500 \\
\underline{10t + 500} \\
0
\end{array}$$

1.10 Solving Equations

1.

(a)

$$x - 3 = -12$$

$$x - 3 + 3 = -12 + 3$$

$$x = -9$$

(b)

$$x + 3 = -12$$

$$x + 3 - 3 = -12 - 3$$

$$x = -15$$

(c)

$$\frac{x}{3} = -12$$

$$3\left(\frac{x}{3}\right) = 3(-12)$$

$$x = -36$$

(d)

$$3x = -12$$

$$\frac{3x}{3} = \frac{-12}{3}$$

$$x = -4$$

2.

$$7 - 2t = 9$$

$$7 - 7 - 2t = 9 - 7$$

$$-2t = 2$$

$$\frac{-2t}{-2} = \frac{2}{-2}$$

$$t = -1$$

Check:

$$7 - 2t = 9$$

$$7 - 2(-1) = 9$$

$$7 - (-2) = 9$$

$$9 = 9$$

3.

$$x - 7 = 3x - (8 - 6x)$$

$$x - 7 = 3x - 8 + 6x$$

$$x - 7 = 9x - 8$$

$$-8x = -1$$

$$x = \frac{1}{8}$$

4.

$$\frac{1.52}{60.0} = \frac{I}{48.0}$$

$$I = 48.0 \left(\frac{1.52}{60.0} \right)$$

$$I = 1.216 \text{ A}$$

$$I = 1.22 \text{ A}$$

5.

$$x - 2 = 7$$

$$x = 7 + 2$$

$$x = 9$$

6.

$$x - 4 = -1$$

$$x = -1 + 4$$

$$x = 3$$

7.

$$x + 5 = 4$$

$$x = 4 - 5$$

$$x = -1$$

8.

$$s + 6 = -3$$

$$s = -3 - 6$$

$$s = -9$$

9.

$$\frac{t}{2} = -5$$

$$t = 2(-5)$$

$$t = -10$$

10.

$$\frac{x}{-4} = 2$$

$$x = -4(2)$$

$$x = -8$$

11.

$$4E = -20$$

$$E = \frac{-20}{4}$$

$$E = -5$$

12.

$$2x = 12$$

$$x = \frac{12}{2}$$

$$x = 6$$

13.

$$3t + 5 = -4$$

$$3t = -4 - 5$$

$$t = \frac{-9}{3}$$

$$t = -3$$

14.

$$5D - 2 = 13$$

$$5D = 13 + 2$$

$$D = \frac{15}{5}$$

$$D = 3$$

15.

$$5 - 2y = -3$$

$$-2y = -3 - 5$$

$$y = \frac{-8}{-2}$$

$$y = 4$$

16.

$$8 - 5t = 18$$

$$-5t = 18 - 8$$

$$t = \frac{10}{-5}$$

$$t = -2$$

17.

$$3x + 7 = x$$

$$x - 3x = 7$$

$$-2x = 7$$

$$x = -\frac{7}{2}$$

18.

$$6 + 4L = 5 - 3L$$

$$4L + 3L = 5 - 6$$

$$7L = -1$$

$$L = -\frac{1}{7}$$

19.

$$2(s - 4) = s$$

$$s = 2s - 8$$

$$s - 2s = -8$$

$$-s = -8$$

$$s = 8$$

20.

$$3(4 - n) = -n$$

$$-n = 12 - 3n$$

$$-n + 3n = 12$$

$$2n = 12$$

$$n = \frac{12}{2}$$

$$n = 6$$

21.

$$6 - (r - 4) = 2r$$

$$2r = 6 - r + 4$$

$$2r + r = 10$$

$$3r = 10$$

$$r = \frac{10}{3}$$

22.

$$5 - (x + 2) = 5x$$

$$5x = 5 - x - 2$$

$$5x + x = 3$$

$$6x = 3$$

$$x = \frac{3}{6} = \frac{1}{2}$$

23.

$$2(x-3) = -x$$

$$-x = 2x - 6$$

$$-x - 2x = -6$$

$$-3x = -6$$

$$x = \frac{-6}{-3}$$

$$x = 2$$

24.

$$4(7 - F) = -7$$

$$28 - 4F = -7$$

$$-4F = -7 - 28$$

$$F = \frac{-35}{-4} = \frac{35}{4}$$

25.

$$0.1x - 0.5(x - 2) = 2$$

$$x - 5(x - 2) = 2(10)$$

$$x - 5x + 10 = 20$$

$$-4x = 20 - 10$$

$$x = \frac{10}{-4} = -\frac{5}{2}$$

26.

$$1.5x - 0.3(x - 4) = 6$$

$$15x - 3(x - 4) = 6(10)$$

$$15x - 3x + 12 = 60$$

$$12x = 60 - 12$$

$$x = \frac{48}{12}$$

$$x = 4$$

27.

$$7 - 3(1 - 2p) = 4 + 2p$$

$$7 - 3 + 6p = 4 + 2p$$

$$4 + 6p - 2p = 4$$

$$4p = 4 - 4$$

$$p = \frac{0}{4}$$

$$p = 0$$

28.

$$3 - 6(2 - 3t) = t - 5$$

$$3 - 12 + 18t = t - 5$$

$$-9 + 18t - t = -5$$

$$17t = 4$$

$$t = \frac{4}{17}$$

29.

$$\frac{4x - 2(x - 4)}{3} = 8$$

$$4x - 2x + 8 = 3(8)$$

$$2x = 24 - 8$$

$$x = \frac{16}{2}$$

$$x = 8$$

30.

$$2x = \frac{3 - 5(7 - 3x)}{4}$$

$$4(2x) = 3 - 35 + 15x$$

$$8x - 15x = -32$$

$$-7x = -32$$

$$x = \frac{-32}{-7} = \frac{32}{7}$$

31.

$$|x| - 1 = 8$$

$$|x| = 8 + 1$$

$$x = 9 \text{ or } x = -9$$

32.

$$2 - |x| = 4$$

$$-|x| = 4 - 2$$

$$|x| = \frac{2}{-1}$$

$$|x| = -2$$

There is no real solution for x

33.

$$5.8 - 0.3(x - 6.0) = 0.5x$$

$$0.5x = 5.8 - 0.3x + 1.8$$

$$0.5x + 0.3x = 7.6$$

$$0.8x = 7.6$$

$$x = \frac{7.6}{0.8}$$

$$x = 9.5$$

34.

$$1.9t = 0.5(4.0 - t) - 0.8$$

$$1.9t = 2.0 - 0.5t - 0.8$$

$$1.9t + 0.5t = 1.2$$

$$2.4t = 1.2$$

$$t = \frac{1.2}{2.4}$$

$$t = 0.50$$

35.

$$-0.24(C - 0.50) = 0.63$$

$$-0.24C + 0.12 = 0.63$$

$$-0.24C = 0.63 - 0.12$$

$$-0.24C = 0.51$$

$$C = \frac{0.51}{-0.24}$$

$$C = -2.125$$

$$C = -2.1$$

36.

$$27.5(5.17 - 1.44x) = 73.4$$

$$142.175 - 39.6x = 73.4$$

$$-39.6x = 73.4 - 142.175$$

$$-39.6x = -68.775$$

$$x = \frac{-68.775}{-39.6}$$

$$x = 1.736742424$$

$$x = 1.74$$

37.

$$\frac{x}{2.0} = \frac{17}{6.0}$$

$$x = 2.0 \left(\frac{17}{6.0} \right)$$

$$x = 5.66666666\dots$$

$$x = 5.7$$

38.

$$\frac{3.0}{7.0} = \frac{R}{42}$$

$$R = 42 \left(\frac{3.0}{7.0} \right)$$

$$R = 18$$

39.

$$\frac{165}{223} = \frac{13V}{15}$$

$$\frac{15}{13} \left(\frac{165}{223} \right) = \frac{15}{13} \left(\frac{13V}{15} \right)$$

$$V = \frac{2475}{2899}$$

$$V = 0.85374267$$

$$V = 0.85$$

40.

$$\frac{276x}{17.0} = \frac{1360}{46.4}$$

$$276x = 17 \left(\frac{1360}{46.4} \right)$$

$$x = \frac{498.2758621}{276}$$

$$x = 1.805347326$$

$$x = 1.81$$

41.**(a)**

$$2x + 3 = 3 + 2x$$

$$2x + 3 = 2x + 3$$

Is an identity, since it is true for all values of x .

(b)

$$2x - 3 = 3 - 2x$$

$$4x = 6$$

$$x = \frac{6}{4} = \frac{3}{2}$$

Is conditional as x has one answer only.

42.

$$2x + a = 2x$$

$$2x - 2x + a = 2x - 2x$$

$$a = 0$$

Since a only has one value, this equation is conditional on a being 0.

Check:

$$2x + a = 2x$$

$$2x + 0 = 2x$$

$$2x = 2x$$

43.

$$x - 7 = 3x - (6x - 8)$$

$$0 = 3x - 6x + 8 - x + 7$$

$$0 = -4x + 15$$

$$x = 3.75$$

44.

$$0.0595 - 0.525i - 8.85(i + 0.0316) = 0$$

$$0.595 - 0.525i - 8.85i - 0.27966 = 0$$

$$-9.375i + 0.31534 = 0$$

$$i = 0.033636266$$

$$i = 0.0336$$

45.

$$2.0v + 40 = 2.5(v + 5.0)$$

$$2.0v + 40 = 2.5v + 12.5$$

$$40 - 12.5 = 2.5v - 2.0v$$

$$27.5 = 0.5v$$

$$v = \frac{27.5}{0.5}$$

$$v = 55 \text{ km/h}$$

46.

$$15(5.5 + v) = 24(5.5 - v)$$

$$82.5 + 15v = 132 - 24v$$

$$15v + 24v = 132 - 82.5$$

$$39v = 49.5$$

$$v = \frac{49.5}{39}$$

$$v = 1.269230769 \text{ km/h}$$

$$v = 1.3 \text{ km/h}$$

47.

$$1.1 = \frac{(T - 76)}{40}$$

$$40(1.1) = T - 76$$

$$44 = T - 76$$

$$T = 44 + 76$$

$$T = 120 \text{ }^\circ\text{C}$$

48.

$$1.12V - 0.67(10.5 - V) = 0$$

$$1.12V - 7.035 + 0.67V = 0$$

$$1.79V - 7.035 = 0$$

$$1.79V = 7.035$$

$$V = \frac{7.035}{1.79}$$

$$V = 3.930167598 \text{ V}$$

$$V = 3.9 \text{ V}$$

49.

$$0.14n + 0.06(2000 - n) = 0.09(2000)$$

$$0.14n + 120 - 0.06n = 180$$

$$0.14n - 0.06n = 180 - 120$$

$$0.08n = 60$$

$$n = \frac{60}{0.08}$$

$$n = 750 \text{ L}$$

50.

$$215(3x) = 55.3x + 38.5(8.25 - 3x)$$

$$645x = 55.3x + 317.625 - 115.5x$$

$$645x - 55.3x + 115.5x = 317.625$$

$$705.2x = 317.625$$

$$x = \frac{317.625}{705.2}$$

$$x = 0.45040414 \text{ m}$$

$$x = 0.450 \text{ m}$$

51.

$$\frac{2050 \text{ km}}{55 \text{ L}} = \frac{x}{22 \text{ L}}$$

$$x = 22 \text{ L} \left(\frac{2050 \text{ km}}{55 \text{ L}} \right)$$

$$x = 820 \text{ km}$$

52.

$$\frac{1.8 \text{ m}}{20 \text{ mm}} = \frac{x}{16 \text{ mm}}$$

$$x = 16 \text{ mm} \left(\frac{1.8 \text{ m}}{20 \text{ mm}} \right)$$

$$x = 1.44 \text{ mm}$$

$$x = 1.4 \text{ mm}$$

1.11 Formulas and Literal Equations

1.

$$v = v_0 + at$$

$$v - v_0 = at$$

$$a = \frac{v - v_0}{t}$$

2.

$$W = \frac{L(wL + 2P)}{8}$$

$$8W = L(wL + 2P)$$

$$8W = wL^2 + 2LP$$

$$wL^2 = 8W - 2LP$$

$$w = \frac{8W - 2LP}{L^2}$$

3.

$$V = V_0[1 + b(T - T_0)]$$

$$V = V_0[1 + bT - bT_0]$$

$$V = V_0 + bTV_0 - bT_0V_0$$

$$bT_0V_0 = V_0 + bTV_0 - V$$

$$T_0 = \frac{V_0 + bTV_0 - V}{bV_0}$$

4.

$$R = R_0 + R_0\alpha T$$

$$R - R_0 = R_0\alpha T$$

$$\alpha = \frac{R - R_0}{R_0T}$$

5.

$$E = IR$$

$$R = \frac{E}{I}$$

6.

$$pV = nRT$$

$$T = \frac{pV}{nR}$$

7.

$$rL = g_2 - g_1$$

$$g_1 + rL = g_2$$

$$g_1 = g_2 - rL$$

8.

$$W = S_d T - Q$$

$$Q + W = S_d T$$

$$Q = S_d T - W$$

9.

$$Q = SLd^2$$

$$L = \frac{Q}{Sd^2}$$

10.

$$P = 2\pi T f$$

$$T = \frac{P}{2\pi f}$$

11.

$$p = p_a + dgh$$

$$p - p_a = dgh$$

$$h = \frac{p - p_a}{dg}$$

12.

$$2Q = 2I + A + S$$

$$2I = 2Q - A - S$$

$$I = \frac{2Q - A - S}{2}$$

13.

$$A = \frac{Rt}{PV}$$

$$Rt = APV$$

$$t = \frac{APV}{R}$$

14.

$$u = -\frac{eL}{2m}$$

$$eL = -2mu$$

$$L = -\frac{2mu}{e}$$

15.

$$ct^2 = 0.3t - ac$$

$$ac + ct^2 = 0.3t$$

$$ac = 0.3t - ct^2$$

$$a = \frac{-ct^2 + 0.3t}{c}$$

16.

$$2p + dv^2 = 2d(C - W)$$

$$2p + dv^2 = 2Cd - 2dW$$

$$2Cd = dv^2 + 2p + 2dW$$

$$C = \frac{dv^2 + 2dW + 2p}{2d}$$

17.

$$T = \frac{c + d}{v}$$

$$c + d = Tv$$

$$d = Tv - c$$

18.

$$L = \frac{N\Phi}{i}$$

$$N\Phi = iL$$

$$\Phi = \frac{iL}{N}$$

19.

$$\frac{K_1}{K_2} = \frac{m_1 + m_2}{m_1}$$

$$K_2(m_1 + m_2) = K_1m_1$$

$$K_2m_1 + K_2m_2 = K_1m_1$$

$$K_2m_2 = K_1m_1 - K_2m_1$$

$$m_2 = \frac{K_1m_1 - K_2m_1}{K_2}$$

20.

$$f = \frac{F}{d - F}$$

$$f(d - F) = F$$

$$fd - fF = F$$

$$fd = F + fF$$

$$d = \frac{F + fF}{f}$$

21.

$$a = \frac{2mg}{M + 2m}$$

$$a(M + 2m) = 2gm$$

$$aM + 2am = 2gm$$

$$aM = 2gm - 2am$$

$$M = \frac{2gm - 2am}{a}$$

22.

$$v = \frac{V(m + M)}{m}$$

$$mv = mV + MV$$

$$MV = mv - mV$$

$$M = \frac{mv - mV}{V}$$

23.

$$C_0^2 = C_1^2(1 + 2V)$$

$$C_0^2 = C_1^2 + 2C_1^2V$$

$$2C_1^2V = C_0^2 - C_1^2$$

$$V = \frac{C_0^2 - C_1^2}{2C_1^2}$$

24.

$$A_1 = A(M + 1)$$

$$A_1 = AM + A$$

$$AM = A_1 - A$$

$$M = \frac{A_1 - A}{A}$$

25.

$$N = r(A - s)$$

$$N = Ar - rs$$

$$rs + N = Ar$$

$$rs = Ar - N$$

$$s = \frac{Ar - N}{r}$$

26.

$$T = 3(T_2 - T_1)$$

$$T = 3T_2 - 3T_1$$

$$3T_1 + T = 3T_2$$

$$3T_1 = 3T_2 - T$$

$$T_1 = \frac{3T_2 - T}{3}$$

27.

$$T_2 = T_1 - \frac{h}{100}$$

$$100T_2 = 100T_1 - h$$

$$h + 100T_2 = 100T_1$$

$$h = 100T_1 - 100T_2$$

28.

$$p_2 = p_1 + rp_1(1 - p_1)$$

$$p_2 - p_1 = rp_1(1 - p_1)$$

$$r = \frac{p_2 - p_1}{p_1(1 - p_1)}$$

29.

$$Q_1 = P(Q_2 - Q_1)$$

$$Q_1 = PQ_2 - PQ_1$$

$$PQ_2 = Q_1 + PQ_1$$

$$Q_2 = \frac{Q_1 + PQ_1}{P}$$

30.

$$p - p_a = dg(y_2 - y_1)$$

$$y_2 - y_1 = \frac{p - p_a}{dg}$$

$$y_2 = \frac{p - p_a}{dg} + y_1$$

31.

$$N = N_1T - N_2(1 - T)$$

$$N_1T = N + N_2(1 - T)$$

$$N_1 = \frac{N + N_2 - N_2T}{T}$$

32.

$$t_a = t_c + (1 - h)t_m$$

$$t_a = t_c + t_m - ht_m$$

$$t_a + ht_m = t_c + t_m$$

$$ht_m = t_c + t_m - t_a$$

$$h = \frac{t_c + t_m - t_a}{t_m}$$

33.

$$L = \pi(r_1 + r_2) + 2x_1 + 2x_2$$

$$L = \pi r_1 + \pi r_2 + 2x_1 + 2x_2$$

$$\pi r_1 = L - \pi r_2 - 2x_1 - 2x_2$$

$$r_1 = \frac{L - \pi r_2 - 2x_1 - 2x_2}{\pi}$$

34.

$$I = \frac{VR_2 + VR_1(1 + \mu)}{R_1 R_2}$$

$$IR_1 R_2 = VR_2 + VR_1 + VR_1 \mu$$

$$VR_1 \mu = IR_1 R_2 - VR_2 + VR_1$$

$$\mu = \frac{IR_1 R_2 - VR_2 + VR_1}{VR_1}$$

35.

$$P = \frac{V_1(V_2 - V_1)}{gJ}$$

$$gJP = V_1 V_2 - V_1^2$$

$$V_1 V_2 = V_1^2 + gJP$$

$$V_2 = \frac{V_1^2 + gJP}{V_1}$$

36.

$$W = T(S_1 - S_2) - Q$$

$$W + Q = TS_1 - TS_2$$

$$TS_2 = TS_1 - W - Q$$

$$S_2 = \frac{TS_1 - W - Q}{T}$$

37.

$$C = \frac{2eAk_1 k_2}{d(k_1 + k_2)}$$

$$Cd(k_1 + k_2) = 2eAk_1 k_2$$

$$e = \frac{Cd(k_1 + k_2)}{2Ak_1 k_2}$$

38.

$$d = \frac{3LPx^2 - Px^3}{6EI}$$

$$6dEI = 3LPx^2 - Px^3$$

$$3LPx^2 = 6dEI + Px^3$$

$$L = \frac{6dEI + Px^3}{3Px^2}$$

39.

$$V = C \left(1 - \frac{n}{N} \right)$$

$$V = C - \frac{Cn}{N}$$

$$V + \frac{Cn}{N} = C$$

$$\frac{Cn}{N} = C - V$$

$$Cn = CN - NV$$

$$n = \frac{CN - NV}{C}$$

40.

$$\frac{p}{P} = \frac{AI}{B + AI}$$

$$p(B + AI) = AIP$$

$$pB + AIp = AIP$$

$$pB = AIP - AIp$$

$$B = \frac{AIP - AIp}{p}$$

41.

$$\eta = \frac{T_2}{T_1 + T_2}$$

$$\eta(T_1 + T_2) = T_2$$

$$\eta T_1 + \eta T_2 = T_2$$

$$\eta T_1 = T_2 - \eta T_2$$

$$T_1 = \frac{T_2 - \eta T_2}{\eta}$$

$$T_1 = \frac{875 \text{ K} - 0.450(875 \text{ K})}{0.450}$$

$$T_1 = \frac{875 \text{ K} - 393.75 \text{ K}}{0.450}$$

$$T_1 = \frac{481.25 \text{ K}}{0.450}$$

$$T_1 = 1069.444444 \text{ K}$$

$$T_1 = 1070 \text{ K}$$

42.

$$P_t = P_c(1 + 0.500m^2)$$

$$P_c = \frac{P_t}{1 + 0.500m^2}$$

$$P_c = \frac{685 \text{ W}}{1 + 0.500(0.925)^2}$$

$$P_c = \frac{685 \text{ W}}{1 + 0.500(0.855625)}$$

$$P_c = \frac{685 \text{ W}}{1 + 0.4278125}$$

$$P_c = \frac{685 \text{ W}}{1.4278125}$$

$$P_c = 479.7548698 \text{ W}$$

$$P_c = 4.80 \times 10^2 \text{ W}$$

43.

$$F = \frac{9}{5}C + 32$$

$$90.2 = \frac{9}{5}C + 32$$

$$\frac{5}{9}(90.2 - 32) = C$$

$$C = \frac{5}{9} \times 58.2$$

$$C = 32.3^\circ \text{C}$$

44.

$$V = \frac{1}{2}L(B + b)$$

$$2V = BL + bL$$

$$bL = 2V - BL$$

$$b = \frac{2V - BL}{L}$$

$$b = \frac{2(1.09 \text{ m}^3) - (0.244 \text{ m}^2)(4.91 \text{ m})}{(4.91 \text{ m})}$$

$$b = \frac{2.18 \text{ m}^3 - 1.19804 \text{ m}^3}{4.91 \text{ m}}$$

$$b = \frac{0.98186 \text{ m}^3}{4.91 \text{ m}}$$

$$b = 0.199991853 \text{ m}^2$$

$$b = 0.200 \text{ m}^2$$

45.

$$V_1 = \frac{VR_1}{R_1 + R_2}$$

$$V_1(R_1 + R_2) = VR_1$$

$$R_1 + R_2 = \frac{VR_1}{V_1}$$

$$R_2 = \frac{VR_1}{V_1} - R_1$$

$$R_2 = \frac{(12.0 \text{ V})(3.56 \Omega)}{6.30 \text{ V}} - (3.56 \Omega)$$

$$R_2 = 6.780952381 \Omega - 3.56 \Omega$$

$$R_2 = 3.220952381 \Omega$$

$$R_2 = 3.22 \Omega$$

46.

$$\eta = \frac{1}{q + p(1 - q)}$$

$$\eta[q + p(1 - q)] = 1$$

$$\eta q + \eta p(1 - q) = 1$$

$$\eta p(1 - q) = 1 - \eta q$$

$$p = \frac{1 - \eta q}{\eta(1 - q)}$$

$$p = \frac{1 - (0.66)(0.83)}{0.66(1 - 0.83)}$$

$$p = \frac{1 - 0.5478}{0.66(0.17)}$$

$$p = \frac{0.4522}{0.1122}$$

$$p = 4.03030303$$

$$p = 4 \text{ processors}$$

47.

$$d = v_2 t_2 + v_1 t_1$$

$$d = v_2(4 \text{ h}) + v_1(t + 2 \text{ h})$$

$$tv_1 + v_1(2 \text{ h}) = d - v_2(4 \text{ h})$$

$$tv_1 = d - v_2(4 \text{ h}) - v_1(2 \text{ h})$$

$$t = \frac{d - v_2(4 \text{ h}) - v_1(2 \text{ h})}{v_1}$$

48.

$$C = x + 15y$$

$$15y = C - x$$

$$y = \frac{C - x}{15}$$

1.12 Applied Word Problems

1.

Let x = the number of 1.5 Ω resistors.

Let $34-x$ = the number of 2.5 Ω resistors.

$$1.5x + 2.5(34 - x) = 56$$

$$1.5x + 85 - 2.5x = 56$$

$$-x = 56 - 85$$

$$-x = -29$$

$$x = 29$$

There are 29 of the 1.5 Ω resistors and $(34 - 29) = 5$ of the 2.5 Ω resistors.

Check:

$$29(1.5 \Omega) + 5(2.5 \Omega) = 56 \Omega$$

$$43.5 \Omega + 12.5 \Omega = 56 \Omega$$

$$56 \Omega = 56 \Omega$$

2.

Let x = the number of slides with 5 mg.

Let $x-3$ = the number of slides with 6 mg.

$$(5 \text{ mg})x = (6 \text{ mg})(x - 3)$$

$$(5 \text{ mg})x = (6 \text{ mg})x - 18 \text{ mg}$$

$$-x = -18$$

$$x = 18 \text{ slides}$$

There are 18 slides with 5 mg and $(18 - 3) = 15$ slides with 6 mg.

Check:

$$5 \text{ mg}(18) = 6 \text{ mg}(15)$$

$$90 \text{ mg} = 90 \text{ mg}$$

3.

Let t = the time for the shuttle to reach the satellite.

$$(29\,500 \text{ km/h})t = 6000 \text{ km} + (27\,500 \text{ km/h})t$$

$$(2000 \text{ km/h})t = 6000 \text{ km}$$

$$t = \frac{6000 \text{ km}}{2000 \text{ km/h}}$$

$$t = 3.000 \text{ h}$$

It will take the shuttle 3.000 h to reach the satellite.

Check:

$$(29\,500 \text{ km/h})(3 \text{ h}) = 6000 \text{ km} + (27\,500 \text{ km/h})(3 \text{ h})$$

$$88\,500 \text{ km} = 6000 \text{ km} + 82\,500 \text{ km}$$

$$88\,500 \text{ km} = 88\,500 \text{ km}$$

4.Let x = the number of litres of 50% methanol blend that must be added.

$$0.0600(7250 \text{ L}) + 0.500(x) = 0.100(7250 \text{ L} + x)$$

$$435 \text{ L} + 0.500(x) = 725 \text{ L} + 0.100x$$

$$0.400(x) = 290 \text{ L}$$

$$x = \frac{290 \text{ L}}{0.400}$$

$$x = 725 \text{ L}$$

725 L of the 50% methanol blend must be added.

Check:

$$0.0600(7250 \text{ L}) + 0.500(725 \text{ L}) = 0.100(7250 \text{ L} + 725 \text{ L})$$

$$435 \text{ L} + 362.5 \text{ L} = 0.1(7975 \text{ L})$$

$$797.5 \text{ L} = 797.5 \text{ L}$$

5.Let x = the cost of the car 6 years ago.Let $x + \$5000$ = the cost of the car model today.

$$x + (x + \$5000) = \$49\,000$$

$$2x = \$44\,000$$

$$x = \frac{\$44\,000}{2}$$

$$x = \$22\,000$$

The cost of the car 6 years ago was \$22 000, and the cost of the today's model is $(\$22\,000 + 5000) = \$27\,000$.

Check:

$$\$22\,000 + (\$22\,000 + \$5000) = \$49\,000$$

$$\$22\,000 + \$27\,000 = \$49\,000$$

$$\$49\,000 = \$49\,000$$

6.Let x = the flow from the first stream in m^3/s .Let $x - 45 \text{ m}^3/\text{s}$ = the flow from the second stream in m^3/s .

$$x + (x - 45 \text{ m}^3/\text{s}) = \frac{414\,000 \text{ m}^3}{3600 \text{ s}}$$

$$2x - 45 \text{ m}^3/\text{s} = 160 \text{ m}^3/\text{s}$$

$$2x = 160 \text{ m}^3/\text{s}$$

$$x = \frac{160 \text{ m}^3/\text{s}}{2}$$

$$x = 80 \text{ m}^3/\text{s}$$

The first stream flows $80 \text{ m}^3/\text{s}$ and the second stream flows $(80 \text{ m}^3/\text{s} - 45 \text{ m}^3/\text{s}) = 35 \text{ m}^3/\text{s}$.

Check:

$$80 \text{ m}^3/\text{s} + (80 \text{ m}^3/\text{s} - 45 \text{ m}^3/\text{s}) = \frac{414\,000 \text{ m}^3}{3600 \text{ s}}$$

$$80 \text{ m}^3/\text{s} + 35 \text{ m}^3/\text{s} = 115 \text{ m}^3/\text{s}$$

$$115 \text{ m}^3/\text{s} = 115 \text{ m}^3/\text{s}$$

7.Let x = the number of cars recycled the first year.Let $x + 700\,000$ = the number of cars recycled the second year.

$$x + (x + 700\,000 \text{ cars}) = 4\,500\,000 \text{ cars}$$

$$2x + 700\,000 \text{ cars} = 4\,500\,000 \text{ cars}$$

$$2x = 3\,800\,000 \text{ cars}$$

$$x = \frac{3\,800\,000 \text{ cars}}{2}$$

$$x = 1\,900\,000 \text{ cars}$$

The first year, 1.9×10^5 cars were recycled, and the second year $(1\,900\,000 + 700\,000) = 2.6 \times 10^5$ cars were recycled.

Check:

$$1\,900\,000 \text{ cars} + (1\,900\,000 \text{ cars} + 700\,000 \text{ cars}) = 4\,500\,000 \text{ cars}$$

$$1\,900\,000 \text{ cars} + 2\,600\,000 \text{ cars} = 4\,500\,000 \text{ cars}$$

$$4\,500\,000 \text{ cars} = 4\,500\,000 \text{ cars}$$

8.Let x = the number of hits to the website on the first day.Let $\frac{1}{4}x + 4000$ = the number of hits on the second day.Let $\frac{1}{4}x$ = the number of hits on the third day.

$$\frac{1}{4}x + 4000 \text{ hits} + \frac{1}{4}x = x$$

$$\frac{1}{2}x + 4000 \text{ hits} = x$$

$$\frac{1}{2}x = 4000 \text{ hits}$$

$$x = \frac{4000 \text{ hits}}{\frac{1}{2}}$$

$$x = 8000 \text{ hits}$$

The first day there were 8000 hits, the second day there were $(\frac{1}{4}(8000 \text{ hits}) + 4000 \text{ hits}) = 6000$ hits, and the third day there were $(\frac{1}{4}(8000 \text{ hits})) = 2000$ hits.

Check:

$$\frac{1}{4}(8000 \text{ hits}) + 4000 \text{ hits} + \frac{1}{4}(8000 \text{ hits}) = 8000 \text{ hits}$$

$$2000 \text{ hits} + 4000 \text{ hits} + 2000 \text{ hits} = 8000 \text{ hits}$$

$$8000 \text{ hits} = 8000 \text{ hits}$$

9.Let x = the number hectares of land leased for \$200 per hectare.Let $140 - x$ = the number of hectares of land leased for \$300 per hectare.

$$\$200 / \text{hectare } x + \$300 / \text{hectare}(140 \text{ hectares} - x) = \$37\,000$$

$$-\$100 / \text{hectare } x = -\$5\,000$$

$$x = \frac{-\$5000}{-\$100 / \text{hectare}}$$

$$x = 50 \text{ hectares}$$

There are 50 hectares leased at \$200 per hectare and $(140 \text{ hectares} - 50 \text{ hectares}) = 90$ hectares leased for \$300 per hectare.

Check:

$$\$200 / \text{hectare } (50 \text{ hectares}) + \$300 / \text{hectare}(140 \text{ hectares} - (50 \text{ hectares})) = \$37\,000$$

$$\$10\,000 + \$27\,000 = \$37\,000$$

$$\$37\,000 = \$37\,000$$

10.

Let x = the first dose in mg.

Let $x + 660$ mg = the second dose in mg.

$$x + x + 660 \text{ mg} = 2000 \text{ mg}$$

$$2x = 1340 \text{ mg}$$

$$x = \frac{1340 \text{ mg}}{2}$$

$$x = 670 \text{ mg}$$

The first dose is 670 mg, and the second dose is $(670 \text{ mg} + 660 \text{ mg}) = 1130 \text{ mg}$.

Check:

$$670 \text{ mg} + 670 \text{ mg} + 660 \text{ mg} = 2000 \text{ mg}$$

$$670 \text{ mg} + 1330 \text{ mg} = 2000 \text{ mg}$$

$$2000 \text{ mg} = 2000 \text{ mg}$$

11.

Let x = the amount of pollutant after modification in ppm/h.

$$(5 \text{ h})x = (3 \text{ h})150 \text{ ppm/h}$$

$$x = \frac{450 \text{ ppm}}{5 \text{ h}}$$

$$x = 90 \text{ ppm/h}$$

The amount of pollutant after modification is 90 ppm/h. The device reduced emissions by $(150 \text{ ppm/h} - 90 \text{ ppm/h}) = 60 \text{ ppm/h}$.

Check:

$$(5 \text{ h})90 \text{ ppm/h} = (3 \text{ h})150 \text{ ppm/h}$$

$$450 \text{ ppm} = 450 \text{ ppm}$$

12.

Let $x - 13$ = the number of teeth that the first meshed spur has.

Let x = the number of teeth that the second meshed spur has.

Let $x + 15$ = the number of teeth that the third meshed spur has.

$$x - 13 \text{ teeth} + x + x + 15 \text{ teeth} = 107 \text{ teeth}$$

$$3x + 2 = 107 \text{ teeth}$$

$$3x = 105 \text{ teeth}$$

$$x = \frac{105 \text{ teeth}}{3}$$

$$x = 35 \text{ teeth}$$

The first spur has $(35 - 13) = 22$ teeth, the second spur has 35 teeth, and the third spur has $(35 + 15) = 50$ teeth.

Check:

$$35 \text{ teeth} - 13 \text{ teeth} + 35 \text{ teeth} + 35 \text{ teeth} + 15 \text{ teeth} = 107 \text{ teeth}$$

$$107 \text{ teeth} = 107 \text{ teeth}$$

13.

Let x = the number of 18-m girders needed.

Let $x + 4$ = the number of 15-m girders needed.

$$(18 \text{ m})x = (15 \text{ m})(x + 4)$$

$$(18 \text{ m})x = (15 \text{ m})x + 60 \text{ m}$$

$$(3 \text{ m})x = 60 \text{ m}$$

$$x = \frac{60 \text{ m}}{3 \text{ m}}$$

$$x = 20 \text{ girders}$$

There would be 20 18-m girders needed or $(20 \text{ girders} + 4 \text{ girders}) = 24$ 15-m girders needed.

Check:

$$(18 \text{ m})20 = (15 \text{ m})(20 + 4)$$

$$360 \text{ m} = 360 \text{ m}$$

14.

Let x = the amount of oil used in a normal 8-week period in kL.

Let $x + 20 \text{ kL / week}$ = the amount oil used in the cold 6-week period in kL.

$$(8 \text{ weeks})x = (6 \text{ weeks})(x + 20 \text{ kL/week})$$

$$(8 \text{ weeks})x = (6 \text{ weeks})x + (6 \text{ weeks})20 \text{ kL/week}$$

$$(2 \text{ weeks})x = 120 \text{ kL}$$

$$x = \frac{120 \text{ kL}}{2 \text{ weeks}}$$

$$x = 60 \text{ kL/week}$$

Normally the amount of oil used would be 60 kL/week, which means that the fuel storage depot originally had $(60 \text{ kL/week} \times 8 \text{ weeks}) = 480 \text{ kL}$, which is $4.80 \times 10^5 \text{ L}$.

Check:

$$(8 \text{ weeks})60 \text{ kL/week} = (6 \text{ weeks})(60 \text{ kL/week} + 20 \text{ kL/week})$$

$$480 \text{ kL} = 480 \text{ kL}$$

15.

Let x = the first current in μA .

Let $2x$ = the second current in μA .

Let $x + 9.2 \mu\text{A}$ = the third current in μA

$$x + 2x + x + 9.2 \mu\text{A} = 0 \mu\text{A}$$

$$4x = -9.2 \mu\text{A}$$

$$x = \frac{-9.2 \mu\text{A}}{4}$$

$$x = -2.3 \mu\text{A}$$

The first current is $-2.3 \mu\text{A}$, the second current is $2(-2.3 \mu\text{A}) = -4.6 \mu\text{A}$, and the third current is $(-2.3 \mu\text{A} + 9.2 \mu\text{A}) = 6.9 \mu\text{A}$.

Check:

$$-2.3 \mu\text{A} + 2(-2.3 \mu\text{A}) + (-2.3 \mu\text{A}) + 9.2 \mu\text{A} = 0 \mu\text{A}$$

$$-2.3 \mu\text{A} - 4.6 \mu\text{A} - 2.3 \mu\text{A} + 9.2 \mu\text{A} = 0 \mu\text{A}$$

$$0 \mu\text{A} = 0 \mu\text{A}$$

16.

Let x = the number of trucks in the first fleet.

Let $x + 5$ = the number of trucks in the second fleet.

$$(8 \text{ h})x + (6 \text{ h})(x + 5) = 198 \text{ h}$$

$$(8 \text{ h})x + (6 \text{ h})x + 30 \text{ h} = 198 \text{ h}$$

$$(14 \text{ h})x = 168 \text{ h}$$

$$x = \frac{168 \text{ h}}{14 \text{ h}}$$

$$x = 12 \text{ trucks}$$

There are 12 trucks in the first fleet and $(12 \text{ trucks} + 5 \text{ trucks}) = 17 \text{ trucks}$ in the second fleet.

Check:

$$(8 \text{ h})(12) + (6 \text{ h})(12 + 5) = 198 \text{ h}$$

$$96 \text{ h} + (6 \text{ h})(17) = 198 \text{ h}$$

$$96 \text{ h} + 102 \text{ h} = 198 \text{ h}$$

$$198 \text{ h} = 198 \text{ h}$$

17.

Let x = the length of the first pipeline in km.

Let $x + 2.6 \text{ km}$ = the length of the 3 other pipelines.

$$x + 3(x + 2.6 \text{ km}) = 35.4 \text{ km}$$

$$x + 3x + 7.8 \text{ km} = 35.4 \text{ km}$$

$$4x = 27.6 \text{ km}$$

$$x = \frac{27.6 \text{ km}}{4}$$

$$x = 6.9 \text{ km}$$

The first pipeline is 6.9 km long, and the other three pipelines are each $(6.9 \text{ km} + 2.6 \text{ km}) = 9.5 \text{ km}$ long.

Check:

$$6.9 \text{ km} + 3(6.9 \text{ km} + 2.6 \text{ km}) = 35.4 \text{ km}$$

$$6.9 \text{ km} + 3(9.5 \text{ km}) = 35.4 \text{ km}$$

$$6.9 \text{ km} + 28.5 \text{ km} = 35.4 \text{ km}$$

$$35.4 \text{ km} = 35.4 \text{ km}$$

18.

Let x = the power of the first generator in MW.

Let $750 \text{ MW} - x$ = the power of the second generator in MW.

$$0.65x + 0.75(750 \text{ MW} - x) = 530 \text{ MW}$$

$$0.65x + 562.5 \text{ MW} - 0.75x = 530 \text{ MW}$$

$$-0.1x = -32.5 \text{ MW}$$

$$x = \frac{-32.5 \text{ MW}}{-0.1}$$

$$x = 325 \text{ MW}$$

The first generator produces 325 MW of power, and the second generator produces $(750 \text{ MW} - 325 \text{ MW}) = 425 \text{ MW}$ of power.

Check:

$$0.65(325 \text{ MW}) + 0.75(750 \text{ MW} - (325 \text{ MW})) = 530 \text{ MW}$$

$$211.25 \text{ MW} + 0.75(425 \text{ MW}) = 530 \text{ MW}$$

$$211.25 \text{ MW} + 318.75 \text{ MW} = 530 \text{ MW}$$

$$530 \text{ MW} = 530 \text{ MW}$$

19.Let x = the number of CDs.Let $54 - x$ = the number of DVDs.

$$\$15x + \$18(54 - x) = \$876$$

$$\$15x + \$972 - \$18x = \$876$$

$$-\$3x = -\$96$$

$$x = \frac{-\$96}{-\$3}$$

$$x = 32 \text{ CDs}$$

The person has 32 CDs and $(54 - 32) = 22$ DVDs.

Check:

$$\$15(32) + \$18(54 - 32) = \$876$$

$$\$480 + \$18(22) = \$876$$

$$\$480 + \$396 = \$876$$

$$\$876 = \$876$$

20.The amount of lottery winnings after taxes is $\$20\,000 \times (1 - 0.25) = \$15\,000$.Let x = the amount of money invested at a 40% gain.Let $\$15\,000 - x$ = the amount of money invested at a 10% loss.

$$0.40x - 0.10(\$15\,000 - x) = \$2000$$

$$0.40x - \$1500 + 0.10x = \$2000$$

$$0.50x = \$3500$$

$$x = \frac{\$3500}{0.50}$$

$$x = \$7000$$

The 40% gain investment had $\$7000$ invested, and the 10% loss investment had $(\$15\,000 - \$7000) = \$8000$ invested.

Check:

$$0.40(\$7000) - 0.10(\$15\,000 - \$7000) = \$2000$$

$$\$2800 - \$1500 + 0.10(\$7000) = \$2000$$

$$\$2800 - \$1500 + \$700 = \$2000$$

$$\$2000 = \$2000$$

21.Let x = the amount of time the skier spends on the ski lift in minutes.Let 24 minutes $-x$ = the amount of time the skier spends skiing down the hill in minutes.

$$(50 \text{ m/min})x = (150 \text{ m/min})(24 \text{ min} - x)$$

$$(50 \text{ m/min})x = 3600 \text{ m} - (150 \text{ m/min})x$$

$$(200 \text{ m/min})x = 3600 \text{ m}$$

$$x = \frac{3600 \text{ m}}{200 \text{ m/min}}$$

$$x = 18 \text{ min}$$

The length of the slope is 18 minutes \times 50 m/minute = 900m.

Check:

$$(50 \text{ m/min})18 \text{ min} = (150 \text{ m/min})(24 \text{ min} - 18 \text{ min})$$

$$900 \text{ m} = 3600 \text{ m} - (150 \text{ m/min})(18 \text{ min})$$

$$900 \text{ m} = 3600 \text{ m} - 2700 \text{ m}$$

$$900 \text{ m} = 900 \text{ m}$$

22.

Let x = the speed of sound.

Let $x - 100$ km/h = speed travelled for 1 h.

Let $x + 400$ km/h = the speed travelled for 3 h.

$$1 \text{ h}(x - 100 \text{ km/h}) + 3 \text{ h}(x + 400 \text{ km/h}) = 5740 \text{ km}$$

$$(1 \text{ h})x - (1 \text{ h})(100 \text{ km/h}) + (3 \text{ h})x + (3 \text{ h})(400 \text{ km/h}) = 5740 \text{ km}$$

$$(1 \text{ h})x - 100 \text{ km} + (3 \text{ h})x + 12000 \text{ km} = 5740 \text{ km}$$

$$(4 \text{ h})x = 4640 \text{ km}$$

$$x = \frac{4640 \text{ km}}{4 \text{ h}}$$

$$x = 1160 \text{ km/h}$$

The speed of sound is 1160 km/h.

Check:

$$1 \text{ h}(1160 \text{ km/h} - 100 \text{ km/h}) + 3 \text{ h}(1160 \text{ km/h} + 400 \text{ km/h}) = 5740 \text{ km}$$

$$1 \text{ h}(1060 \text{ km/h}) + 3 \text{ h}(1560 \text{ km/h}) = 5740 \text{ km}$$

$$1060 \text{ km} + 4680 \text{ km} = 5740 \text{ km}$$

$$5740 \text{ km} = 5740 \text{ km}$$

23.

Let x = the speed the train leaving England in km/h.

Let $x + 8$ km/h = speed of the train leaving France in km/h.

The distance travelled by each train is speed \times time.

$$x \left(\frac{17 \text{ min}}{60 \text{ min/h}} \right) + (x + 8 \text{ km/h}) \left(\frac{17 \text{ min}}{60 \text{ min/h}} \right) = 50 \text{ km}$$

$$(0.28333 \text{ h})x + (x + 8 \text{ km/h})(0.28333 \text{ h}) = 50 \text{ km}$$

$$(0.28333 \text{ h})x + (0.28333 \text{ h})x + 2.26667 \text{ km} = 50 \text{ km}$$

$$(0.56666 \text{ h})x = 47.73333 \text{ km}$$

$$x = \frac{47.73333 \text{ km}}{0.56666 \text{ h}}$$

$$x = 84.23529421 \text{ km/h}$$

$$x = 84.2 \text{ km/h}$$

The train leaving England was travelling at 84.2 km/h, and the train leaving France was travelling at $(84.2 \text{ km/h} + 8 \text{ km/h}) = 92.2 \text{ km/h}$.

Check:

$$84.23529421 \text{ km/h} \left(\frac{17 \text{ min}}{60 \text{ min/h}} \right) + (84.23529421 \text{ km/h} + 8 \text{ km/h}) \left(\frac{17 \text{ min}}{60 \text{ min/h}} \right) = 50 \text{ km}$$

$$23.86666 \text{ km} + (92.23529421 \text{ km/h}) \left(\frac{17 \text{ min}}{60 \text{ min/h}} \right) = 50 \text{ km}$$

$$23.86666 \text{ km} + 26.13333 \text{ km} = 50 \text{ km}$$

$$50 \text{ km} = 50 \text{ km}$$

24.

Let x = time left until the appointment.

Let $x - 10.0$ min = time taken to get to the appointment travelling at 60.0 km/h.

Let $x - 5.0$ min = time taken to get to the appointment travelling at 45.0 km/h.

The distance travelled by the executive in each scenario is the same. Distance = speed \times time

$$60.0 \text{ km/h} \left(x - \frac{10.0 \text{ min}}{60 \text{ min/h}} \right) = 45 \text{ km/h} \left(x - \frac{5.0 \text{ min}}{60 \text{ min/h}} \right)$$

$$(60.0 \text{ km/h})x - 60 \text{ km/h} \left(\frac{10.0 \text{ min}}{60 \text{ min/h}} \right) = (45 \text{ km/h})x - 45 \text{ km/h} \left(\frac{5.0 \text{ min}}{60 \text{ min/h}} \right)$$

$$(60.0 \text{ km/h})x - 10 \text{ km} = (45.0 \text{ km/h})x - 3.75 \text{ km}$$

$$(15.0 \text{ km/h})x = 6.25 \text{ km}$$

$$x = \frac{6.25 \text{ km}}{15.0 \text{ km/h}}$$

$$x = 0.416666667 \text{ h}$$

$$x = 0.416666667 \text{ h} \times 60 \text{ min/h}$$

$$x = 25 \text{ min}$$

There is 25 minutes left until the executive's appointment.

Check:

$$60.0 \text{ km/h} \left(0.41667 \text{ h} - \frac{10.0 \text{ min}}{60 \text{ min/h}} \right) = 45 \text{ km/h} \left(0.41667 \text{ h} - \frac{5.0 \text{ min}}{60 \text{ min/h}} \right)$$

$$60.0 \text{ km/h}(0.25 \text{ h}) = 45 \text{ km/h}(0.33333 \text{ h})$$

$$15 \text{ km} = 15 \text{ km}$$

25.

Let $x - 30.0 \text{ s}$ = time since the first car started moving in the race in seconds.

Let x = time since the second car started the race in seconds.

The distance travelled by each car will be the same at the point where the first car overtakes the second car. Distance = speed \times time.

$$79.0 \text{ m/s}(x - 30.0 \text{ s}) = 73.0 \text{ m/s}(x)$$

$$(79.0 \text{ m/s})x - (79.0 \text{ m/s})(30.0 \text{ s}) = (73.0 \text{ m/s})x$$

$$(79.0 \text{ m/s})x - 2370 \text{ m} = (73.0 \text{ m/s})x$$

$$(6.0 \text{ m/s})x = 2370 \text{ m}$$

$$x = \frac{2370 \text{ m}}{6.0 \text{ m/s}}$$

$$x = 395 \text{ s}$$

The first car will overtake the second car after 395 s. The first car travels $79 \text{ m/s} \times (395 \text{ s} - 30 \text{ s}) = 28\,835 \text{ m}$ by this point. 8 laps around the track is 4.36 km/lap . $8 \text{ laps} \times 1000 \text{ m/km} = 34\,880 \text{ m}$, so the first car will already be in the lead at the end of the 8th lap.

Check:

$$79.0 \text{ m/s}(395 \text{ s} - 30.0 \text{ s}) = 73.0 \text{ m/s}(395 \text{ s})$$

$$79.0 \text{ m/s}(365 \text{ s}) = 73.0 \text{ m/s}(395 \text{ s})$$

$$28\,835 \text{ m} = 28\,835 \text{ m}$$

26.

Let x = the number of the first chips that is defective 0.50%.

Let $6100 - x$ = the number of the second chips that is defective 0.80%.

$$0.0050(x) + 0.0080(6100 \text{ chips} - x) = 38 \text{ chips}$$

$$(0.0050)x + 48.8 \text{ chips} - (0.0080)x = 38 \text{ chips}$$

$$-(0.0030)x = -10.8 \text{ chips}$$

$$x = \frac{-10.8 \text{ chips}}{-0.0030}$$

$$x = 3600 \text{ chips}$$

There are 3600 chips that are 0.50% defective and $(6100 \text{ chips} - 3600 \text{ chips}) = 2500 \text{ chips}$ that are defective 0.80%.

Check:

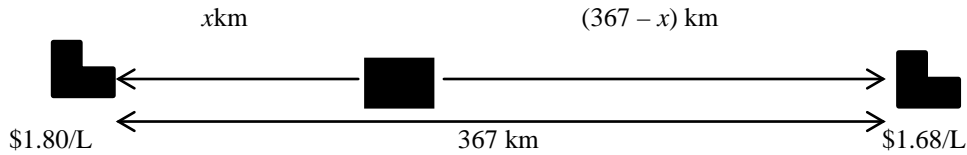
$$0.0050(3600 \text{ chips}) + 0.0080(6100 \text{ chips} - 3600 \text{ chips}) = 38 \text{ chips}$$

$$18 \text{ chips} + 0.0080(2500 \text{ chips}) = 38 \text{ chips}$$

$$18 \text{ chips} + 20 \text{ chips} = 38 \text{ chips}$$

$$38 \text{ chips} = 38 \text{ chips}$$

27.



Assuming that the customer is located between the two gasoline distributors:

Let x = the distance in km to the first gasoline distributor that costs \$1.80/L.

Let $367 \text{ km} - x$ = the distance in km to the second gasoline distributor that costs \$1.68.

$$\$1.80 + \$0.0016(x) = \$1.68 + \$0.0016(367 - x)$$

$$\$1.80 + \$0.0016(x) = \$1.68 + \$0.5872 - \$0.0016(x)$$

$$\$0.0032(x) = \$0.4672$$

$$x = \frac{\$0.4672}{\$0.0032}$$

$$x = 146 \text{ km}$$

The customer is 146 km away from the first gas distributor (\$1.80/L) and $(367 \text{ km} - 146 \text{ km}) = 221 \text{ km}$ away from the second gas distributor (\$1.68).

Check:

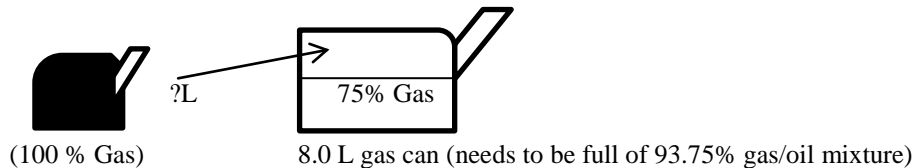
$$\$1.80 + \$0.0016(146 \text{ km}) = \$1.68 + \$0.0016(367 \text{ km} - 146 \text{ km})$$

$$\$1.80 + \$0.2336 = \$1.68 + \$0.0016(221 \text{ km})$$

$$\$1.80 + \$0.2336 = \$1.68 + \$0.3536$$

$$\$2.0336 = \$2.0336$$

28.



A 15:1 gas/oil mixture is $\frac{15}{16}$ gasoline = 93.75%.

Let x = the amount of 100% gasoline added in L.

Let $8.0 \text{ L} - x$ = the amount of 75% gasoline mixture in L.

$$1.00(x) + 0.75(8.0 \text{ L} - x) = 0.9375(8.0 \text{ L})$$

$$1.00(x) + 6.0 \text{ L} - 0.75(x) = 7.5 \text{ L}$$

$$0.25(x) = 1.5 \text{ L}$$

$$x = \frac{1.5 \text{ L}}{0.25}$$

$$x = 6.0 \text{ L}$$

6.0 L of 100% gasoline must be added to the 75% gas/oil mixture to make 8 L of 15:1 gasoline/ oil.

Check:

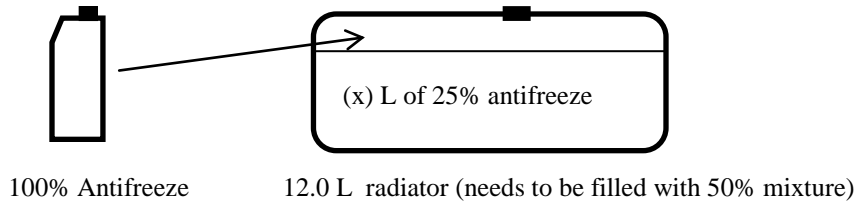
$$1.00(6.0 \text{ L}) + 0.75(8.0 \text{ L} - 6.0 \text{ L}) = 0.9375(8.0 \text{ L})$$

$$6 \text{ L} + 0.75(2.0 \text{ L}) = 7.5 \text{ L}$$

$$6 \text{ L} + 1.5 \text{ L} = 7.5 \text{ L}$$

$$7.5 \text{ L} = 7.5 \text{ L}$$

29.



Let x = the amount in L of 25% antifreeze left in radiator
 Let $12.0 \text{ L} - x$ = the amount of 100% antifreeze added in L.

$$0.25(x) + 1.00(12.0 \text{ L} - x) = 0.5(12.0 \text{ L})$$

$$0.25(x) + 12.0 \text{ L} - 1.00(x) = 6.0 \text{ L}$$

$$-0.75(x) = -6.0 \text{ L}$$

$$x = \frac{-6.0 \text{ L}}{-0.75}$$

$$x = 8.0 \text{ L}$$

There needs to be 8L of 25% antifreeze left in radiator, so $(12.0 \text{ L} - 8.0 \text{ L}) = 4.0 \text{ L}$ must be drained.

Check:

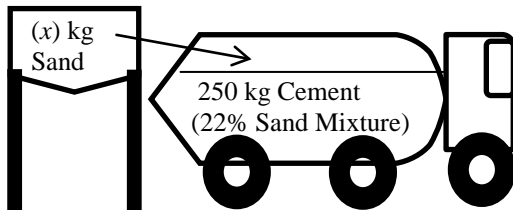
$$0.25(8.0 \text{ L}) + 1.00(12.0 \text{ L} - 8.0 \text{ L}) = 0.5(12.0 \text{ L})$$

$$2.0 \text{ L} + 1.00(4.0 \text{ L}) = 6.0 \text{ L}$$

$$2.0 \text{ L} + 4.0 \text{ L} = 6.0 \text{ L}$$

$$6.0 \text{ L} = 6.0 \text{ L}$$

30.



Let x = the amount of sand added.

Let $250 \text{ kg} + x$ = the amount in kg of the final 25% sand mixture.

$$1.00(x) + 0.22(250 \text{ kg}) = 0.25(250 \text{ kg} + x)$$

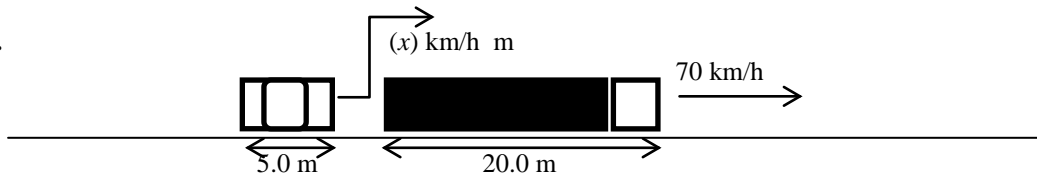
$$1.00(x) + 55 \text{ kg} = 62.5 \text{ kg} + 0.25(x)$$

$$0.75(x) = 7.5 \text{ kg}$$

$$x = \frac{7.5 \text{ kg}}{0.75}$$

$$x = 10 \text{ kg}$$

31.



Let x = the speed the car needs to travel in km/h to pass the semi in 10 s.

Speed = distance/time. 10 s is $10\text{s}/3600 \text{ s/h} = 0.002777777 \text{ h}$.

$$x = \frac{\text{distance needed to pass truck} + \text{distance travelled by truck in } 10\text{s}}{10\text{s}}$$

$$x = \frac{0.025 \text{ km} + 70 \text{ km/h}(0.0027777 \text{ h})}{0.0027777 \text{ h}}$$

$$x = \frac{0.025 \text{ km} + 0.19444 \text{ km}}{0.0027777 \text{ h}}$$

$$x = \frac{2.19444 \text{ km}}{0.0027777 \text{ h}}$$

$$x = 79 \text{ km/h}$$

The car needs to travel at a speed of 79 km/h to pass the semitrailer in 10s.

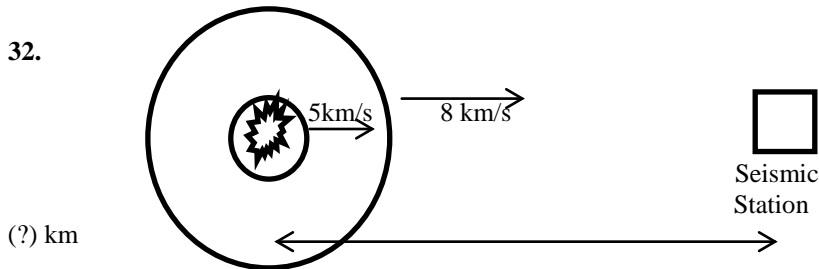
Check:

$$79 \text{ km/h} = \frac{0.025 \text{ km} + 70 \text{ km/h}(0.0027777 \text{ h})}{0.0027777 \text{ h}}$$

$$79 \text{ km/h} = \frac{0.025 \text{ km} + 0.19444 \text{ km}}{0.0027777 \text{ h}}$$

$$79 \text{ km/h} = 79 \text{ km/h}$$

32.



Let x = the time the first wave takes to travel to the seismic station in s.

Let $x + 120$ s = the time the first wave takes to travel to the seismic station in s.

Distance = speed \times time. The distances travelled by both waves to the seismic station are the same. 2.0 min is $(2.0 \text{ min} \times 60 \text{ s/min}) = 120$ s.

$$8.0 \text{ km/s}(x) = 5.0 \text{ km/s}(x + 120 \text{ s})$$

$$8.0 \text{ km/s}(x) = 5.0 \text{ km/s}(x) + (5 \text{ km/s})(120 \text{ s})$$

$$3.0 \text{ km/s}(x) = 600 \text{ km}$$

$$x = \frac{600 \text{ km}}{3.0 \text{ km/s}}$$

$$x = 200 \text{ s}$$

The distance to the seismic station is $(200 \text{ s} \times 8.0 \text{ km/s}) = 1600 \text{ km}$.

Check:

$$8.0 \text{ km/s}(200 \text{ s}) = 5.0 \text{ km/s}(200 \text{ s} + 120 \text{ s})$$

$$1600 \text{ km} = 5.0 \text{ km/s}(320 \text{ s})$$

$$1600 \text{ km} = 1600 \text{ km}$$

Review Exercises**1.**

$$(-2) + (-5) - 3 = -2 - 5 - 3 = -10$$

2.

$$6 - 8 - (-4) = 6 - 8 + 4 = 2$$

3.

$$\frac{(-5)(6)(-4)}{(-2)(3)} = \frac{(20)\cancel{(\emptyset)}}{-\cancel{(\emptyset)}} = -20$$

4.

$$\frac{(-9)(-12)(-4)}{24} = \frac{108(-4)}{24} = \frac{-432}{24} = -18$$

5.

$$-5 - |2(-6)| + \frac{-15}{3} = -5 - |-12| + (-5) = -5 - 12 - 5 = -22$$

6.

$$3 - 5|-3 - 2| - \frac{12}{-4} = 3 - 5|-5| - (-3) = 3 - 5(5) + 3 = 6 - 25 = -19$$

7.

$$\frac{18}{3-5} - (-4)^2 = \frac{18}{-2} - (-4)(-4) = -9 - 16 = -25$$

8.

$$-(-3)^2 - \frac{-8}{(-2) - |-4|} = -(-3)(-3) - \frac{-8}{(-2) - 4} = -9 - \frac{-8}{-6} = -9 - \frac{27}{3} - \frac{4}{3} = -\frac{31}{3}$$

9.

$$\sqrt{16} - \sqrt{64} = \sqrt{(4)(4)} - \sqrt{(8)(8)} = 4 - 8 = -4$$

10.

$$-\sqrt{81+144} = -\sqrt{225} = -\sqrt{(5)(5)(3)(3)} = -(3)(5) = -15$$

11.

$$(\sqrt{7})^2 - \sqrt[3]{8} = (\sqrt{7})(\sqrt{7}) - \sqrt[3]{(2)(2)(2)} = 7 - 2 = 5$$

12.

$$-\sqrt[4]{16} + (\sqrt{6})^2 = -\sqrt[4]{(2)(2)(2)(2)} + (\sqrt{6})(\sqrt{6}) = -2 + 6 = 4$$

13.

$$(-2rt^2)^2 = (-2)^2 r^2 t^{2 \times 2} = 4r^2 t^4$$

14.

$$(3a^0 b^{-2})^3 = (3)^3 (1)^3 b^{-2 \times 3} = 27(1)b^{-6} = \frac{27}{b^6}$$

15.

$$-3mn^{-5}t(8m^{-3}n^4) = -(3)(8)m^{1-3}n^{-5+4}t = -24m^{-2}n^{-1}t = -\frac{24t}{m^2n}$$

16.

$$\frac{15p^4q^2r}{5pq^5r} = \frac{3p^{4-1}\cancel{r}}{q^{5-2}\cancel{r}} = \frac{3p^3}{q^3}$$

17.

$$\frac{-16N^{-2}(NT^2)}{-2N^0T^{-1}} = \frac{8N^{-2+1}T^{2+1}}{(1)} = \frac{8N^{-1}T^3}{(1)} = \frac{8T^3}{N}$$

18.

$$\frac{-35x^{-1}y(x^2y)}{5xy^{-1}} = \frac{-7y^{1+1+1}x^2}{x^{1+1}} = \frac{-7y^3\cancel{x^2}}{\cancel{x^2}} = -7y^3$$

19.

$$\sqrt{45} = \sqrt{(5)(3)(3)} = 3\sqrt{5}$$

20.

$$\sqrt{9+36} = \sqrt{45} = \sqrt{(5)(3)(3)} = 3\sqrt{5}$$

21.

8840 has 3 significant digits. Rounded to 2 significant digits, it is 8800.

22.

21 450 has 4 significant digits. Rounded to 2 significant digits, it is 21 000.

23.

9.040 has 4 significant digits. Rounded to 2 significant digits, it is 9.0.

24.

0.700 has 3 significant digits. Rounded to 2 significant digits, it is 0.70.

25.

$$\begin{aligned} 37.3 - 16.92(1.067)^2 &= 37.3 - 16.92(1.138489) \\ &= 37.3 - 19.26323388 \\ &= 18.03676612 \end{aligned}$$

which rounds to 18.0.

26.

$$\begin{aligned} \frac{8.896 \times 10^{-12}}{3.5954 + 6.0449} &= \frac{8.896 \times 10^{-12}}{9.6403} \\ &= 9.227928591 \times 10^{-13} \end{aligned}$$

which rounds to 9.228×10^{-13} .

27.

$$\frac{\sqrt{0.1958+2.844}}{3.142(65)^2} = \frac{\sqrt{3.0398}}{3.142(4225)}$$

$$= \frac{1.743502223}{13274.95}$$

$$= 0.000131337$$

which rounds to 1.3×10^{-4} .

28.

$$\frac{1}{0.03568} + \frac{37\,466}{29.63^2} = 28.02690583 + \frac{37\,466}{877.9369}$$

$$= 28.02690583 + 42.67504874$$

$$= 70.70195457$$

which rounds to 70.70, assuming that the 1 is exact.

29.

$$a - 3ab - 2a + ab = -2ab - a$$

30.

$$xy - y - 5y - 4xy = -3xy - 6y$$

31.

$$6LC - (3 - LC) = 6LC - 3 + LC = 7LC - 3$$

32.

$$-(2x - b) - 3(-x - 5b) = -2x + b + 3x + 15b = 16b + x$$

33.

$$(2x - 1)(x + 5) = (2x)(x) + (2x)(5) + (-1)(x) + (-1)(5)$$

$$= 2x^2 + 10x - x - 5$$

$$= 2x^2 + 9x - 5$$

34.

$$(C - 4D)(2C - D) = (C)(2C) + (C)(-D) + (-4D)(2C) + (-4D)(-D)$$

$$= 2C^2 - CD - 8CD + 4D^2$$

$$= 2C^2 - 9CD + 4D^2$$

35.

$$(x + 8)^2 = (x + 8)(x + 8)$$

$$= (x)(x) + (x)(8) + (8)(x) + (8)(8)$$

$$= x^2 + 8x + 8x + 64$$

$$= x^2 + 16x + 64$$

36.

$$(2r - 9s)^2 = (2r - 9s)(2r - 9s)$$

$$= (2r)(2r) + (2r)(-9s) + (-9s)(2r) + (-9s)(-9s)$$

$$= 4r^2 - 18rs - 18rs + 81s^2$$

$$= 4r^2 - 36rs + 81s^2$$

37.

$$\begin{aligned}\frac{2h^3k^2 - 6h^4k^5}{2h^2k} &= \frac{2h^3k^2}{2h^2k} - \frac{6h^4k^5}{2h^2k} \\ &= h^{3-2}k^{2-1} - 3h^{4-2}k^{5-1} \\ &= -3h^2k^4 + hk\end{aligned}$$

38.

$$\begin{aligned}\frac{4a^2x^3 - 8ax^4}{-2ax^2} &= \frac{4a^2x^3}{-2ax^2} - \frac{8ax^4}{-2ax^2} \\ &= -2a^{2-1}x^{3-2} + \frac{4\cancel{a}x^{4-2}}{\cancel{a}} \\ &= 4x^2 - 2ax\end{aligned}$$

39.

$$\begin{aligned}4R - [2r - (3R - 4r)] &= 4R - [2r - 3R + 4r] \\ &= 4R - [6r - 3R] \\ &= 4R - 6r + 3R \\ &= 7R - 6r\end{aligned}$$

40.

$$\begin{aligned}3b - [3a - (a - 3b)] + 4a &= 4a + 3b - [3a - a + 3b] \\ &= 4a + 3b - [2a + 3b] \\ &= 4a + 3b - 2a - 3b \\ &= 2a\end{aligned}$$

41.

$$\begin{aligned}2xy - \{3z - [5xy - (7z - 6xy)]\} &= 2xy - \{3z - [5xy - 7z + 6xy]\} \\ &= 2xy - \{3z - [11xy - 7z]\} \\ &= 2xy - \{3z - 11xy + 7z\} \\ &= 2xy - \{10z - 11xy\} \\ &= 2xy - 10z + 11xy \\ &= 13xy - 10z\end{aligned}$$

42.

$$\begin{aligned}x^2 + 3b + [(b - y) - 3(2b - y + z)] &= x^2 + 3b + [b - y - 6b + 3y - 3z] \\ &= x^2 + 3b + [-5b + 2y - 3z] \\ &= x^2 + 3b - 5b + 2y - 3z \\ &= x^2 - 2b + 2y - 3z\end{aligned}$$

43.

$$\begin{aligned}(2x+1)(x^2-x-3) &= (2x)(x^2) + (2x)(-x) + (2x)(-3) + (1)(x^2) + (1)(-x) + (1)(-3) \\ &= 2x^3 - 2x^2 - 6x + x^2 - x - 3 \\ &= 2x^3 - x^2 - 7x - 3\end{aligned}$$

44.

$$\begin{aligned}
 (x-3)(2x^2-3x+1) &= (x)(2x^2) + (x)(-3x) + (x)(1) + (-3)(2x^2) + (-3)(-3x) + (-3)(1) \\
 &= 2x^3 - 3x^2 + x - 6x^2 + 9x - 3 \\
 &= 2x^3 - 9x^2 + 10x - 3
 \end{aligned}$$

45.

$$\begin{aligned}
 -3y(x-4y)^2 &= -3y(x-4y)(x-4y) \\
 &= -3y[(x)(x) + (x)(-4y) + (-4y)(x) + (-4y)(-4y)] \\
 &= -3y[x^2 - 4xy - 4xy + 16y^2] \\
 &= -3y[x^2 - 8xy + 16y^2] \\
 &= -3x^2y + 24xy^2 - 48y^3
 \end{aligned}$$

46.

$$\begin{aligned}
 -s(4s-3t)^2 &= -s(4s-3t)(4s-3t) \\
 &= -s[(4s)(4s) + (4s)(-3t) + (-3t)(4s) + (-3t)(-3t)] \\
 &= -s[16s^2 - 12st - 12st + 9t^2] \\
 &= -s[16s^2 - 24st + 9t^2] \\
 &= -16s^3 + 24s^2t - 9st^2
 \end{aligned}$$

47.

$$\begin{aligned}
 3p[(q-p) - 2p(1-3q)] &= 3p[q-p-2p+6pq] \\
 &= 3p[q-3p+6pq] \\
 &= 18p^2q - 9p^2 + 3pq
 \end{aligned}$$

48.

$$\begin{aligned}
 3x[2y-r-4(s-2r)] &= 3x[2y-r-4s+8r] \\
 &= 3x[2y+7r-4s] \\
 &= 21rx - 12sx + 6xy
 \end{aligned}$$

49.

$$\begin{aligned}
 \frac{12p^3q^2 - 4p^4q + 6pq^5}{2p^4q} &= \frac{12p^3q^2}{2p^4q} - \frac{4p^4q}{2p^4q} + \frac{6pq^5}{2p^4q} \\
 &= \frac{6q^{2-1}}{p^{4-3}} - \frac{2\cancel{p^4}q}{\cancel{p^4}q} + \frac{3q^{5-1}}{p^{4-1}} \\
 &= \frac{3q^1}{p^1} + \frac{6q}{p} - 2
 \end{aligned}$$

50.

$$\begin{aligned}
 \frac{27s^3t^2 - 18s^4t + 9s^2t}{9s^2t} &= \frac{27s^3t^2}{9s^2t} - \frac{18s^4t}{9s^2t} + \frac{9s^2t}{9s^2t} \\
 &= 3s^{3-2}t^{2-1} - \frac{2s^{4-2}\cancel{t}}{\cancel{t}} + \frac{\cancel{9s^2t}}{\cancel{9s^2t}} \\
 &= -2s^2 + 3st + 1
 \end{aligned}$$

51.

$$\begin{array}{r}
 \overline{) 2x^2 + 7x - 30} \\
 \underline{2x^2 + 12x} \\
 -5x - 30 \\
 \underline{-5x - 30} \\
 0
 \end{array}$$

52.

$$\begin{array}{r}
 \overline{) 4x^2 + 0x - 41} \\
 \underline{4x^2 + 14x} \\
 -14x - 41 \\
 \underline{-14x - 49} \\
 8
 \end{array}$$

$$\frac{4x^2 - 41}{2x + 7} = 2x - 7 + \frac{8}{2x + 7}$$

53.

$$\begin{array}{r}
 \overline{) 3x^3 - 7x^2 + 11x - 3} \\
 \underline{3x^3 - x^2} \\
 -6x^2 + 11x \\
 \underline{-6x^2 + 2x} \\
 9x - 3 \\
 \underline{9x - 3} \\
 0
 \end{array}$$

54.

$$\begin{array}{r}
 \overline{) w^3 - 4w^2 + 7w - 12} \\
 \underline{w^3 - 3w^2} \\
 -w^2 + 7w \\
 \underline{-w^2 + 3w} \\
 4w - 12 \\
 \underline{4w - 12} \\
 0
 \end{array}$$

55.

$$\begin{array}{r}
 4x^3 - 2x^2 + 6x \\
 x+3 \overline{) 4x^4 + 10x^3 + 0x^2 + 18x - 1} \\
 \underline{4x^4 + 12x^3} \\
 -2x^3 + 0x^2 \\
 \underline{-2x^3 - 6x^2} \\
 6x^2 + 18x \\
 \underline{6x^2 + 18x} \\
 0x - 1 \\
 \hline
 \frac{4x^4 + 10x^3 + 18x - 1}{x + 3} = 4x^3 - 2x^2 + 6x - \frac{1}{x + 3}
 \end{array}$$

56.

$$\begin{array}{r}
 4x^2 - 6x + 2 \\
 2x+3 \overline{) 8x^3 + 0x^2 - 14x + 3} \\
 \underline{8x^3 + 12x^2} \\
 -12x^2 - 14x \\
 \underline{-12x^2 - 18x} \\
 4x + 3 \\
 \underline{4x + 6} \\
 -3 \\
 \hline
 \frac{8x^3 - 14x + 3}{2x + 3} = 4x^2 - 6x + 2 - \frac{3}{2x + 3}
 \end{array}$$

57.

$$\begin{aligned}
 -3\{(r+s-t) - 2[(3r-2s) - (t-2s)]\} &= -3\{r+s-t - 2[3r-2s-t+2s]\} \\
 &= -3\{r+s-t - 2[3r-t]\} \\
 &= -3\{r+s-t - 6r+2t\} \\
 &= -3\{-5r+s+t\} \\
 &= 15r - 3s - 3t
 \end{aligned}$$

58.

$$\begin{aligned}
 &(1-2x)(x-3) - (x+4)(4-3x) \\
 &= [(1)(x) + (1)(-3) + (-2x)(x) + (-2x)(-3)] - [(x)(4) + (x)(-3x) + (4)(4) + (4)(-3x)] \\
 &= [x - 3 - 2x^2 + 6x] - [4x + -3x^2 + 16 + -12x] \\
 &= [-2x^2 + 7x - 3] - [-3x^2 - 8x + 16] \\
 &= -2x^2 + 7x - 3 + 3x^2 + 8x - 16 \\
 &= x^2 + 15x - 19
 \end{aligned}$$

59.

$$\begin{array}{r}
 y^2 + 5y - 1 \\
 2y - 1 \overline{) 2y^3 + 9y^2 - 7y + 5} \\
 \underline{2y^3 - 1y^2} \\
 10y^2 - 7y \\
 \underline{10y^2 - 5y} \\
 -2y + 5 \\
 \underline{-2y + 1} \\
 4
 \end{array}$$

$$\frac{2y^3 + 9y^2 - 7y + 5}{2y - 1} = y^2 + 5y - 1 + \frac{4}{2y - 1}$$

60.

$$\begin{array}{r}
 3x + 4y \\
 2x - y \overline{) 6x^2 + 5xy - 4y^2} \\
 \underline{6x^2 - 3xy} \\
 8xy - 4y^2 \\
 \underline{8xy - 4y^2} \\
 0
 \end{array}$$

61.

$$\begin{aligned}
 3x + 1 &= x - 8 \\
 2x &= -9 \\
 x &= -\frac{9}{2}
 \end{aligned}$$

62.

$$\begin{aligned}
 4y - 3 &= 5y + 7 \\
 -y &= 10 \\
 y &= -10
 \end{aligned}$$

63.

$$\begin{aligned}
 \frac{5x}{7} &= \frac{3}{2} \\
 2(5x) &= 3(7) \\
 10x &= 21 \\
 x &= \frac{21}{10}
 \end{aligned}$$

64.

$$\frac{2(N-4)}{3} = \frac{5}{4}$$

$$\frac{2N-8}{3} = \frac{5}{4}$$

$$4(2N-8) = 3(5)$$

$$8N-32 = 15$$

$$8N = 47$$

$$N = \frac{47}{8}$$

65.

$$6x-5 = 3(x-4)$$

$$6x-5 = 3x-12$$

$$3x = -7$$

$$x = -\frac{7}{3}$$

66.

$$-2(-4-y) = 3y$$

$$8+2y = 3y$$

$$y = 8$$

67.

$$2s+4(3-s) = 6$$

$$2s+12-4s = 6$$

$$-2s = -6$$

$$s = \frac{-6}{-2}$$

$$s = 3$$

68.

$$2|x|-1 = 3$$

$$2|x| = 4$$

$$|x| = \frac{4}{2}$$

$$|x| = 2$$

$$x = -2 \text{ and } 2$$

69.

$$3t-2(7-t) = 5(2t+1)$$

$$3t-14+2t = 10t+5$$

$$5t-14 = 10t+5$$

$$-5t = 19$$

$$t = -\frac{19}{5}$$

70.

$$-(8-x) = x - 2(2-x)$$

$$-8 + x = x - 4 + 2x$$

$$-8 + x = 3x - 4$$

$$-2x = 4$$

$$x = -\frac{4}{2}$$

$$x = -2$$

71.

$$2.7 + 2.0(2.1x - 3.4) = 0.1$$

$$2.7 + 4.2x - 6.8 = 0.1$$

$$4.2x - 4.1 = 0.1$$

$$4.2x = 4.2$$

$$x = \frac{4.2}{4.2}$$

$$x = 1.0$$

72.

$$0.250(6.721 - 2.44x) = 2.08$$

$$1.68025 - 0.610x = 2.08$$

$$-0.610x = 0.39975$$

$$x = -\frac{0.39975}{0.610}$$

$$x = 0.655327868$$

$$x = 0.655$$

73.

$$\text{(a) } 60\,000\,000\,000 \text{ bytes} = 6 \times 10^{10} \text{ bytes}$$

$$\text{(b) } 60\,000\,000\,000 \text{ bytes} = 60 \times 10^9 \text{ bytes} \\ = 60 \text{ gigabytes}$$

74.

$$\text{(a) } 40\,000 \text{ km/h} = 4 \times 10^4 \text{ km/h}$$

$$\text{(b) } 40\,000 \text{ km/h} = 40 \times 10^3 \text{ km/h} \\ = 40 \times 10^6 \text{ m/h} \\ = 40 \text{ Mm/h}$$

75.

$$\text{(a) } 192\,000\,000 \text{ km} = 1.92 \times 10^8 \text{ km}$$

$$\text{(b) } 192\,000\,000 \text{ km} = 192 \times 10^6 \text{ km} \\ = 192 \times 10^9 \text{ m} \\ = 192 \text{ Gm}$$

76.

$$\text{(a) } 1.02 \times 10^9 \text{ Hz} = 1\,020\,000\,000 \text{ Hz}$$

$$\text{(b) } 1.02 \times 10^9 \text{ Hz} = 1.02 \text{ GHz}$$

77.

(a) $4.05 \times 10^{13} \text{ km} = 40\,500\,000\,000\,000 \text{ km}$

(b) $4.05 \times 10^{13} \text{ km} = 40.5 \times 10^{12} \text{ km}$
 $= 40.5 \times 10^{15} \text{ m}$
 $= 40.5 \text{ Pm}$

(Note that the symbol P stands for peta, which is the SI prefix associated with the multiple 10^{15} .)

78.

(a) $10^6 \text{ m}^2 = 1\,000\,000 \text{ m}^2$

(b) $10^6 \text{ m}^2 = 1 \text{ km}^2$

(Note that these are squared units, so 10^6 is substituted by k.)

79.

(a) $10^{-12} \text{ W/m}^2 = 0.000\,000\,000\,001 \text{ W/m}^2$

(b) $10^{-12} \text{ W/m}^2 = 1 \text{ pW/m}^2$

80.

(a) $0.000\,000\,15 \text{ m} = 1.5 \times 10^{-7} \text{ m}$

(b) $0.000\,000\,15 \text{ m} = 150 \times 10^{-9} \text{ m}$
 $= 150 \text{ nm}$

81.

(a) $1.5 \times 10^{-1} \text{ Bq/L} = 0.15 \text{ Bq/L}$

(b) $1.5 \times 10^{-1} \text{ Bq/L} = 150 \times 10^{-3} \text{ mBq/L}$

82.

(a) $0.000\,000\,18 \text{ m} = 1.8 \times 10^{-7} \text{ m}$

(b) $0.000\,000\,18 \text{ m} = 180 \times 10^{-9} \text{ m}$
 $= 180 \text{ nm}$

83.

$$R = n^2 Z$$

$$Z = \frac{R}{n^2}$$

84.

$$R = \frac{2GM}{c^2}$$

$$c^2 R = 2GM$$

$$G = \frac{c^2 R}{2M}$$

85.

$$P = \frac{\pi^2 EI}{L^2}$$

$$L^2 P = \pi^2 EI$$

$$E = \frac{L^2 P}{\pi^2 I}$$

86.

$$f = p(c-1) - c(p-1)$$

$$f = cp - p - cp + c$$

$$f - c = -p$$

$$p = c - f$$

87.

$$Pp + Qq = Rr$$

$$Qq = Rr - Pp$$

$$q = \frac{Rr - Pp}{Q}$$

88.

$$V = IR + Ir$$

$$IR = V - Ir$$

$$R = \frac{V - Ir}{I}$$

89.

$$d = (n-1)A$$

$$d = An - A$$

$$d + A = An$$

$$n = \frac{d + A}{A}$$

90.

$$mu = (m + M)v$$

$$mu = mv + Mv$$

$$mu - mv = Mv$$

$$M = \frac{mu - mv}{v}$$

91.

$$N_1 = T(N_2 - N_3) + N_3$$

$$N_1 - N_3 = N_2T - N_3T$$

$$N_2T = N_1 - N_3 + N_3T$$

$$N_2 = \frac{N_1 - N_3 + N_3T}{T}$$

92.

$$q = \frac{KA(B-C)}{L}$$

$$Lq = ABK - ACK$$

$$ABK = Lq + ACK$$

$$B = \frac{Lq + ACK}{AK}$$

93.

$$R = \frac{A(T_2 - T_1)}{H}$$

$$HR = AT_2 - AT_1$$

$$AT_2 = HR + AT_1$$

$$T_2 = \frac{HR + AT_1}{A}$$

94.

$$Z^2 \left(1 - \frac{\lambda}{2a} \right) = k$$

$$Z^2 - \frac{Z^2 \lambda}{2a} = k$$

$$Z^2 - k = \frac{Z^2 \lambda}{2a}$$

$$2a(Z^2 - k) = Z^2 \lambda$$

$$\lambda = \frac{2aZ^2 - 2ak}{Z^2}$$

95.

$$d = kx^2[3(a+b) - x]$$

$$d = kx^2[3a + 3b - x]$$

$$d = 3akx^2 + 3bkx^2 - kx^3$$

$$3akx^2 = d - 3bkx^2 + kx^3$$

$$a = \frac{d - 3bkx^2 + kx^3}{3kx^2}$$

96.

$$V = V_0[1 + 3a(T_2 - T_1)]$$

$$V = V_0[1 + 3aT_2 - 3aT_1]$$

$$V = V_0 + 3aT_2V_0 - 3aT_1V_0$$

$$3aT_2V_0 = V - V_0 + 3aT_1V_0$$

$$T_2 = \frac{V - V_0 + 3aT_1V_0}{3aV_0}$$

97.

$$\frac{5.25 \times 10^{10} \text{ bytes}}{6.4 \times 10^4 \text{ bytes}} = 82\,0312.5$$

which rounds to 8.2×10^5 . The newer computer's memory is 8.2×10^5 larger.

98.

$$t = 0.45\sqrt{22} = 2.110687092 \text{ s}$$

which rounds to 2.1 s. It would take the person 2.1 s to fall 22 m.

99.

$$\frac{0.533 \text{ km}}{0.443 \text{ km}} = 1.203160271$$

which rounds to 1.20. The CN Tower is 1.20 times taller than the Sears tower.

100.

$$t = \left(\frac{48 \text{ cells}}{2650} \right)^2 = (0.018113207)^2 = 0.000328088 \text{ s}$$

which rounds to 3.28×10^{-4} s. It would take the computer 3.28×10^{-4} s to check 48 memory cells.

101.

$$\begin{aligned} \frac{R_1 R_2}{R_1 + R_2} &= \frac{(0.0275 \Omega)(0.0590 \Omega)}{0.0275 \Omega + 0.0590 \Omega} \\ &= \frac{0.0016225 \Omega^2}{0.0865 \Omega} \\ &= 0.018757225 \Omega \end{aligned}$$

which rounds to 0.0188Ω . The combined electric resistance is 0.0188Ω .

102.

$$\begin{aligned} 1.5 \times 10^{11} \sqrt{\frac{m}{M}} &= 1.5 \times 10^{11} \sqrt{\frac{5.98 \times 10^{24} \text{ kg}}{1.99 \times 10^{30} \text{ kg}}} \\ &= 1.5 \times 10^{11} \sqrt{0.000003005} \\ &= 1.5 \times 10^{11} (0.0017335) \\ &= 260\,025\,124.4 \text{ m} \end{aligned}$$

which rounds to 2.6×10^8 m. The distance the space craft will be from the earth is 2.6×10^8 m.

103.

$$\begin{aligned} (x - 2a) + 100 \text{ cm/m}(x + 2a) &= x - 2a + 100(x) + 100(2a) \\ &= x - 2a + 100x + 200a \\ &= 101x + 198a \end{aligned}$$

The sum of their length is $101x + 198a$ cm.

104.

$$\begin{aligned} (Ai - R)(1 + i)^2 &= (Ai - R)(1 + i)(1 + i) \\ &= (Ai - R)[(1)(1) + (1)(i) + (i)(1) + (i)(i)] \\ &= (Ai - R)[i^2 + 2i + 1] \\ &= (Ai)(i^2) + (Ai)(2i) + (Ai)(1) + (-R)(i^2) + (-R)(2i) + (-R)(1) \\ &= Ai^3 + 2Ai^2 + Ai - i^2R - 2iR - R \end{aligned}$$

105.

$$\begin{aligned} 4(t + h) - 2(t + h)^2 &= 4t + 4h - 2(t + h)(t + h) \\ &= 4t + 4h - 2[(t)(t) + (t)(h) + (h)(t) + (h)(h)] \\ &= 4t + 4h - 2[t^2 + 2ht + h^2] \\ &= 4t + 4h - 2t^2 - 4ht - 2h^2 \\ &= -2t^2 - 2h^2 - 4ht + 4t + 4h \end{aligned}$$

106.

$$\begin{aligned}\frac{k^2r - 2h^2k + h^2rv^2}{k^2r} &= \frac{k^2r}{k^2r} - \frac{2h^2k}{k^2r} + \frac{h^2rv^2}{k^2r} \\ &= \frac{\cancel{k^2}r}{\cancel{k^2}r} - \frac{2h^2}{k^{2-1}r} + \frac{h^2\cancel{r}v^2}{k^2\cancel{r}} \\ &= 1 - \frac{2h^2}{kr} + \frac{h^2v^2}{k^2}\end{aligned}$$

107.

$$3 \times 18 \div (9 - 6) = 54 \div (3) = 18$$

$$3 \times 18 \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$$

Yes, the removal of the parentheses does affect the answer.

108.

$$(3 \times 18) \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$$

$$3 \times 18 \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$$

No, the removal of the parentheses does not affect the answer.

109.

$$x - (3 - x) = 2x - 3$$

$$x - 3 + x = 2x - 3$$

$$2x - 3 = 2x - 3$$

The equation is valid for all values of the unknown, so the equation is an identity.

110.

$$7 - (2 - x) = x + 2$$

$$7 - 2 + x = x + 2$$

$$x + 5 = x + 2$$

$$5 = 2$$

The equation has no values of the unknown for which it is valid, so the equation is a contradiction.

111.

$$\begin{aligned}(x - y)^3 &= (x - y)(x - y)(x - y) \\ &= -(y - x)(-(y - x))(-(y - x)) \\ &= -(y - x)(y - x)(y - x) \\ &= -(y - x)^3\end{aligned}$$

112.

$$(a \div b) \div c \neq a \div (b \div c)$$

$$(8 \div 4) \div 2 = 2 \div 2 = 1$$

$$8 \div (4 \div 2) = 8 \div 2 = 4$$

Division is not associative.

113.

$$\frac{8 \times 10^{-3}}{2 \times 10^4} = 4 \times 10^{-7}$$

114.

$$\frac{\sqrt{4+36}}{\sqrt{4}} = \frac{\sqrt{(2)(2)(10)}}{2} = \frac{2\sqrt{10}}{2} = \sqrt{10}$$

115.Let x = the cost of the first computer program.Let $x + \$72$ = the cost of the second computer program.

$$x + (x + \$72) = \$190$$

$$2x + \$72 = \$190$$

$$2x = \$118$$

$$x = \frac{\$118}{2}$$

$$x = \$59$$

The cost of the first computer program is \$59, and the other program costs $(\$59 + \$72) = \$131$.Check: $\$59 + \$131 = 190$ **116.**Let x = the cost to run the commercial on the first station.Let $x + \$1100$ = the cost to run the commercial on the second station.

$$x + (x + \$1100) = \$9500$$

$$2x + \$1100 = \$9500$$

$$2x = \$8400$$

$$x = \frac{\$8400}{2}$$

$$x = \$4200$$

The cost of the run the commercial on the first station is \$4200, and the cost for the other station is $(\$4200 + \$1100) = \$5300$.Check: $\$4200 + \$5300 = \$9500$ **117.**Let $2x$ = the amount of oxygen produced in cm^3 by the first reaction.Let x = the amount of oxygen produced in cm^3 by the second reaction.Let $4x$ = the amount of oxygen produced in cm^3 by the third reaction.

$$2x + x + 4x = 560 \text{ cm}^3$$

$$7x = 560 \text{ cm}^3$$

$$x = \frac{560 \text{ cm}^3}{7}$$

$$x = 80 \text{ cm}^3$$

The first reaction produces $(2 \times 80 \text{ cm}^3) = 160 \text{ cm}^3$ of oxygen, the second reaction produces 80 cm^3 of oxygen, and the third reaction produces $(4 \times 80 \text{ cm}^3) = 320 \text{ cm}^3$ of oxygen.Check: $160 \text{ cm}^3 + 80 \text{ cm}^3 + 320 \text{ cm}^3 = 560 \text{ cm}^3$

118.

Let x = the speed that the river is flowing in km/h.

Let $x + 5.5$ km/h = the speed that the boat travels downstream.

Let $-x + 5.5$ km/h = the speed that the boat travels upstream.

The distance that the boat travelled is the same in both experiments. Distance = speed \times time.

$$(x + 5.5 \text{ km/h})(5.0 \text{ h}) = (-x + 5.5 \text{ km/h})(8.0 \text{ h})$$

$$(5.0 \text{ h})(x) + (5.5 \text{ km/h})(5.0 \text{ h}) = (8.0 \text{ h})(-x) + (5.5 \text{ km/h})(8.0 \text{ h})$$

$$(5.0 \text{ h})(x) + (27.5 \text{ km}) = (-8.0 \text{ h})(x) + (44 \text{ km})$$

$$(13.0 \text{ h})x = 16.5 \text{ km}$$

$$x = \frac{16.5 \text{ km}}{13 \text{ h}}$$

$$x = 1.269230769 \text{ km/h}$$

which rounds to 1.3 km/h. The polluted stream is flowing at 1.3 km/h.

Check:

$$(1.269230769 \text{ km/h} + 5.5 \text{ km/h})(5.0 \text{ h}) = (-1.269230769 \text{ km/h} + 5.5 \text{ km/h})(8.0 \text{ h})$$

$$(6.769230769 \text{ km/h})(5.0 \text{ h}) = (4.2 \text{ km/h})(8.0 \text{ h})$$

$$(33.8 \text{ km}) = (33.8 \text{ km})$$

119.

Let x = the resistance in the first resistor in Ω .

Let $x + 1200 \Omega$ = the resistance in the second resistor in Ω .

Voltage = current \times resistance. $2.4 \mu\text{A} = 2.4 \times 10^{-6} \text{ A}$. $12 \text{ mV} = 0.0120 \text{ V}$

$$(2.4 \times 10^{-6} \text{ A})(x) + (2.4 \times 10^{-6} \text{ A})(x + 1200 \Omega) = 0.0120 \text{ V}$$

$$(2.4 \times 10^{-6} \text{ A})(x) + (2.4 \times 10^{-6} \text{ A})(x) + (2.4 \times 10^{-6} \text{ A})(1200 \Omega) = 0.0120 \text{ V}$$

$$(4.8 \times 10^{-6} \text{ A})(x) + (0.00288 \text{ V}) = 0.0120 \text{ V}$$

$$(4.0 \times 10^{-6} \text{ A})(x) = 0.00912 \text{ V}$$

$$x = \frac{0.00912 \text{ V}}{4.8 \times 10^{-6} \text{ A}}$$

$$x = 1900 \Omega$$

The first resistor's resistance is 1900Ω and the second resistor's is $(1900 \Omega + 1200 \Omega) = 3100 \Omega$.

Check:

$$(2.4 \times 10^{-6} \text{ A})(1900 \Omega) + (2.4 \times 10^{-6} \text{ A})(1900 \Omega + 1200 \Omega) = 0.0120 \text{ V}$$

$$0.00456 \text{ V} + 0.00744 \text{ V} = 0.0120 \text{ V}$$

$$0.0120 \text{ V} = 0.0120 \text{ V}$$

120.

Let x = the concentration of the first pollutant in ppm.

Let $4x$ = the concentration of the second pollutant in ppm.

$$x + 4x = 4.0 \text{ ppm}$$

$$5x = 4.0 \text{ ppm}$$

$$x = \frac{4.0 \text{ ppm}}{5}$$

$$x = 0.8 \text{ ppm}$$

The concentration of the first pollutant is 0.8 ppm, and the concentration of the second is $(4 \times 0.8 \text{ ppm}) = 3.2 \text{ ppm}$.

Check:

$$0.8 \text{ ppm} + 4(0.8 \text{ ppm}) = 4.0 \text{ ppm}$$

$$0.8 \text{ ppm} + 3.2 \text{ ppm} = 4.0 \text{ ppm}$$

$$4.0 \text{ ppm} = 4.0 \text{ ppm}$$

121.

Let x = the time taken in hours for the crew to build 250 m of road.

The crew works at a rate of 450 m/12 h, which is 37.5 m/h. Time = distance / speed.

$$x = \frac{250 \text{ m}}{37.5 \text{ m/h}}$$

$$x = 6.666666667 \text{ h}$$

which rounds to 6.7 h.

122.

Let x = the amount of oil in L in the mixture.

Let $15x$ = the amount of gas in L in the mixture.

$$x + 15x = 6.6 \text{ L}$$

$$16x = 6.6 \text{ L}$$

$$x = \frac{6.6 \text{ L}}{16}$$

$$x = 0.4125 \text{ L}$$

which rounds to 0.41 L. There is 0.41 L of oil in the mixture and $(15 \times 0.41 \text{ L}) = 6.2 \text{ L}$ of gas.

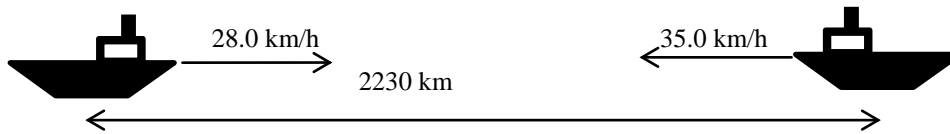
Check:

$$0.4125 \text{ L} + 15(0.4125 \text{ L}) = 6.6 \text{ L}$$

$$0.4125 \text{ L} + 6.1875 \text{ L} = 6.6 \text{ L}$$

$$6.6 \text{ L} = 6.6 \text{ L}$$

123.



Let x = the time taken by the second ship in hours.

Let $x + 2 \text{ h}$ = the amount time taken by the first ship in hours.

The distance travelled adds up to 2230km. Distance = speed \times time.

$$35.0 \text{ km/h}(x) + 28.0 \text{ km/h}(x + 2 \text{ h}) = 2230 \text{ km}$$

$$35.0 \text{ km/h}(x) + 28.0 \text{ km/h}(x) + 28.0 \text{ km/h}(2 \text{ h}) = 2230 \text{ km}$$

$$63.0 \text{ km/h}(x) + 56.0 \text{ km} = 2230 \text{ km}$$

$$63.0 \text{ km/h}(x) = 2174 \text{ km}$$

$$x = \frac{2174 \text{ km}}{63.0 \text{ km/h}}$$

$$x = 34.50793651 \text{ h}$$

which rounds to 34.5 h. The ships will pass 34.5 h after the second ship enters the canal.

Check:

$$35.0 \text{ km/h}(34.50793651 \text{ h}) + 28.0 \text{ km/h}(34.50793651 \text{ h} + 2 \text{ h}) = 2230 \text{ km}$$

$$1207.777778 \text{ km} + 1022.222222 \text{ km} = 2230 \text{ km}$$

$$2230 \text{ km} = 2230 \text{ km}$$

124.Let x = the time take in h for the helicopter to travel from the pond to the fire.Let $0.5 \text{ h} - x$ = the time take in h for the helicopter to travel from the fire to the pond.30 min / 60 min/h = 0.5 h. The distance travelled by the helicopter is the same for both trips. Distance = speed \times time.

$$175.0 \text{ km/h}(0.5 \text{ h} - x) = 115.0 \text{ km/h}(x)$$

$$87.5 \text{ km} - 175.0 \text{ km/h}(x) = 115.0 \text{ km/h}(x)$$

$$87.5 \text{ km} = 290 \text{ km/h}(x)$$

$$x = \frac{87.5 \text{ km}}{290 \text{ km/h}}$$

$$x = 0.301724137 \text{ h}$$

which rounds to 0.30 h. It will take the helicopter 0.30 h to fly from the pond to the fire.

Check:

$$175.0 \text{ km/h}(0.5 \text{ h} - 0.301724137 \text{ h}) = 115.0 \text{ km/h}(0.301724137 \text{ h})$$

$$34.69827 \text{ km} = 34.69827 \text{ km}$$

125.Let x = the number of litres of 0.50% grade oil used.Let $1000 \text{ L} - x$ the number of litres of 0.75% grade oil used.

$$0.005(x) + 0.0075(1000 \text{ L} - x) = 0.0065(1000 \text{ L})$$

$$0.005(x) + 7.5 \text{ L} - 0.0075(x) = 6.5 \text{ L}$$

$$-0.0025(x) = -1.0 \text{ L}$$

$$x = \frac{-1.0 \text{ L}}{-0.0025}$$

$$x = 400 \text{ L}$$

It will take 400 L of the 0.50% grade oil and $(1000 \text{ L} - 400 \text{ L}) = 600 \text{ L}$ of the 0.75% grade oil to make 1000 L of 0.65% grade oil.

Check:

$$0.005(400 \text{ L}) + 0.0075(1000 \text{ L} - 400 \text{ L}) = 0.0065(1000 \text{ L})$$

$$2 \text{ L} + 4.5 \text{ L} = 6.5 \text{ L}$$

$$6.5 \text{ L} = 6.5 \text{ L}$$

126.Let x = the number of mL of water added.Let $x + 20 \text{ mL}$ = the resulting number of mL in the 45% saline solution.

$$0.60(20 \text{ mL}) = 0.45(x + 20 \text{ mL})$$

$$12 \text{ mL} = 0.45(x) + 9 \text{ mL}$$

$$3 \text{ mL} = 0.45(x)$$

$$x = \frac{3 \text{ mL}}{0.45}$$

$$x = 6.666666667 \text{ mL}$$

which rounds to 6.67 mL. It will take 6.67 mL of water to make the 45% saline solution.

Check:

$$0.60(20 \text{ mL}) = 0.45(6.666666667 \text{ mL} + 20 \text{ mL})$$

$$12 \text{ mL} = 0.45(26.666666667 \text{ mL})$$

$$12 \text{ mL} = 12 \text{ mL}$$

127.Let x = the area of space in m^2 in the kitchen and bath.

$$\frac{\text{m}^2 \text{ of tile in the house}}{\text{m}^2 \text{ in the house}} = 0.25$$

$$\frac{x + 0.15(205 \text{ m}^2)}{(x + 205 \text{ m}^2)} = 0.25$$

$$x + 30.75 \text{ m}^2 = 0.25(x) + (0.25)(205 \text{ m}^2)$$

$$x + 30.75 \text{ m}^2 = 0.25(x) + 51.25 \text{ m}^2$$

$$0.75x = 20.5 \text{ m}^2$$

$$x = \frac{20.5 \text{ m}^2}{0.75}$$

$$x = 27.33333333 \text{ m}^2$$

which rounds to 27 m^2 . The kitchen and bath area is 27 m^2 .

Check:

$$\frac{27.33333333 \text{ m}^2 + 0.15(205 \text{ m}^2)}{(27.33333333 \text{ m}^2 + 205 \text{ m}^2)} = 0.25$$

$$\frac{58.08333333 \text{ m}^2}{232.33333333 \text{ m}^2} = 0.25$$

$$0.25 = 0.25$$

128.Let x = the number of grams of 9-karat gold.Let $200 \text{ g} - x$ = the number of grams of 18-karat gold. 9-karat gold is $9/24$ gold = 0.375 , 18-karat gold is $18/24$ gold = 0.75 , and 14-karat gold is $14/24$ gold = 0.583333333 .

$$0.375(x) + 0.75(200 \text{ g} - x) = 0.583333333(200 \text{ g})$$

$$0.375(x) + 150 \text{ g} - 0.75(x) = 116.6666666 \text{ g}$$

$$-0.375(x) = -33.3333334 \text{ g}$$

$$x = \frac{-33.3333334 \text{ g}}{-0.375}$$

$$x = 88.88888907 \text{ g}$$

which rounds to 89 g . There is 89 g of 9-karat gold and $(200 \text{ g} - 89 \text{ g}) = 111 \text{ g}$ of 18-karat gold needed to make 200 g of 14-karat gold.

Check:

$$0.375(88.88888907 \text{ g}) + 0.75(200 \text{ g} - 88.88888907 \text{ g}) = 0.583333333(200 \text{ g})$$

$$33.3333334 \text{ g} + 83.3333332 \text{ g} = 116.6666666 \text{ g}$$

$$116.6666666 \text{ g} = 116.6666666 \text{ g}$$

129.

$$P = P_0 + P_0rt$$

$$P - P_0 = P_0rt$$

$$r = \frac{P - P_0}{P_0t}$$

$$r = \frac{\$7625 - \$6250}{\$6250(4.000 \text{ years})}$$

$$r = \frac{\$1375}{25\,000}$$

$$r = 0.055$$

The rate is equal to 5.500%.

On the calculator type:

$$(7625 - 6250) / (6250 \times 4.000)$$